

2000 July Lecture

## QUANTUM COMPUTING: New beads on the abacus

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## Classical Physics / Quantum Physics

**Classical Physics**

- Everyday experience
- Big objects we can look at
- Everything is smooth, continuous and sharp
- The scale of humans

**Quantum Physics**

- Only in the last 100 years
- Objects as small as molecules, atoms and below
- Everything is indivisibly packaged
- Things are blurry, move in jumps

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## Classical computing: Moore's Law

The remarkable development of computers

- Gordon Moore:
  - in 1965 was Director of Fairchild Semiconductor
  - made a 32 transistor integrated circuit one year
  - 64 the next
- "The number of transistors (and hence computer power) doubles every 18 months to two years"
- (Now making one transistor per ant per year -  $10^{17}$  ants on Earth)

Motorola Power PC 620 Chip  
7 million transistors  
(ancient relic)

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## The end of Moore's law

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## The end of Moore's law?

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## The end of Moore's Law!

- As electronic devices shrink, soon there will be just a few electrons in each device
- Electric currents become erratic!

Large device, current is average of many electrons

Small device, current of one electron

ON OFF

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### Classical Computers

- Prospects for the future
- Cannot get indefinite speed increases by indefinite miniaturisation
- Can get some advantages from parallel processors (more than one computer chip working together)
- BUT: Some problems will always be difficult for classical computers
- One class of these problems involves the factoring of large numbers into prime factors

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### Factorizing Large Numbers

- Essential for security of transactions over the internet ("RSA security"), etc
- Example:
  - $127 \times 129 = ?$  Easy! A few minutes
  - $? \times ? = 29083$  Hard! Maybe an hour
  - "hardness" of factorizing large numbers is the key to internet security
- Best supercomputers today can manage a 140 digit number
- What about a 500 digit number? - Forget it!

REMEMBER: Fundamentally, we do not live in a classical world!  
Enter the Quantum Computer

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### The Quantum Computer

What can a quantum computer do?

- Quantum computers do the factorization problem  $10^8$  times faster than conventional computers
- Searching through long lists
- Quantum encryption for secure information exchange
- Solving chemical and biological structures
- Modelling the real (quantum) world
- How is this done?

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### The Quantum Computer

Use quantum particles as the bits in a quantum computer!

- Conventional computer memory states:
 

1

0

1

1

1

0

0

1

1

0

...

binary bits
- Quantum computer memory states:
 

D

Q

D

D

D

Q

Q

D

Q

Q

...

binary *qubits*

  - A quantum computer memory can occupy all possible states at the one time
  - The solution to the problem appears in the final state of the computer when the state of the qubits are read out
  - What can we use as qubits?

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### Essential Quantum Mechanics

We need to get a feel for these non-classical attributes:

- The art of being in two places at the one time
- Occupying two states simultaneously
- Entanglement
- "Spooky action at a distance"

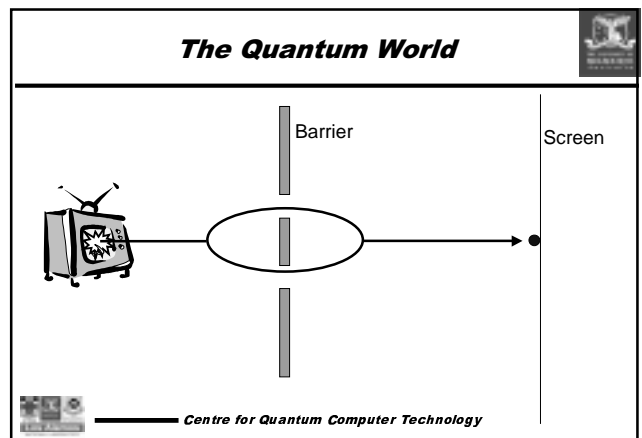
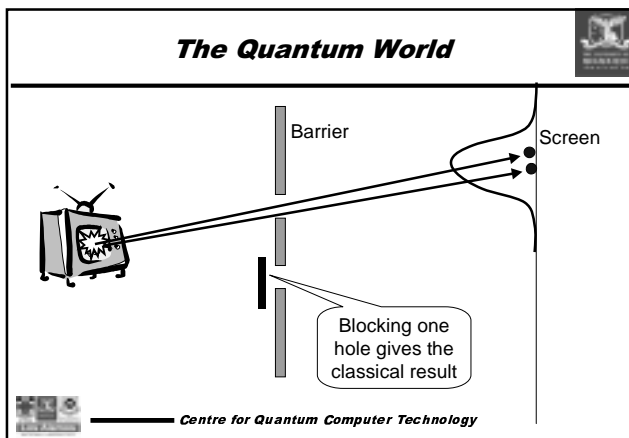
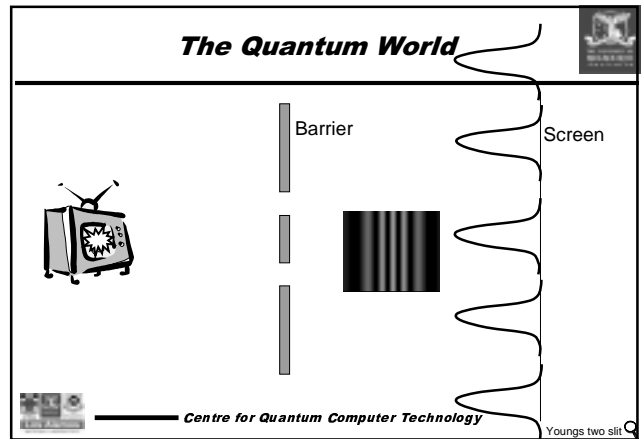
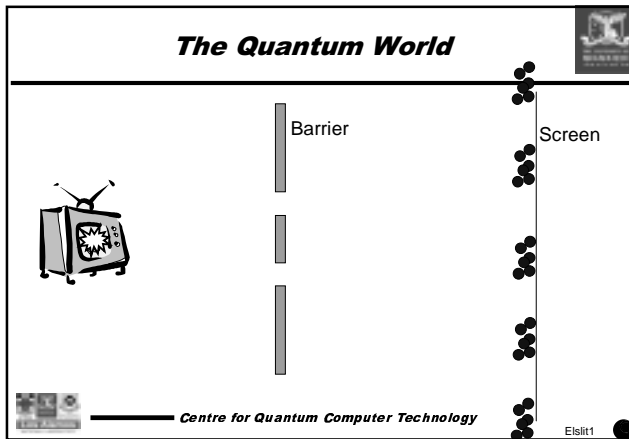
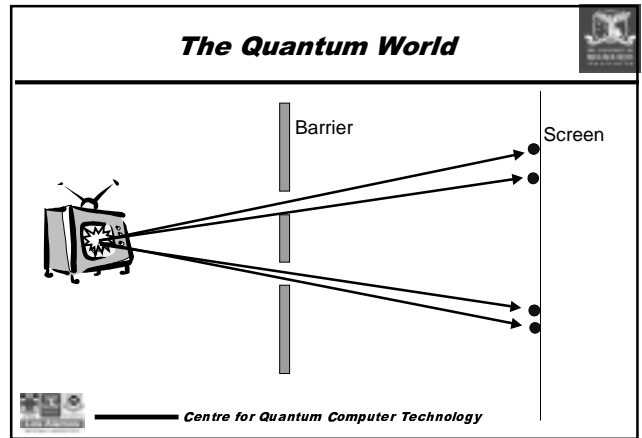
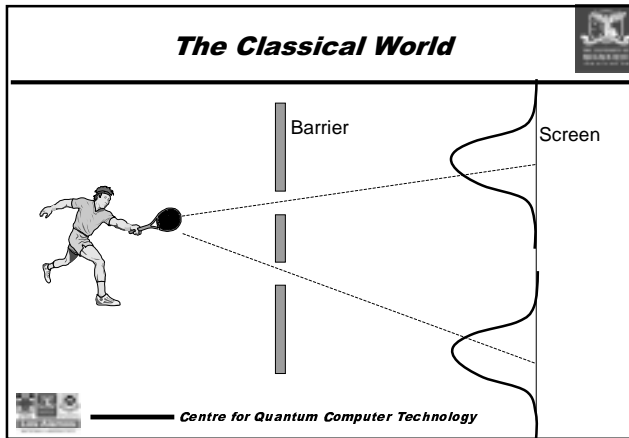
\*A. Einstein

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### The Classical World

The diagram shows a person on the left throwing a ball towards a vertical barrier. The ball hits the barrier and bounces back. On the right, there is a vertical screen. Multiple arrows represent the ball's possible paths after hitting the barrier, but only one path is shown as a solid line, indicating that in the classical world, the ball's position is determined at the moment of impact.

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### The Quantum World

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### The Quantum World

First Result

- Can probe for holes in a screen with a *large number of classical particles* (one particle for each point on the screen)
- Can probe for holes in a screen with *one quantum particle!*
- The "wave function" collapses to a particle when measured
- Quantum objects can do many things at once
- But there is more: Entanglement

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### Entanglement

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### Entanglement

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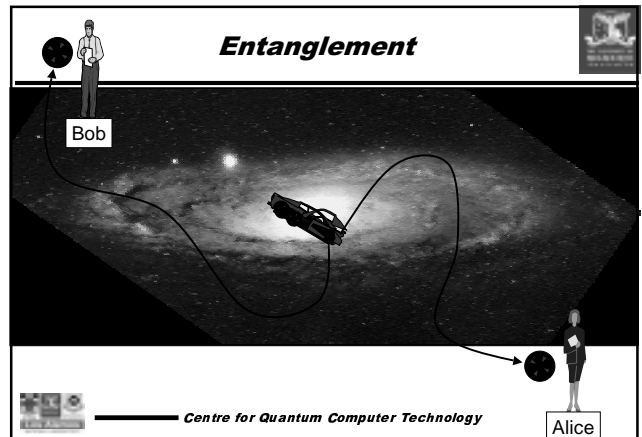
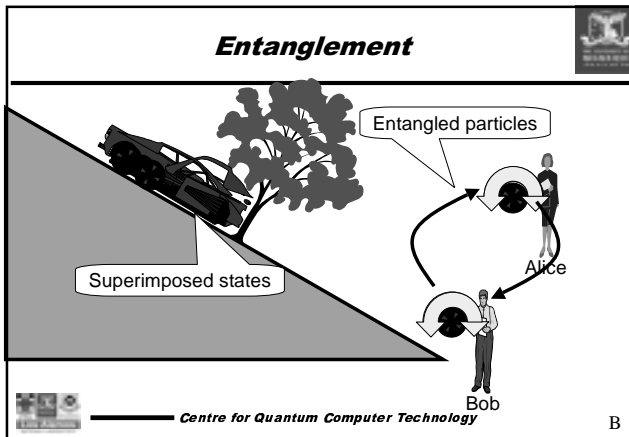
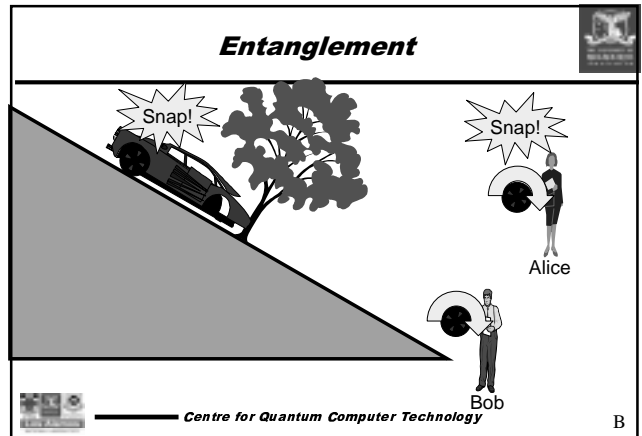
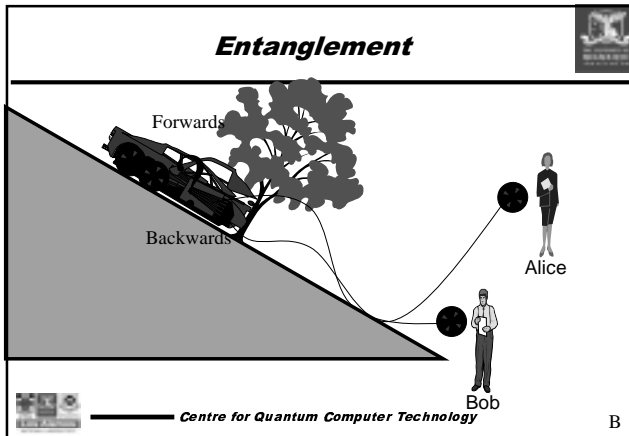
### Entanglement

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### Entanglement

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1



**The Quantum World**

Second Result

- Quantum objects can exist in *two superimposed (entangled) states*
- This superimposed state can *collapse* into a definite state upon measurement
- Entangled particles can be created that retain the superimposed state until measurement

• But how do we use this for quantum computing?

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**Magnetic Resonance**

Sub-atomic particles *spin*! Look at the proton:

- A spinning charged particle acts like a tiny loop of electric current
- This produces a magnetic field
- So the spinning particle is like a tiny bar magnet

$\mu_o = iA$

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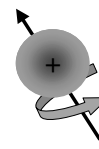
### Magnetic Resonance

Magnetic moments

- The strength of the equivalent magnet depends of the "speed" of the spin and the "size" of the particle
- This is measured by the dipole moment,  $\mu$

Some examples:

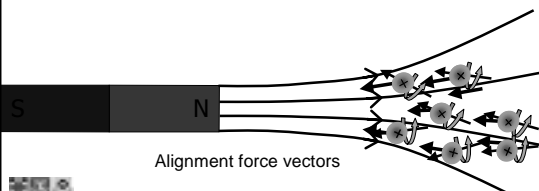
Particle	Dipole moment, $\mu$ (Joule/Tesla)
Small Bar Magnet	5
Earth	$8 \times 10^{22}$
Proton	$1.4 \times 10^{-26}$
Neutron	(1/2.8)proton
Electron	$9.3 \times 10^{-24} = 660\text{proton}$



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### Magnetic Resonance

Spinning charged particles can be lined up with an external magnetic field



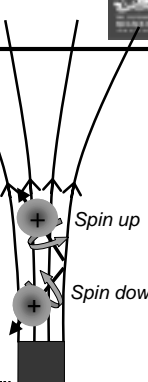
Alignment force vectors

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### Magnetic Resonance

Space Quantisation

- Like many other properties, *space itself is quantised*
- The spinning particles cannot have arbitrary orientations in space relative to the external magnetic field
- The allowed orientations depend on the amount of spin
- For protons and electrons, there are *only two allowed orientations*
- (This is a *spin-half* particle)



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### Magnetic Resonance

Spinning subatomic particles are quantum particles

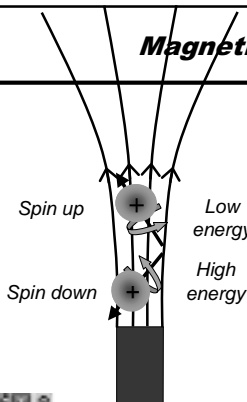
- The spin orientation are two different quantum states
- Before measurement*, the spin orientation can be in two (spin 1/2) directions at the same time - *superimposed states*
- Upon measurement, the spin is found to point in a definite direction - *wavefunction collapse*
- Just what we need for a quantum computer!*
- To program this computer, we need energy

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### Magnetic Resonance

Orientation and energy

- The spin down state is not at equilibrium
- The magnetic field twists the spin vector into alignment
- (Precise alignment is prevented by space quantisation)



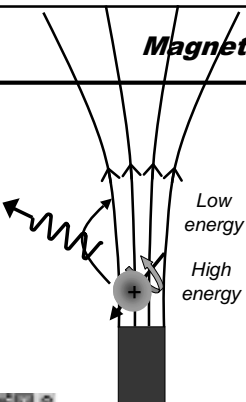
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Classical magnet

### Magnetic Resonance

Change orientations

- The high energy state will spontaneously relax back to the low energy state, releasing energy



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### Magnetic Resonance

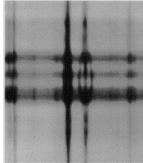
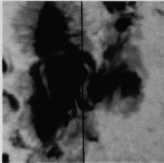
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**Change orientations**

- The high energy state will spontaneously relax back to the low energy state, releasing energy
- The low energy state can absorb energy and flip to the high energy state

### Magnetic Resonance: Zeeman Effect

- Excited mercury vapour emits light owing to electrons jumping up and down between energy levels
- A magnetic field placed around the vapour splits the energy levels and causes small changes in the colour of the light
- These changes can be detected with a sensitive spectrometer
- Can also see the effect in sunspots...

Spectrometer      Photograph

Zeeman Effect

### Magnetic Resonance

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**Assign qubits**

Qubit	Classical equivalent
$ 1\rangle$	1
$ 0\rangle$	0

$|10\rangle$   
(No classical equivalent!  
1 and 0 simultaneously!)

### The Kane Quantum Computer

We are now ready to commence construction:

- "A Silicon-based nuclear spin quantum computer" by B. E. Kane, *Nature*, May 14, 1998
- Proposes a device that:
  - encodes qubits as the orientation of spinning nuclei
  - provides entanglement by means of electron clouds
  - is constructed in silicon like conventional computers
- Will use a block of pure  $^{28}\text{Si}$  (spin-zero nucleus)
- Will use atoms of phosphorous ( $^{31}\text{P}$ ) to carry the spins

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### The Kane Quantum Computer

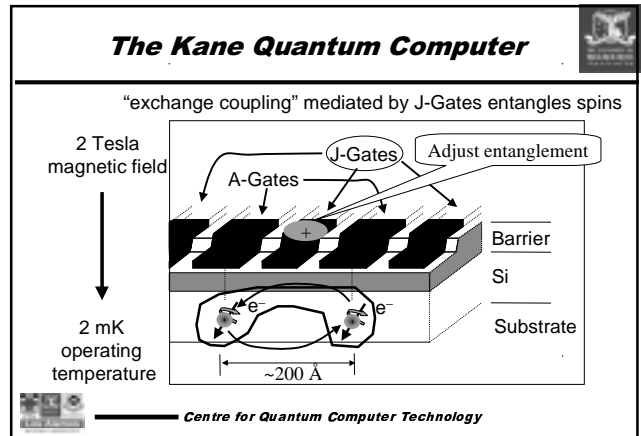
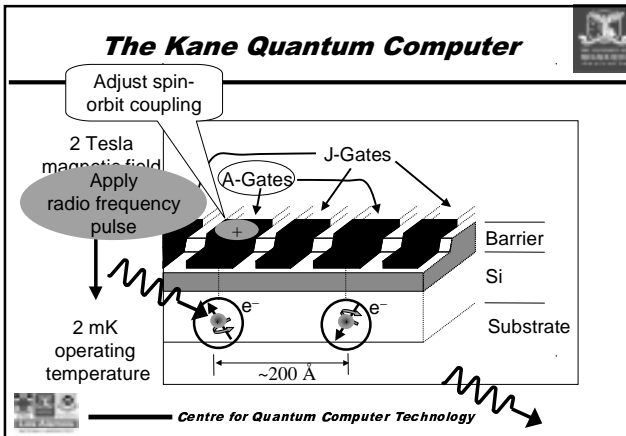
- Close-up of a phosphorous atom (not to scale)

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Snapshot at 2 mK (-273°C)

### The Kane Quantum Computer

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### The Kane Quantum Computer

Operating sequence summary:

- Initialise nuclear spins by means of A-Gates and NMR pulses
- Commence "computation" by entangling nuclear spins through J-Gates and spin-orbit coupling
- Read final state of spins by means of a single electron transistor
- Final state is the equivalent to the diffraction pattern in the two slit experiment

SPIN READOUT

Si

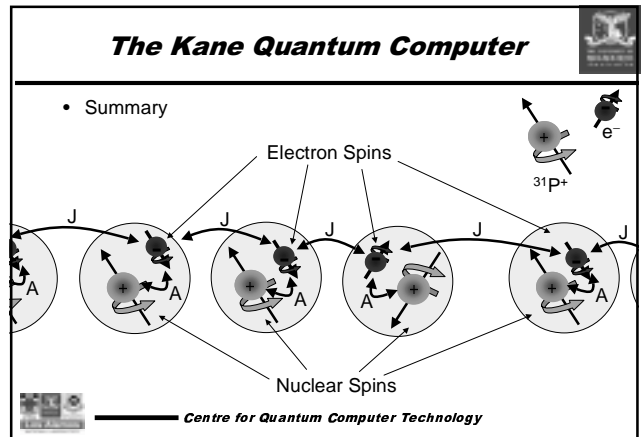
P

P

e<sup>-</sup>

e<sup>+</sup>

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### Fabrication Pathways

Who is going to make this?

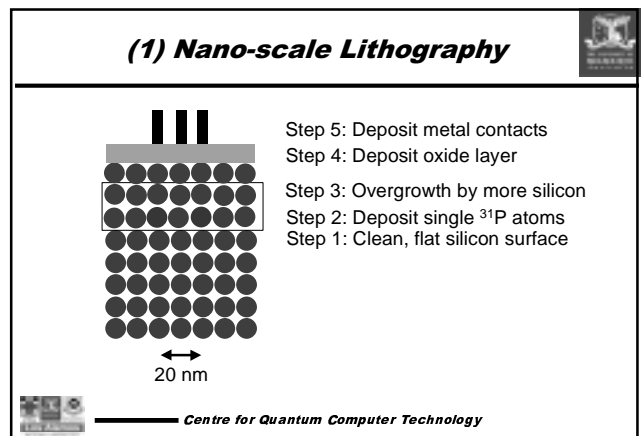
We are!

- Semiconductor National Nanofabrication (SNF) Laboratory, School of Physics, University of New South Wales
- Microanalytical Research Centre, School of Physics, University of Melbourne
- Laser Physics Centre, Department of Physics, University of Queensland
- Los Alamos National Laboratories, U.S.A.

Fabrication strategies:

- (1) Nano-scale lithography:
- (2) Direct <sup>31</sup>P ion implantation

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### (1) Nano-scale Lithography

- Electron beam lithography at the University of New South Wales

Sub-300Å AuPd gates on GaAs

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### (1) Nano-scale Lithography

- Scanning Tunneling Microscope with silicon crystal growth capabilities at the UNSW

Image of individual atoms on silicon surface

- 25K - 1500K Variable T
- 3-Chamber UHV
- Plus: Si-MBE, RHEED, LEED, Auger

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### (2) Alternative Fabrication Pathway

Difficulties:

- Must place  $^{31}\text{P}$  to a precision of a few billionths of a metre
- Having done that, need to come back and add metal electrodes on the buried  $^{31}\text{P}$  atoms for the gates
- The  $^{31}\text{P}$  must not move about while doing this

An alternative strategy:

- Direct  $^{31}\text{P}$  ion implantation
- Can create templates for electrodes automatically

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### (2) Direct $^{31}\text{P}$ ion implantation

Electron irradiation: 30 keV e<sup>-</sup>, 60 keV e<sup>-</sup>

Ion irradiation: 2 MeV He<sup>+</sup>

Scale bars: 10 µm, 5 µm, 0.5 µm

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### (2) Direct $^{31}\text{P}$ ion implantation

- Single MeV heavy ions produce latent damage
- Etching in NaOH devel damage to produce pit
- Light ions produce sma

1. Irradiate, 2. Latent damage

The plastic helmet used by astronaut James Lovell during the Apollo 8 mission and (right) silicone rubber replicas of etched cosmic ray tracks from the helmets of the Apollo 12 astronauts. The tracks are about one-fiftieth of an inch long.

Scale bars: 1 µm intervals

From: B.E. Fischer, Nucl. Instr. Meth. B54 (1991) 401.

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### (2) Direct $^{31}\text{P}$ ion implantation

MeV  $^{31}\text{P}$  implant

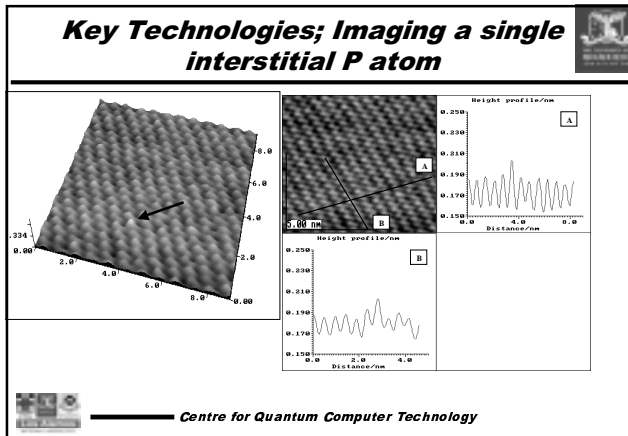
Etch latent damage & metallise

Read-out state of "qubits"

Resist layer, Oxide layer, Si substrate

Qubits:  $|1\rangle, |1\rangle, |0\rangle$

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### Conclusion: Quantum Computer

- Superposition and entanglement enables massive parallel processing  
b q b b q q b q q ... binary *qubits*
- (L qubits can store  $2^L$  numbers at once, classical only 1)
- Shor's prime factorization algorithm (1994) relevant to cryptography
- Grover's exhaustive search algorithm (1996)

Classical Computers      Quantum Computers      Factoring  
 Quantum Physics Problems  
 Exhaustive Search      All Problems

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### Further Reading

- Australian Centre for Quantum Computer Technology  
<http://www.ph.unimelb.edu.au/~gnj/src/srhome.html>
- Oxford quantum computer group <http://www.qubit.org>
- *The Feynman Processor*, G. Milburn, Allen & Unwin, 1998
- *Quantum Technology*, G. Milburn, Allen & Unwin, 1996
- *The Large, the Small and the Human Mind*, R. Penrose, Cambridge, 1997
- *Quantum Teleportation*, A. Zeilinger, *Scientific American*, April 2000
- *Physics and the Information Revolution*, J. Birnbaum, R.S. Williams, *Physics Today*, January 2000

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