

## Problem sheet 2: electrical sensors

1 (2001 exam)

An 80 kg mass is hung from the end of a 30 cm long aluminium (Al) cylinder whose radius is 1 cm before the load is applied. The diameter of the Al cylinder is monitored by a piezoresistive sensor, consisting of an insulated 0.5 mm radius copper wire wrapped once around the cylinder.

- (a) Derive a formula relating the diameter of the Al cylinder to the suspended load.
- (b) Using your result from (a), derive a formula relating the resistance of the copper wire to the suspended load.
- (c) What is the change in resistance of the Cu wire sensor due to the suspended load?
- (d) What is the sensitivity of the Cu sensor to the suspended load?
- (e) What would be the sensitivity of a sensor consisting of 10 loops of copper wire to the suspended load?

Data:

$$\begin{aligned}\text{Al: } Y &= 7 \times 10^{10} \text{ N/m}^2 \\ \rho &= 2.75 \times 10^{-8} \Omega\text{m}\end{aligned}$$

$$\text{Cu: } \rho = 1.69 \times 10^{-8} \Omega\text{m}$$

2 (2001 exam)

- (a) Explain how a pyroelectric sensor differs from one that employs the Seebeck-Peltier effect. Include in your answer a description of the different physical processes used in each sensor.
- (b) Describe two other uses of the Seebeck-Peltier effect additional to being used as a temperature sensor.
- (c) A 1 mm thick BaTiO<sub>3</sub> pyroelectric sensor is subject to a 50 K temperature flux. What voltage does it generate?
- (d) If the same voltage was generated by a PVDF sensor of the same dimensions, what temperature change would this represent?

Data:

$$C = \epsilon A/d$$

$$dV/dT = \alpha dT/dx$$

$$Q = CV \text{ for a capacitor}$$

$$Q = d F \text{ Piezoelectric effect}$$

$$Q = P_Q A \Delta T \text{ Pyroelectric effect}$$

BaTiO<sub>3</sub>:  $\epsilon_r = 1700$   
 $d = 78 \text{ pC/N}$   
 $P_Q = 4 \times 10^{-4} \text{ C/m}^2\text{K}$

PVDF:  $\epsilon_r = 1700$  (?)  
 $d = -30 \text{ pC/N}$   
 $P_Q = 0.4 \times 10^{-4} \text{ C/m}^2\text{K}$

### 3 (2001 exam)

- (a) Briefly describe the physical processes that make a piezoelectric sensor work.
- (b) Derive a formula that relates the magnitude of the force  $F$  applied to a piezo-electric sensor of cross-sectional area  $A$  and thickness  $d$  to the voltage generated across the sensor's surface.
- (c) A 1 mm thick piezoelectric sensor with an area of 1 cm x 1 cm develops a voltage of 1.6 kV. If the sensor is made of PVDF, what weight is being applied to the sensor?
- (d) What voltage would the same load generate if the sensor were made of BaTiO<sub>3</sub>?

Data: use the data from the previous questions.

### 4 (2004 exam)

- (a)
  - (i) What is the difference between piezoelectric and pyroelectric sensors? Include a simple sketch.
  - (ii) Give an example of a sensing application for each type of sensor.
- (b) A pyroelectric force sensor is constructed from a 1 mm thick piece of BaTiO<sub>3</sub> with an electrode area of 1 cm<sup>2</sup>.
  - (i) If a force of 0.5 N is applied to the sensor, what change will develop on the electrodes?
  - (ii) What voltage will be generated on the electrodes as a result of this charge?
  - (iii) What is the sensitivity of this sensor?

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- (a) The resistivity of metals, and thus resistance, varies with temperature according to:  
 $\rho = \rho_0 [ 1 + \alpha (T - T_0) ]$

At  $T_0 = 293 \text{ K}$ ,  $\rho_0 = 1.69 \mu\Omega\cdot\text{cm}$ .

A secondary thermometric standard for measuring temperature in the range 14 - 900 K on the international temperature scale is a platinum resistance thermometer (for Pt,  $\alpha = 3.9 \times 10^{-3} \text{ K}^{-1}$ ).

For a Pt wire thermometer of diameter 0.1 mm and length 3 cm, what is the resistance at 14 K and at 900 K ?

b) A Pt resistive temperature detector (RTD) has a resistance given by.

$$R = R_0 (1 + 39.08 \times 10^{-4} T - 5.8 \times 10^{-7} T^2)$$

(where  $R_0 = 100 \Omega$  is the resistance at  $0^\circ \text{C}$ ).

What is the difference between the linear and second order resistance values at  $T = 150^\circ \text{C}$ ? This is equivalent to how large an error in temperature?

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Consider heating a copper rod. Its resistance, length and cross-sectional area change upon heating.

- (a) If the temperature changes by  $1^\circ \text{C}$ , what percentage changes occur in  $R$ ,  $L$  and  $A$ ? The thermal expansion coefficient of copper is  $1.7 \times 10^{-5} \text{ K}^{-1}$
- (b) Comment on the implications of (a) for using a copper rod as a temperature sensor.

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What is the thermoelectric coefficient (also known as the differential Seebeck coefficient) for the following combinations?

- (a) Copper/Aluminium
- (b) Iron/Nickel
- (c) P-type Si/n-type Si

What temperature change does a voltage of 12 mV represent in each case? Which sensor has the highest sensitivity?

Data:

Metal	$\alpha$ ( $\mu\text{V/K}$ )
Copper	0
Aluminium	-3.2
Iron	13.4
Nickel	-20.4
p-type Si	1000
n-type Si	-1000