

# 640-245 Electromagnetism & Special Relativity

## General Relativity - Part 2

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## Geometry of Space-time

Flat

$C < 2\pi r$

$C > 2\pi r$

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## Apply equivalence principle

- Conclusion:
- Space is curved (into higher dimensions) by gravity
- How can this effect be tested?
- By drawing circles?
- Too difficult!
- Use path of light instead
- Arthur Eddington sent to south seas in 1920 to observe eclipse of the Sun
- Confirmed that the Sun's gravity curves space
- Einstein canonised!

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## Examples of Curved Space

- Space around the Sun
  - Starlight during solar eclipse
  - Radar echo from Venus
  - Radio signals from distant space craft
- Advance in the perihelion of Mercury
- Black Holes
- Gravitational Wave Astronomy

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## Curved space: Gravity of Sun

- Step 1: Observe stars at night, measure separation
- Step 2: Observe stars during eclipse with Sun between, measure separation

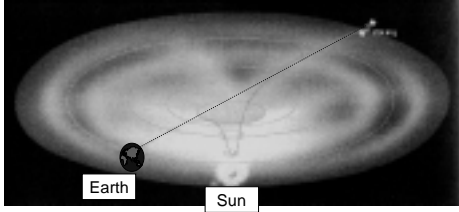
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## Curved space: Gravity of Sun

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## Curved space: Gravity of Sun

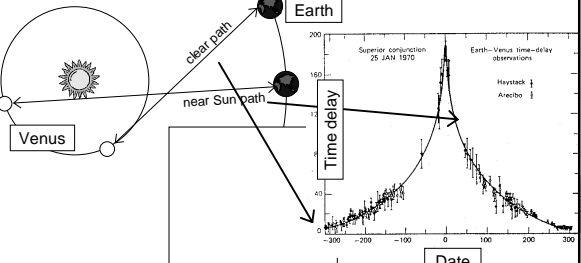
- Radio signals from distant space craft are delayed when Sun is near the path
- There is more space in between!



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## Curved Space: Radar echo from Venus

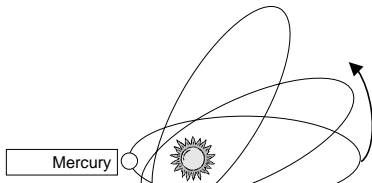
- Radar echo from Venus takes longer when Sun is nearby



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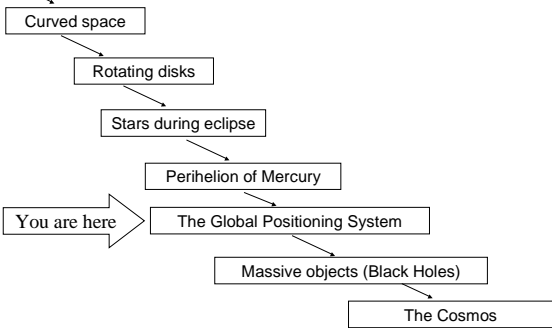
## Curved Space: Advance in Perihelion of Mercury

- Perihelion (closest approach to Sun) advances owing to gravitational influence from rest of solar system by 531" every 100 years
- However this is insufficient to account for the observed advance of 574" every 100 years
- Residual  $574 - 531 = 43''$  is due to General Relativity



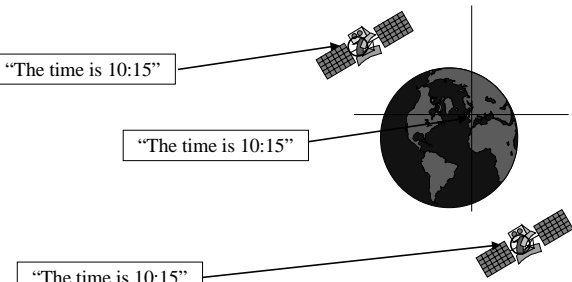
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## General Relativity: Step-by-step



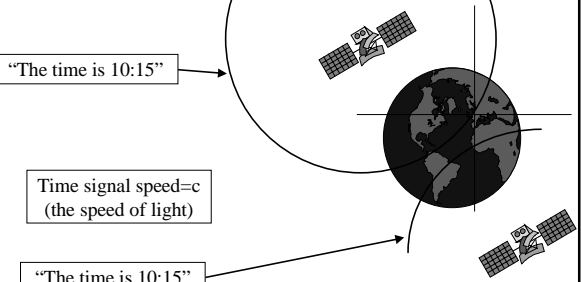
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## How does it work?

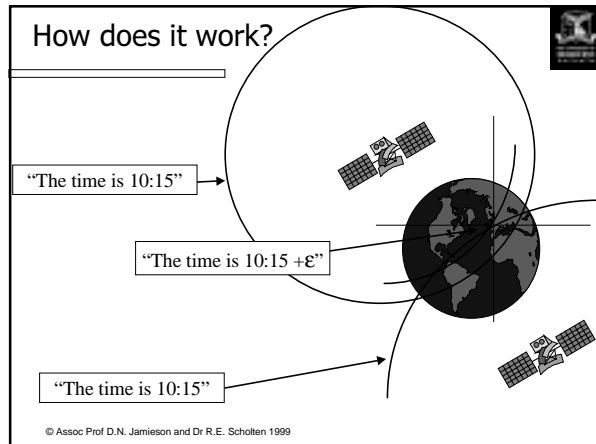


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## How does it work?



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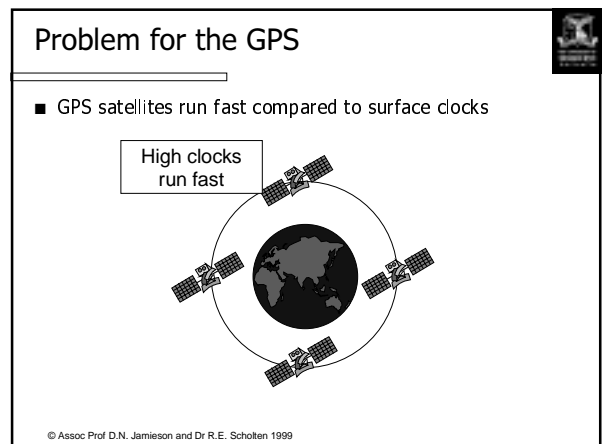
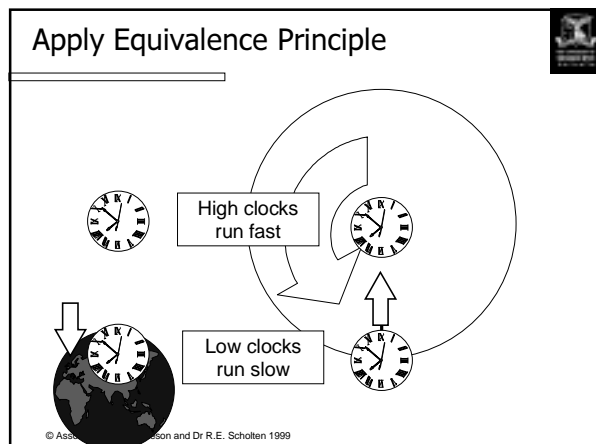
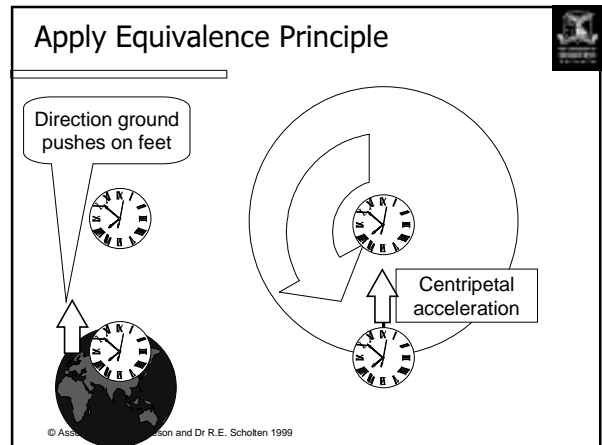
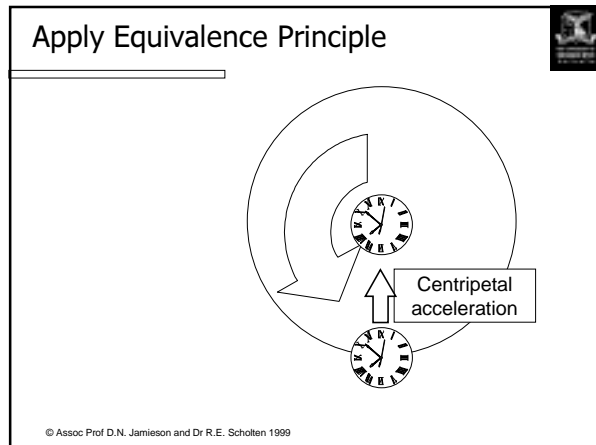
### What accuracy?

- Need signals from 4 satellites to find:
  - latitude
  - longitude
  - altitude
  - time

$$\delta x = c \delta t$$

- Time Error of 1 millionth of a second leads to
- Position Error of 300 m

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## Summary of Problems for the GPS

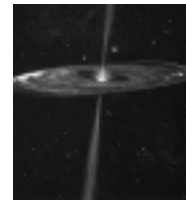


- 1. GPS satellites clocks run slow by 6 millionths of a second per day (SR - time dilation)
- 2. Cannot synchronise by exchange of signals
- 3. GPS satellite clocks run fast by 45 millionths of a second per day (GR - gravitational blue shift)
- Net effect: Run fast by 39 millionths of a second per day (=error of 12 kilometres)!
- SOLUTION: Make the clocks run slow to compensate!

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## Curved Space: Massive Objects

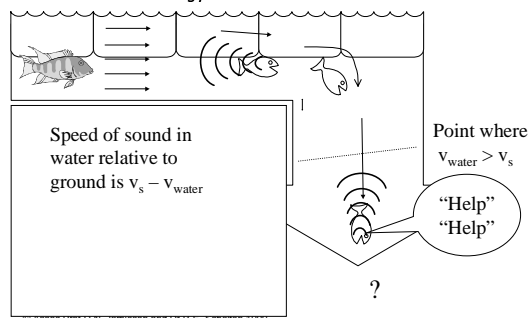
- Gravity - Revision
- Massive objects
  - What determines their size?
- Black holes and the event horizon
- Gravitational red shift
- Detecting black holes



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## Massive objects and light

- Fish in river analogy



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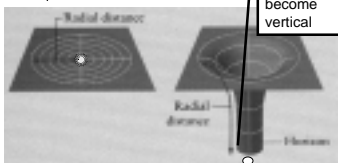
## Applications

- Global positioning system
  - Satellite clocks run fast by 45  $\mu$ s/day
- Black Holes

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## Black Holes: Summary

- No force can prevent gravitational collapse of an object greater than about 3 solar masses
- Object will collapse to a "singularity" (infinitely small)
- Gravity is very strong near the singularity, but otherwise unchanged by the collapse
- Gravity causes light to orbit at the radius of the photosphere
- At the radius of the "event horizon":
  - Volume of space goes to infinity
  - Clocks stop
  - Redshift goes to infinity
  - Radius of event horizon is  $2GM/c^2$
  - "The Schwartzchild radius"



Horizon is point where lines become vertical

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## Size of Event Horizon

Object	Event Horizon Radius*
■ Asteroid	$10^{-15}$ m (diam of nucleus)
■ Earth	1 cm
■ Sun	3 km
■ Globular Cluster ( $10^5$ stars)	300,000 km
■ Entire Galaxy	$10^{12}$ km



\*Size object would have to be compressed to become a black hole

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## Detecting Black Holes

- From observation of orbit of "normal" star can deduce mass of unseen companion

Best candidates:

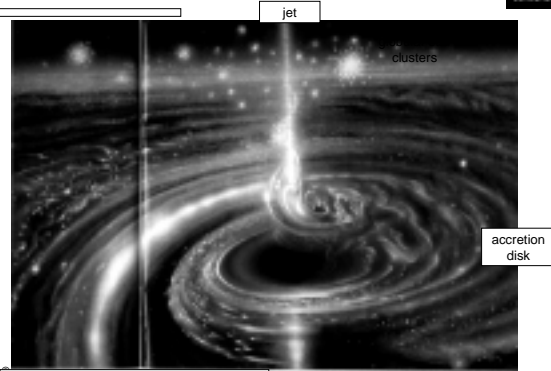
Object	Mass (solar masses)
■ Cygnus X-1	9.5
■ LMC X-1	2.6
■ AN 620-00	3.2
■ LMC X-3	7.0
■ SS433	4.3
■ Sagittarius A	$3.5 \times 10^6$
■ Quasar Engines	$10^8 - 10^{12}$



NB: Mass less than 3 solar masses implies neutron star (too light to be a black hole)

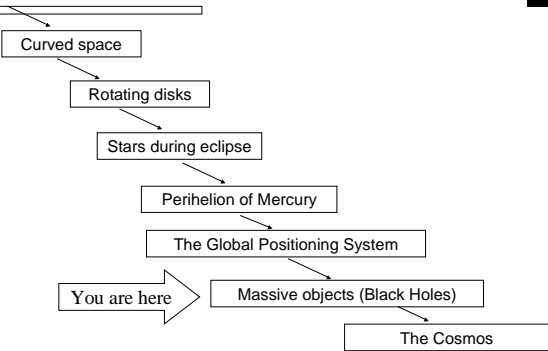
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## Massive Galactic Centre Black Hole



From Sky & Telescope June 1996

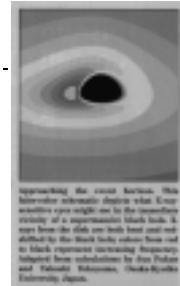
## General Relativity: Step-by-step



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## Black Hole in X-rays

- See intense x-rays from accretion disk
- Huge gravitational field distorts view and introduces massive red-shift of light

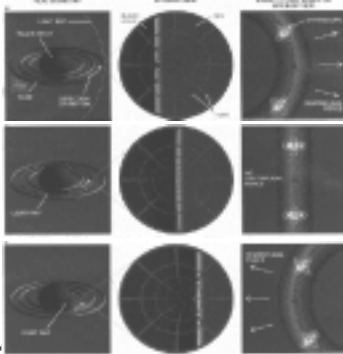


Approaching the event horizon, the innermost accretion disk gets so close that it is stretched into a spaghetti-like form. It is also so close that the light from the disk can be bent and captured by the black hole, which then re-emits it in black radiation. (Image courtesy of NASA/JPL-Caltech)

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## Life around a Black Hole

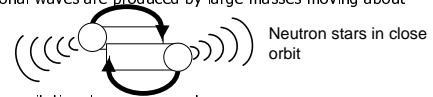
- Strange perspective in a space station constructed around a Black Hole



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## Gravitational Wave Astronomy


- Gravitational waves are produced by large masses moving about
- Effect of gravitational wave on a sphere



- Gravity wave antennas
  - (1) Super cooled bars oscillations in length: diameter of nucleus in 1 m
  - (2) Super accurate interferometers

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## LIGO

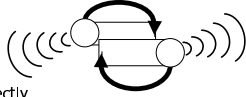


- A giant Michelson-Morely interferometer!
- Massive engineering to detect subtle warps in space-time caused by passing gravity waves

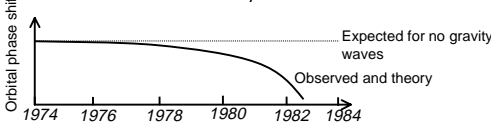
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## Source of gravity waves

- Pulsar PSR 1913+16 is slowing down
  - consists of a neutron star and a white dwarf in close orbit
  - orbital speed is about 400 km/s = 1/750 speed of light
  - located 16,000 l.y. from Earth
  - orbital period 8 hours
  - as energy is radiated in the form of gravity waves the period shortens



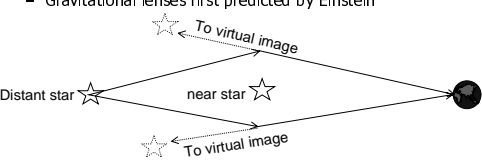
Too weak to be detected directly



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## Gravitational Lensing: Introduction

- Gravity can bend light
  - so strong gravitational fields can form images
  - Gravitational lenses first predicted by Einstein

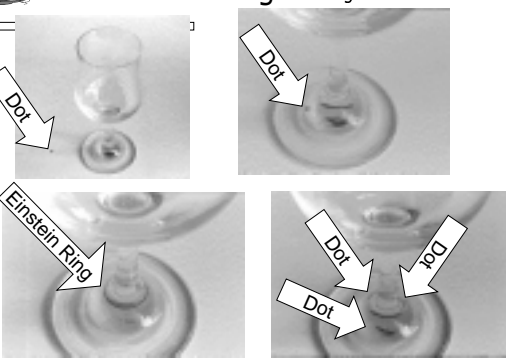


Called an "Einstein Ring"

- Very rare because close alignment of two stars improbable
- Observed instead with galaxies!


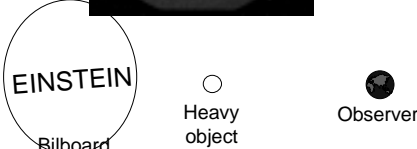
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## Gravitational Lensing: Wine glass



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## Gravitational Lensing: Einstein Billboard

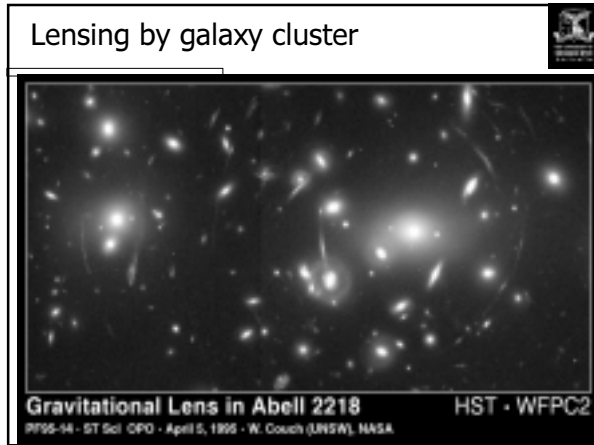
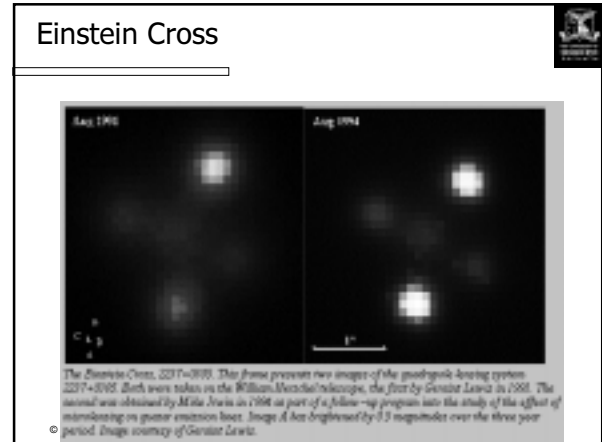
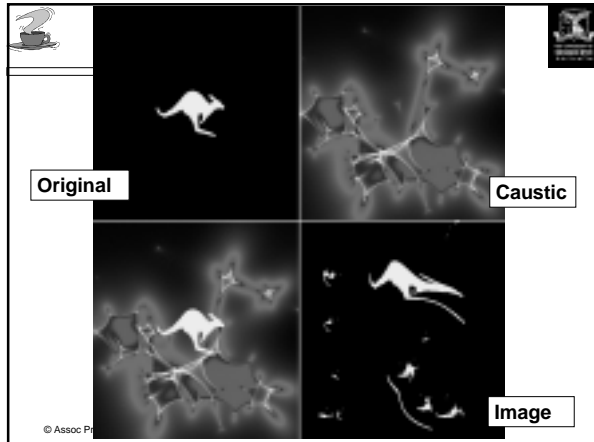
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## Gravitational Lensing: Einstein Ring

- Seen here in radio wavelengths
- Distant galaxy imaged by intermediate galaxy
- Alignment is not perfect



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- ### Predictions of General Relativity
- Gravitational red shift
    - Tested on Earth with the Mössbauer effect over a 20m tall tower
  - Bending of starlight by the Sun
    - Tested by observations of stars during a solar eclipse
  - Advance in the perihelion of Mercury
    - Tested by observation
  - Gravity waves
    - Tested by observations of pulsars in binary systems
    - Other experiments soon to come on line
  - Many others
  - Status: All ok!
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### References

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