

# Introduction to Cosmology



Michele Trenti

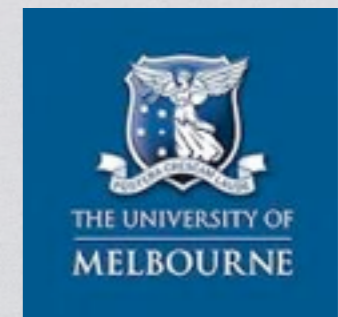


# My (scientific) path around the world

- ★ Born and raised in Italy
- ★ Undergrad. & Ph.D. in Pisa
- ★ Postdoc at STScI, Baltimore, MD
- ★ Postdoc at University of Colorado, Boulder
- ★ Kavli Institute Fellow (lecturer) at the University of Cambridge
- ★ Senior Lecturer at the University of Melbourne

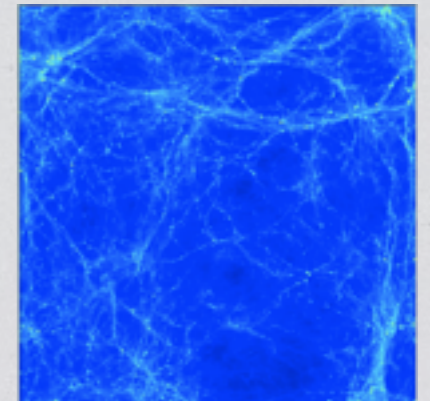


SCUOLA  
NORMALE  
SUPERIORE



# At the crossroad of modeling and observations

★ Models & simulations of dark matter, star/galaxy formation, metal enrichment



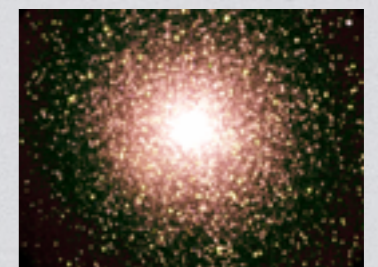
★ Observations of distant galaxies:

★ Ultra-faint

★ Bright



★ Star cluster dynamics/black holes



# Outside the office

- ★ Keen to go out and play (especially mountain “running”)



- ★ Cooking

- ★ Boardgames

- ★ ScienceFiction/Fantasy reading

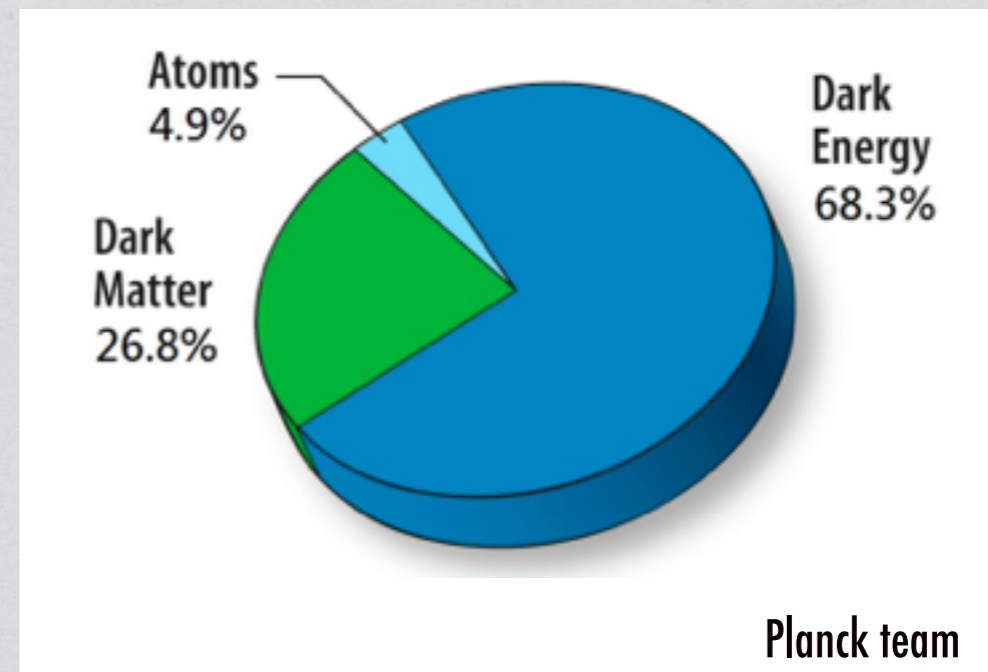
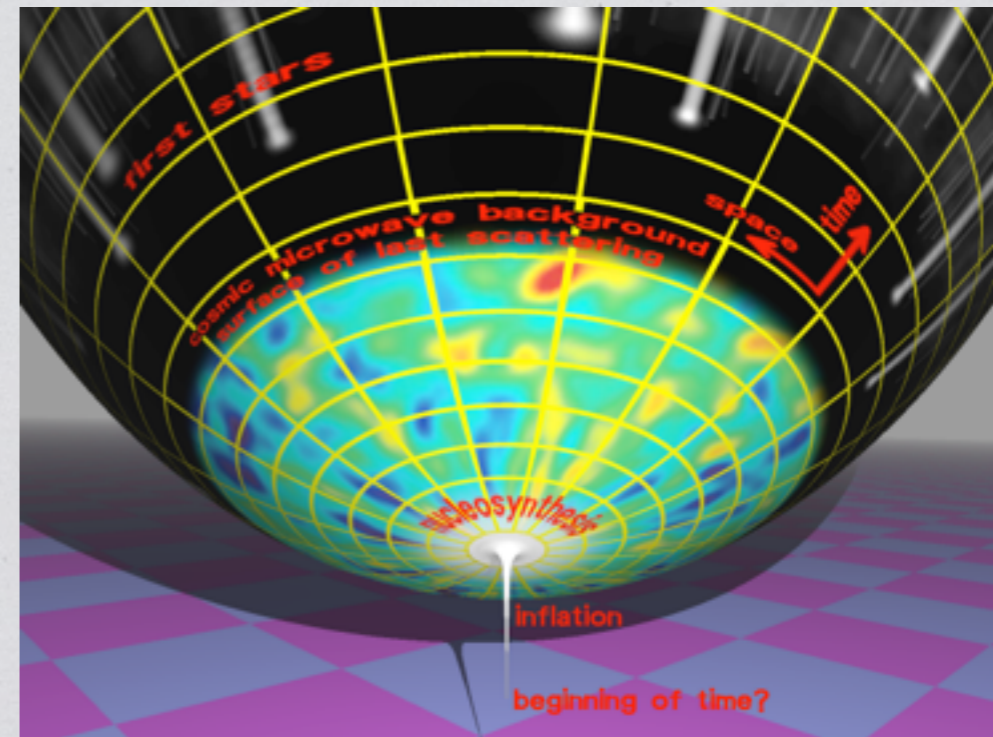


# Outline

- ★ The Friedman-Robertson-Walker model
- ★ Observational evidence for expansion
- ★ A brief history of the Universe
- ★ Gravitational Lensing

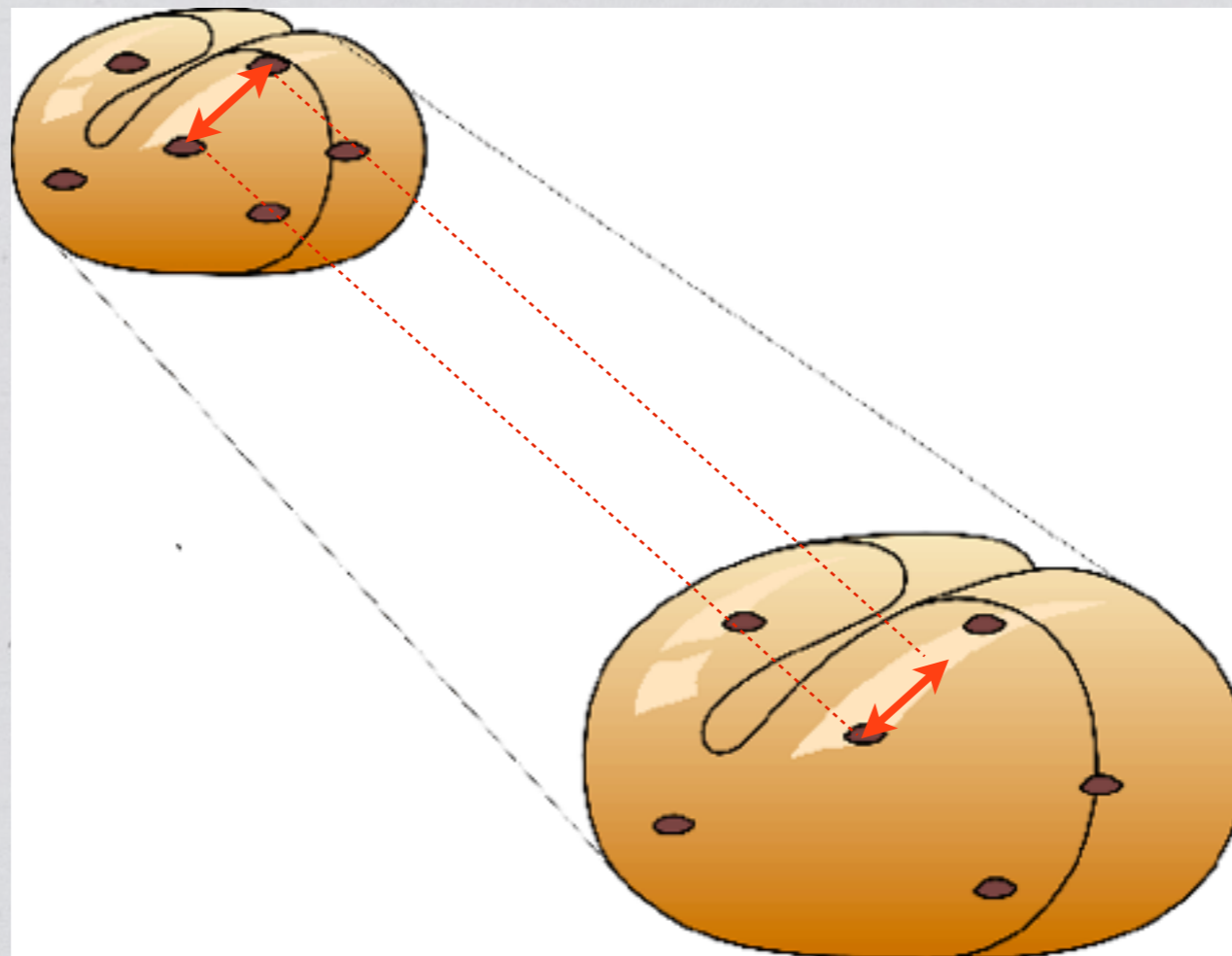
# A simple model for the Universe

- ★ Standard model:  
homogeneous,  
isotropic, expanding  
Universe
- ★ Astronomer's time unit:  
redshift  $z$  [ $z+1$ : inverse  
of expansion factor]
- ★ Simple composition:
  - ★ Dark Energy
  - ★ Dark Matter
  - ★ Baryons



# The raisin bread analogy

★ All raisins are moving away from each other as the loaf grows during raising/baking



★ *First evidence of expansion from Hubble (~1920)*

# Homogeneity and Isotropy

★ What does it mean?

★ Homogeneity: Universe looks the same at all points

★ Isotropy: Universe looks the same in all directions

★ *Can you think of examples of systems that meet one but not the other property?*

# The idea of comoving coordinates

★ Comoving coordinate system carried along with expansion:

★ Treat separately global expansion vs. local motion such as galaxy-galaxy gravity

★ Newtonian gravity is exact in comoving coordinates  
[for homogeneous Universe]



# The Friedman equation

★ How do we describe the expansion of the Universe?

★ Expansion factor:  $a(t) = 1/(1+z)$

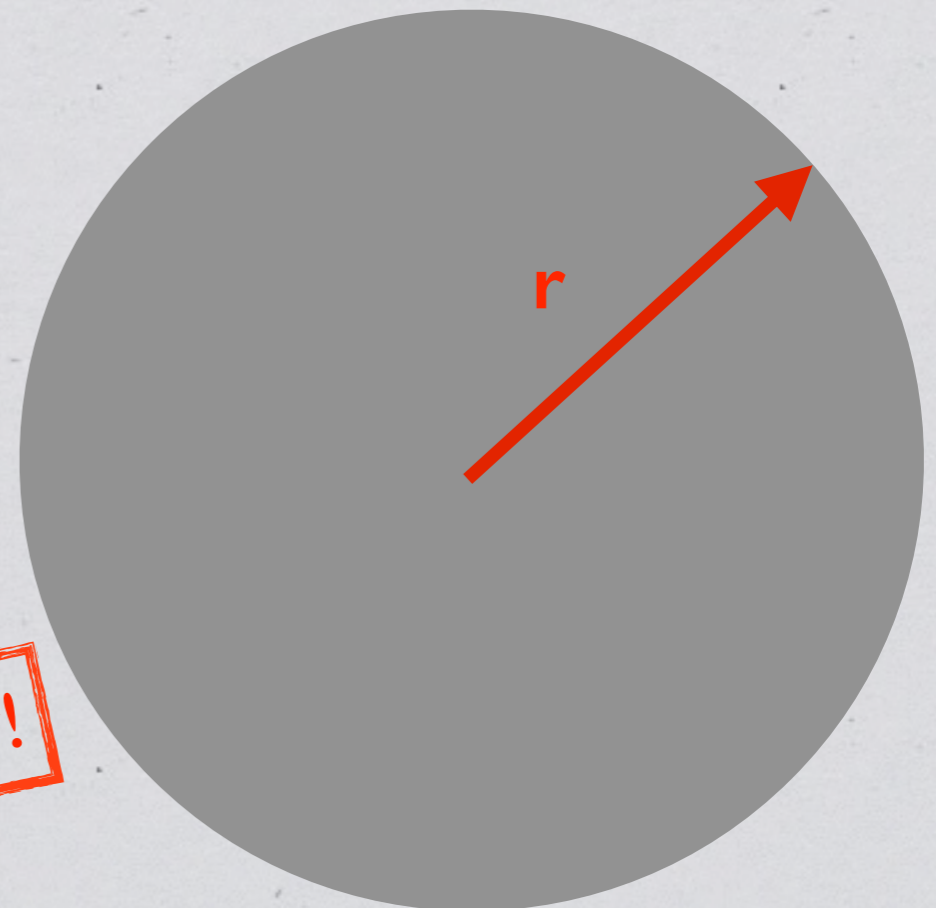
★  $a(t=0) = 0$

★  $a(t_{\text{now}}) = 1$

★ Equation for  $a(t)$  derived from energy conservation of a uniform expanding medium

No worries: No derivation today!

$$\vec{r}(t) = a(t) \vec{x} \quad \text{comoving}$$



# The Friedman equation

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{k}{a^2} + \frac{\Lambda}{3}$$

Curvature

Density

Cosmological constant

# Expansion rate

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\rho - \frac{k}{a^2} + \frac{\Lambda}{3}$$

★ Friedman equation: Density scaling as

★ Matter:  $1/a^3$

★ Radiation:  $1/a^4$  [IDEA of WHY extra  $a$ ?]

★ For a flat Universe

★ Matter Dominated:

$$a(t) \propto t^{2/3}$$

★ Radiation Dominated:

$$a(t) \propto t^{1/2}$$

★  $\Lambda$  Dominated:

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{\Lambda}{3}$$

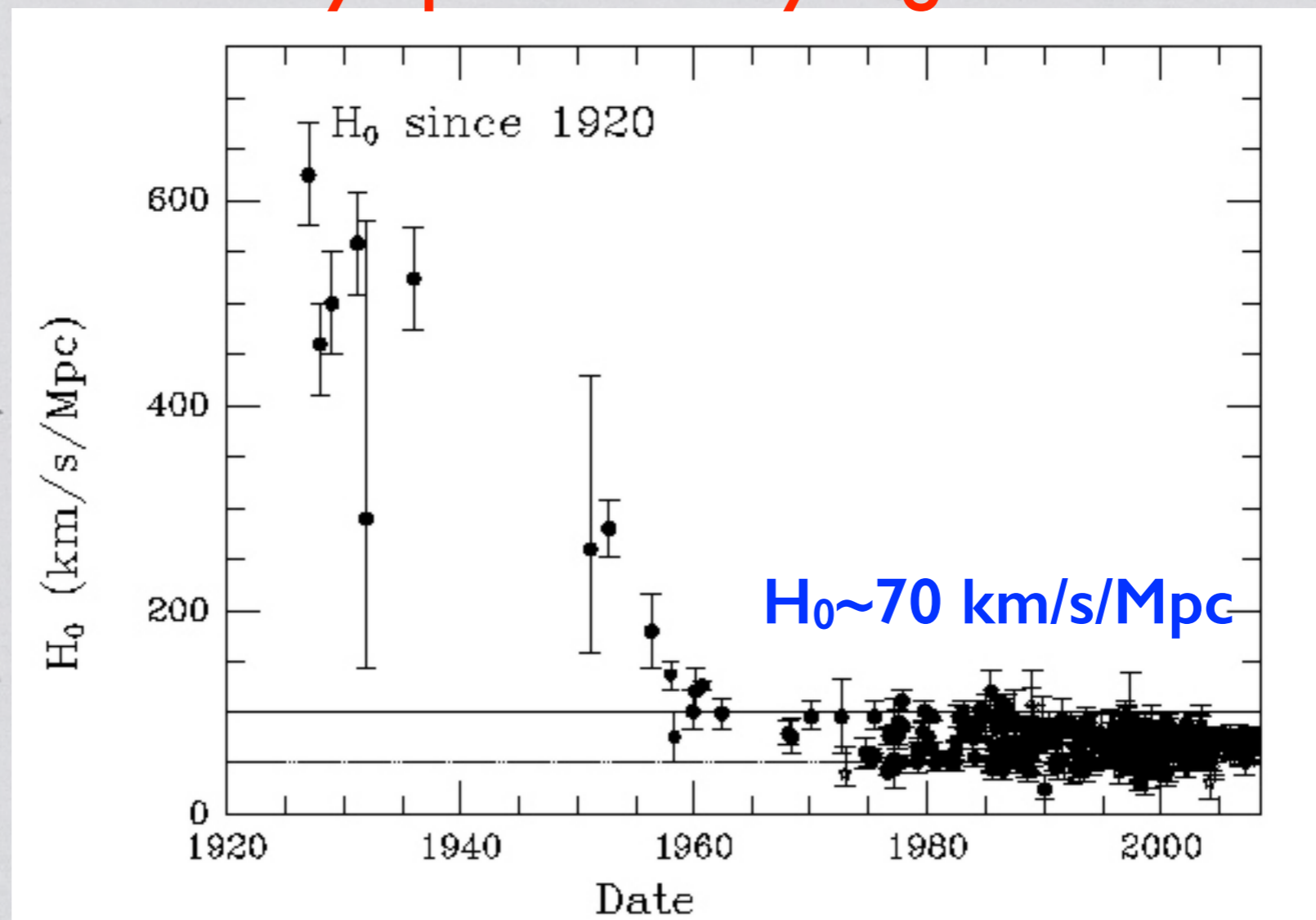
Acceleration



# A basic parameter: Hubble Constant

$$\frac{a(t)}{a(t_0)} = 1 + H_0[t - t_0] + O[(t - t_0)^2]$$

★ Hubble was only qualitatively right

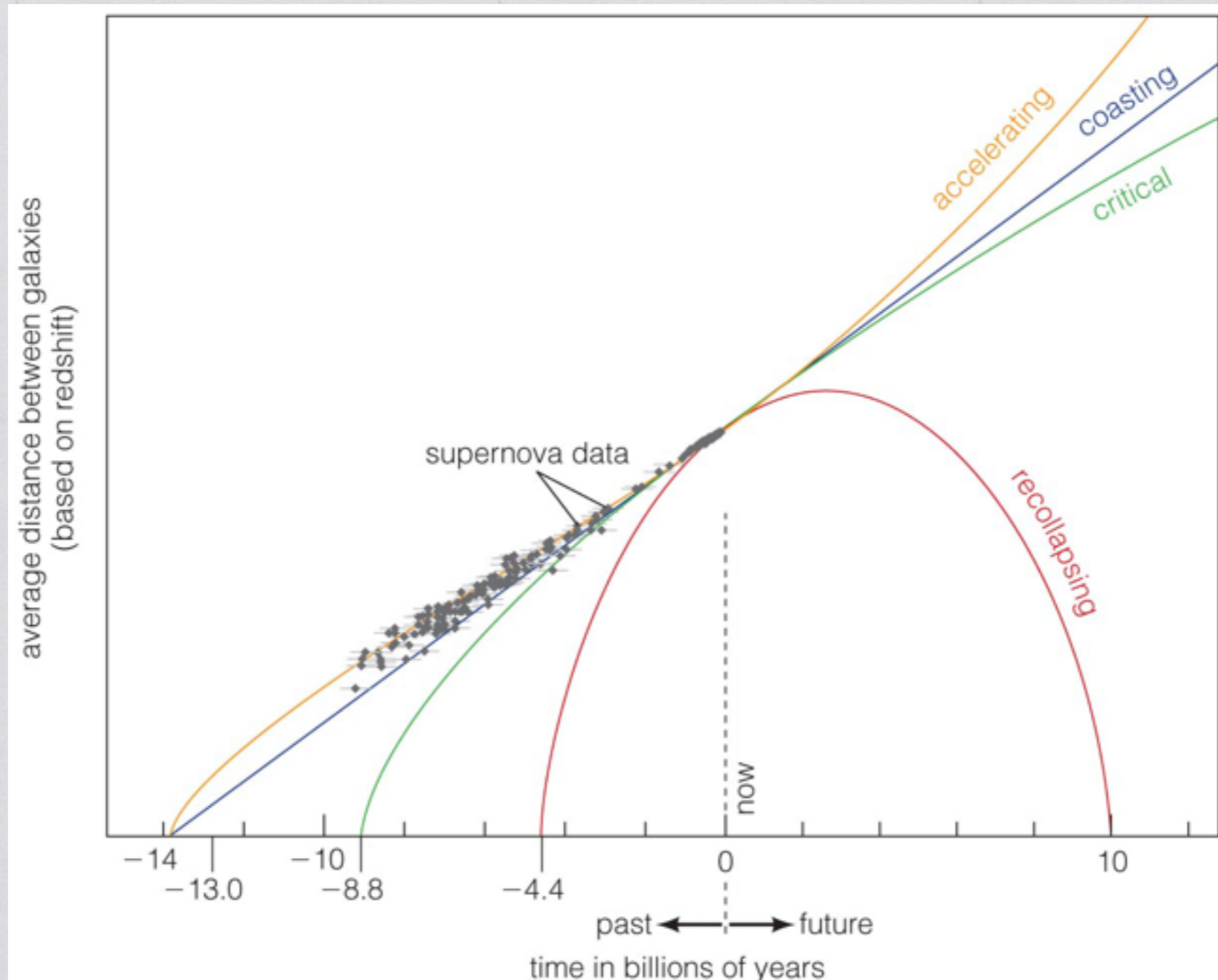


# Measuring expansion with standard candles

- ★ Measure redshift and observed luminosity
- ★ If we know absolute luminosity, we infer luminosity distance (cosmology dependent)



# Observational evidence for an accelerating universe



# Alternative cosmological probes: Oldest stellar populations

- ★ Globular clusters have oldest stars in the MW
- ★ What do they tell us about  $H_0$ ?

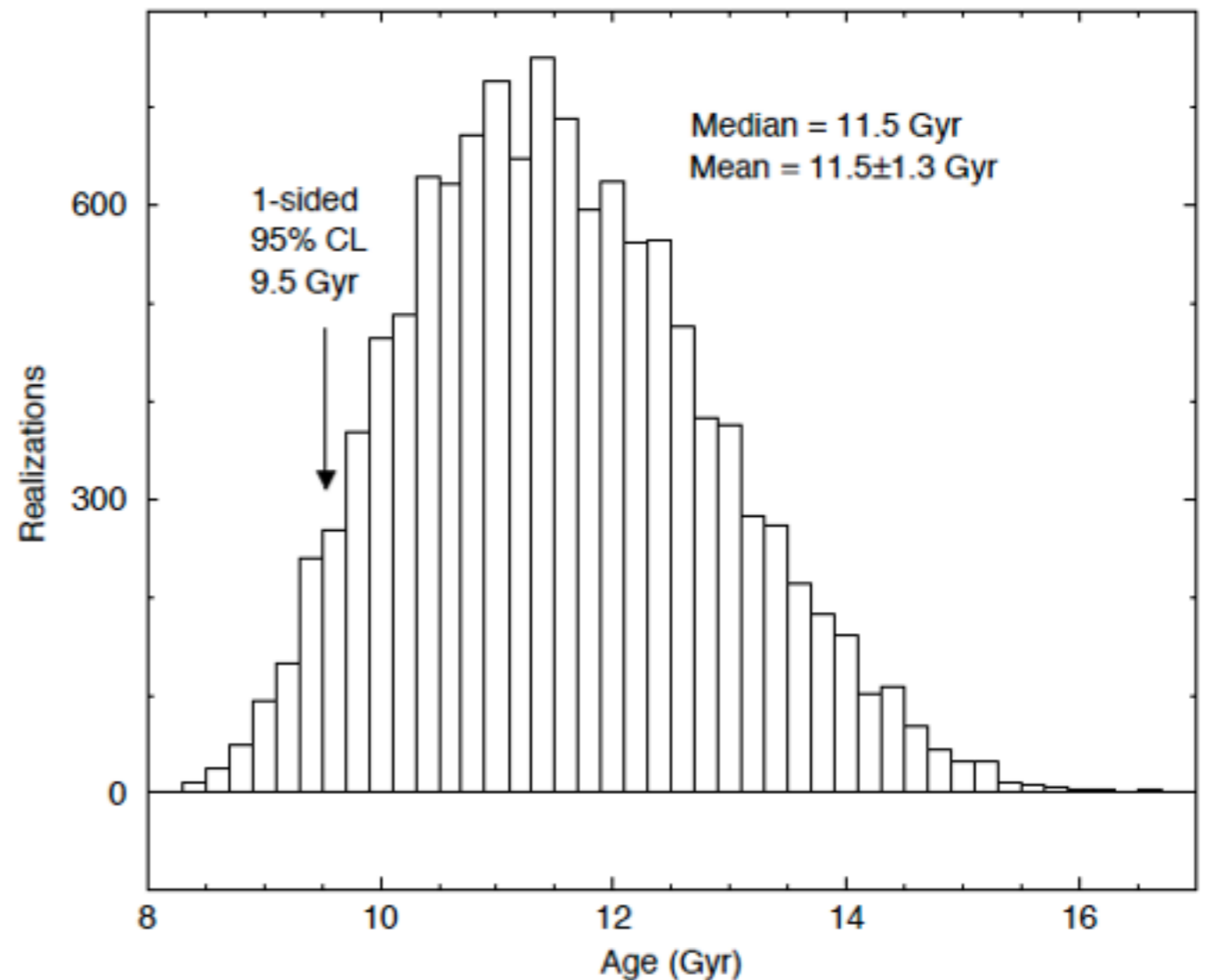


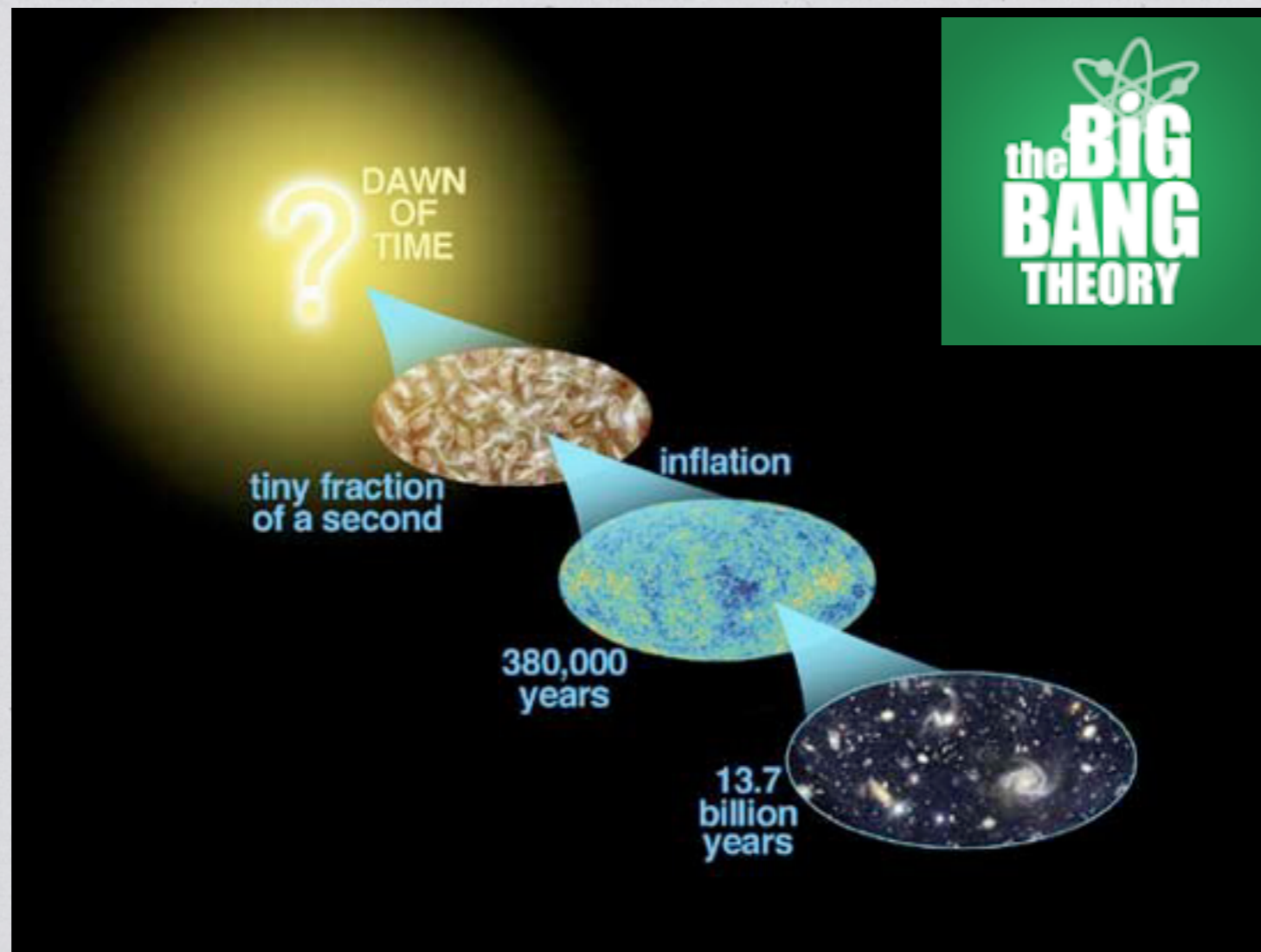
FIG. 2.—Histogram of globular cluster (GC) ages. The median, mean, standard deviation and one-sided 95% confidence level lower limit are all indicated on the figure.

**Consistent evidence that standard cosmological model provides a good description of the Universe**

**What are its basic predictions for the history of the Universe?**

# A brief history of the Universe: The Beginning

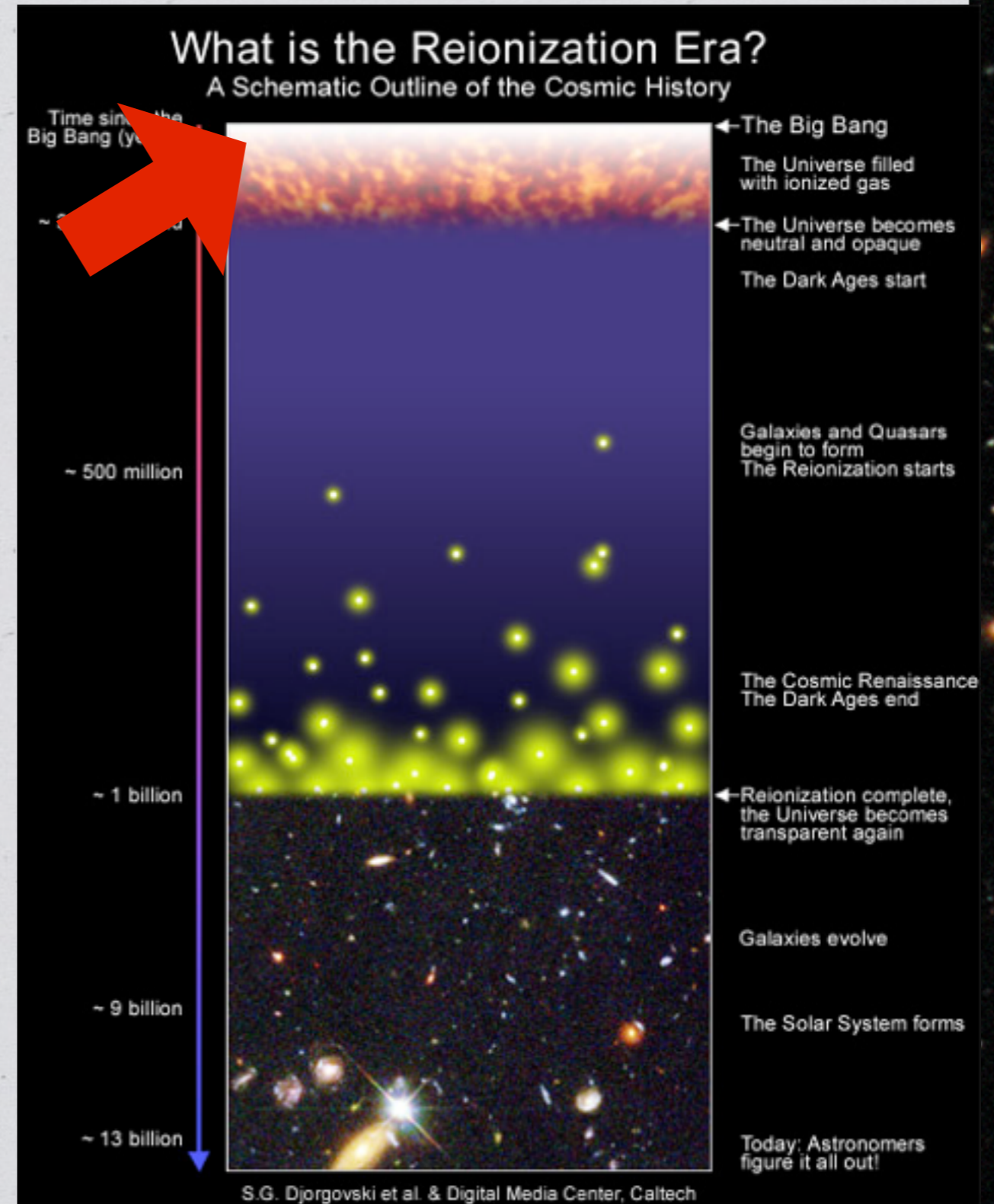
Our whole Universe was in a hot dense state, then nearly fourteen billion years ago expansion started...



# Hot and dense

## The first steps

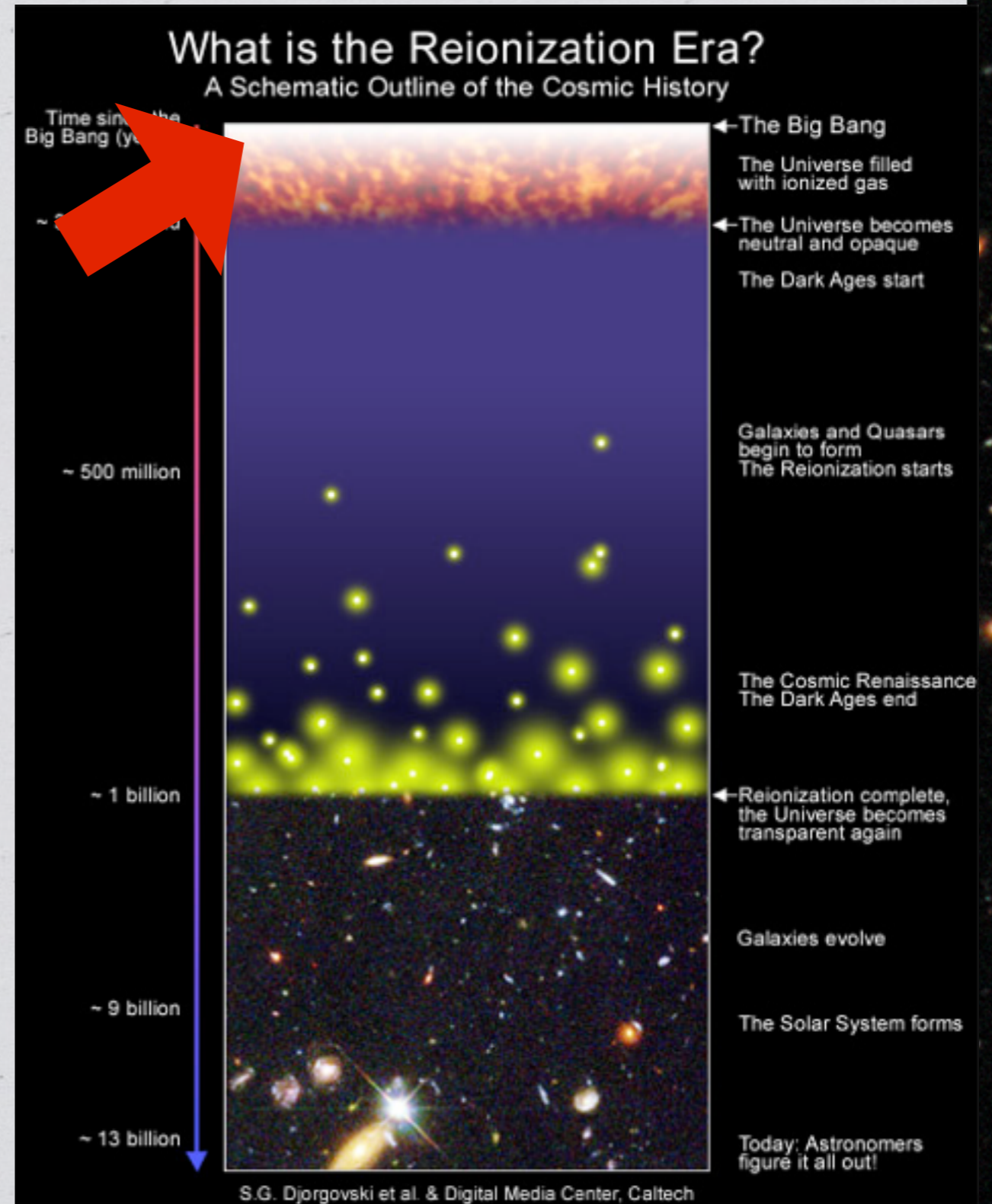
- ★  $t < 10^{-10}$  s: Fairly open to speculation
- ★  $t < 10^{-43}$  s: Planck epoch [gravity is unified]
- ★  $t < 10^{-34}$  s: Forces (except gravity) unified [ $T > 10^{16}$  GeV]



# Hot and dense

## The first steps

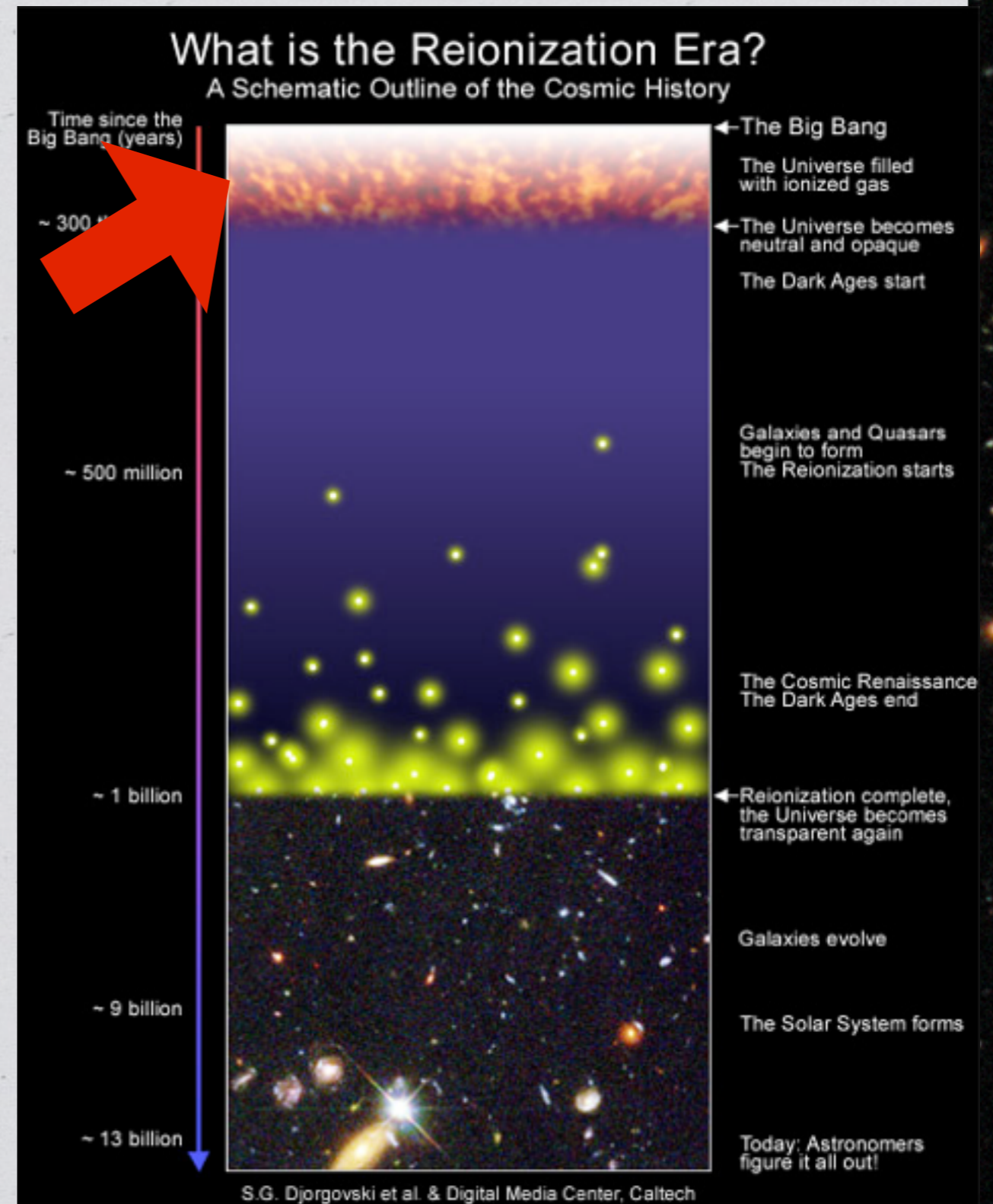
- ★  $t \sim 10^{-40} - 10^{-34}$  s: **Inflation**  
[Universe expands by factor  $\sim e^{99}$ ]
- ★ Inflation conveniently solves:
  - ★ Flatness problem ( $\Omega=1$ )
  - ★ Horizon problem (isotropy)
  - ★ Relic particle abundances



# Hot and dense

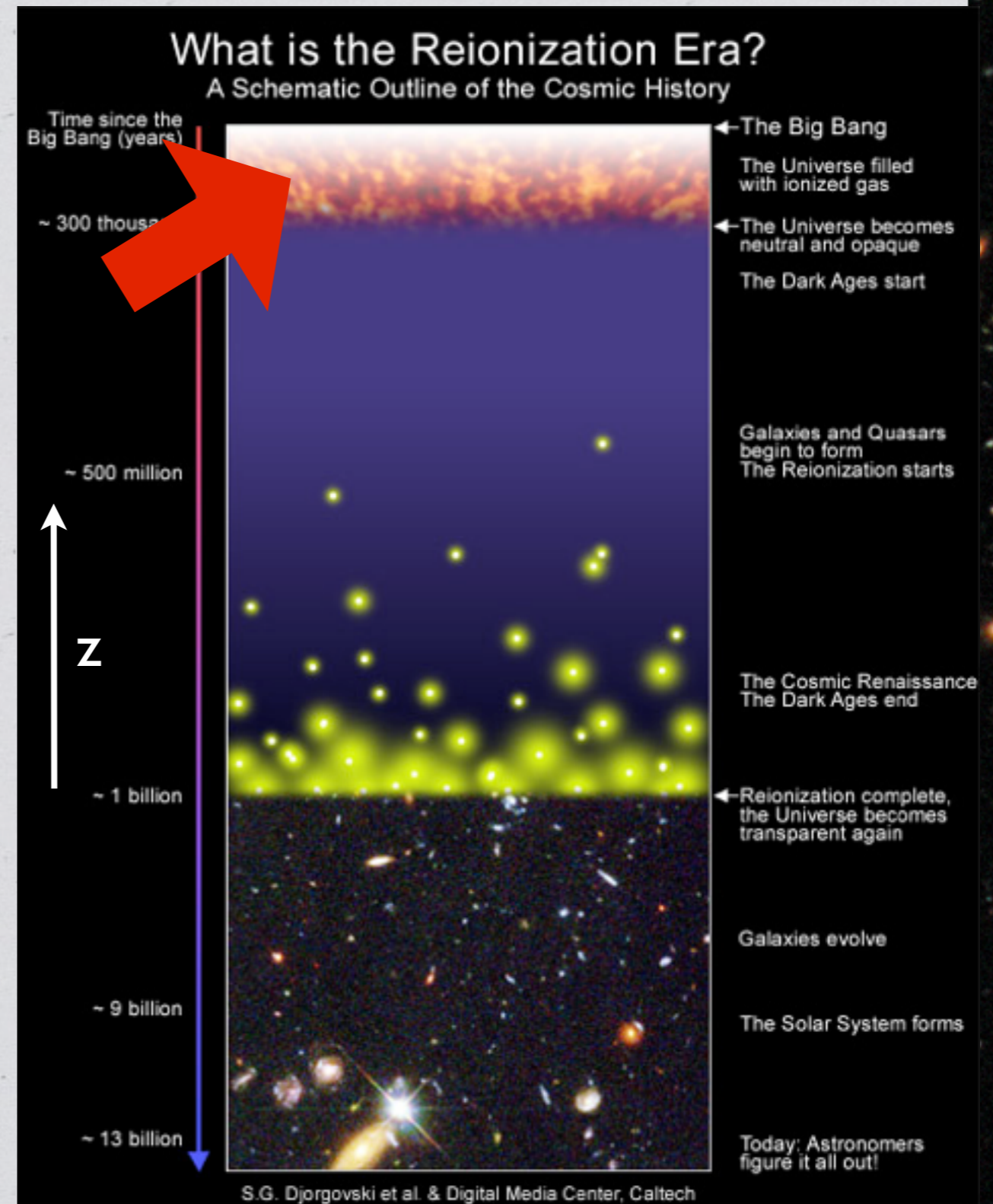
## The first few minutes

- ★  $t \sim 400\text{s}$ : **Nucleosynthesis**  
[ $T \sim 1\text{ MeV}$ ]
- ★ Radiation becomes unable to dissociate nuclei
- ★ Primordial chemical elements are formed (H, He, + traces of Li)



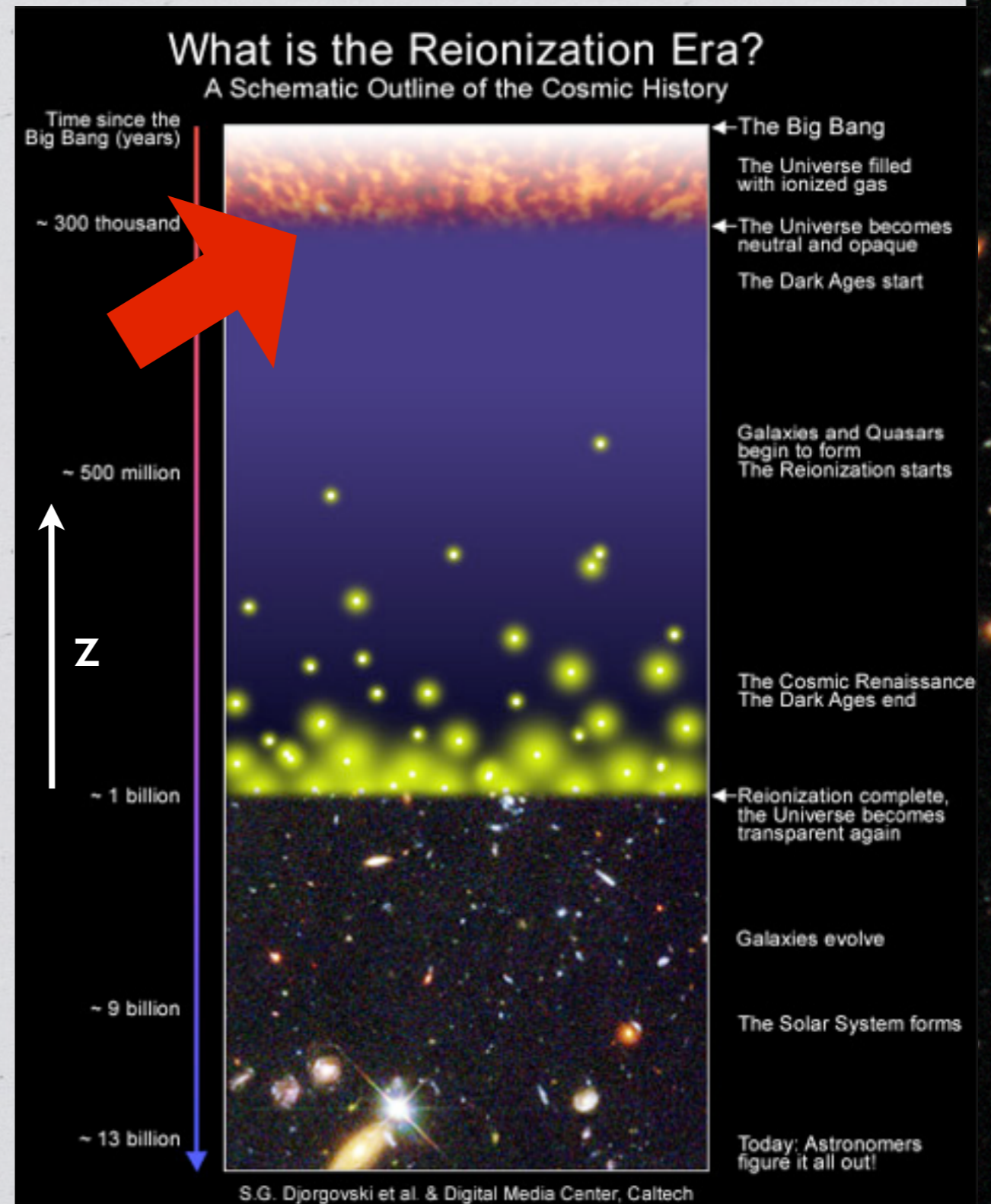
# The infancy of the Universe

- ★ Plasma temperature is decreasing with decreasing redshift (expansion-induced cooling)
- ★  $z \gtrsim 1500$  [ $\sim 3 \times 10^5$  yr]:  
The Universe is ionized



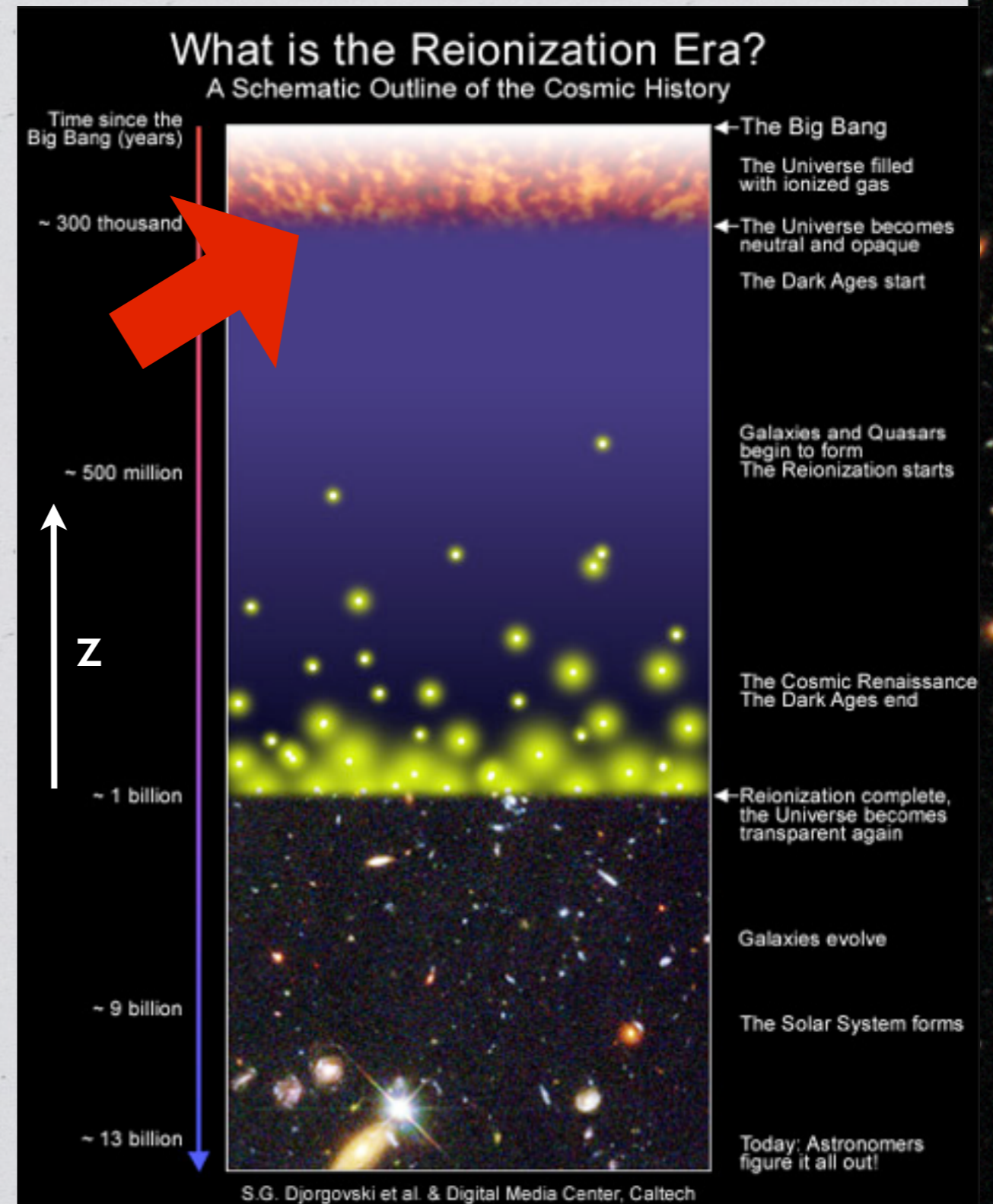
# The Dark Ages

- ★  $z \lesssim 1500$  [ $\sim 3e5$  yr]:  
Gas in the Universe becomes neutral (opaque)
- ★ Temperature has decreased sufficiently to allow efficient recombination
- ★ The Dark Ages begin



# Cosmic microwave background

- ★  $z \sim 1100$  [ $\sim 3.5e5$  yr]:  
Decoupling between radiation and matter
- ★ Radiation can travel freely without further scattering
- ★ Cosmic Microwave Background gives us image of the last scatter surface

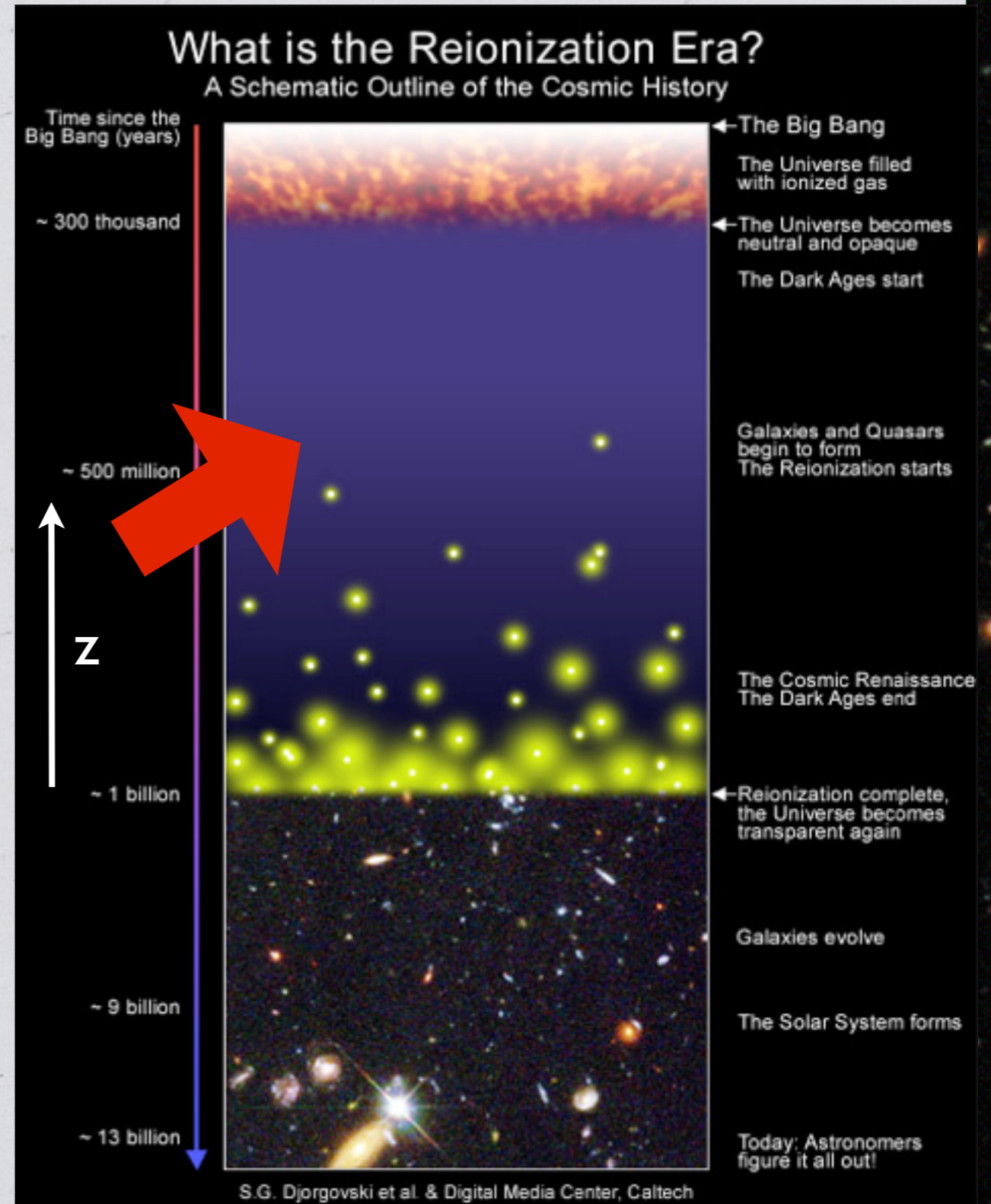


# The First Light

★  $z \lesssim 30$  [ $\sim 1 \text{e}8$  yr]: First dark matter halos with  $10^6$ - $10^8 M_{\text{sun}}$  form from non-linear growth of primordial density fluctuations

★ Gas cooling possible within these halos:

★ **First Stars and Galaxies are born**

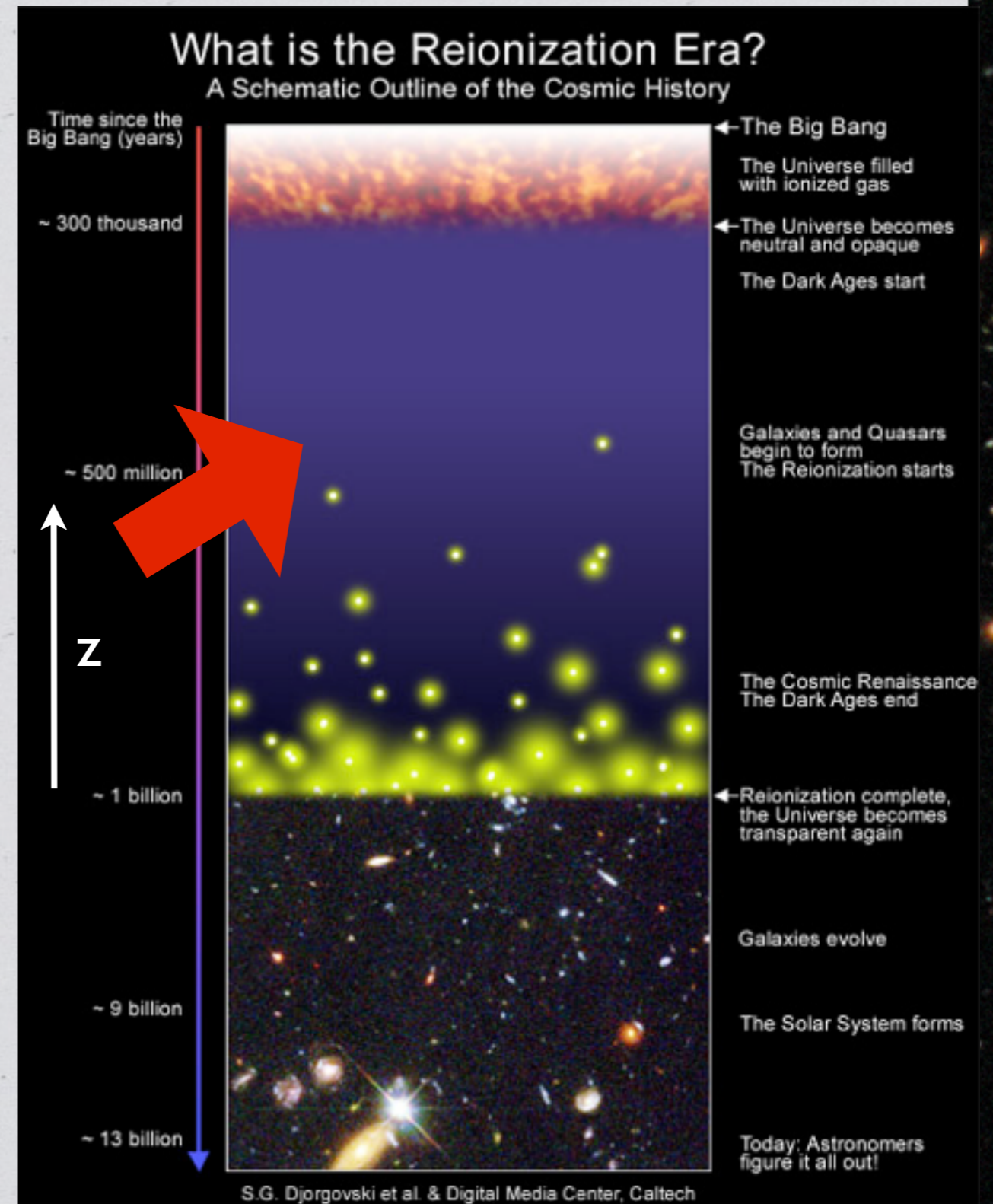


# The beginning of reionization

★  $z \lesssim 30$  [ $\sim 1 \text{ e}8 \text{ yr}$ ]: First light sources emit energetic photons ( $E > 13.6 \text{ eV}$ )

★ Hydrogen (re)ionization begins

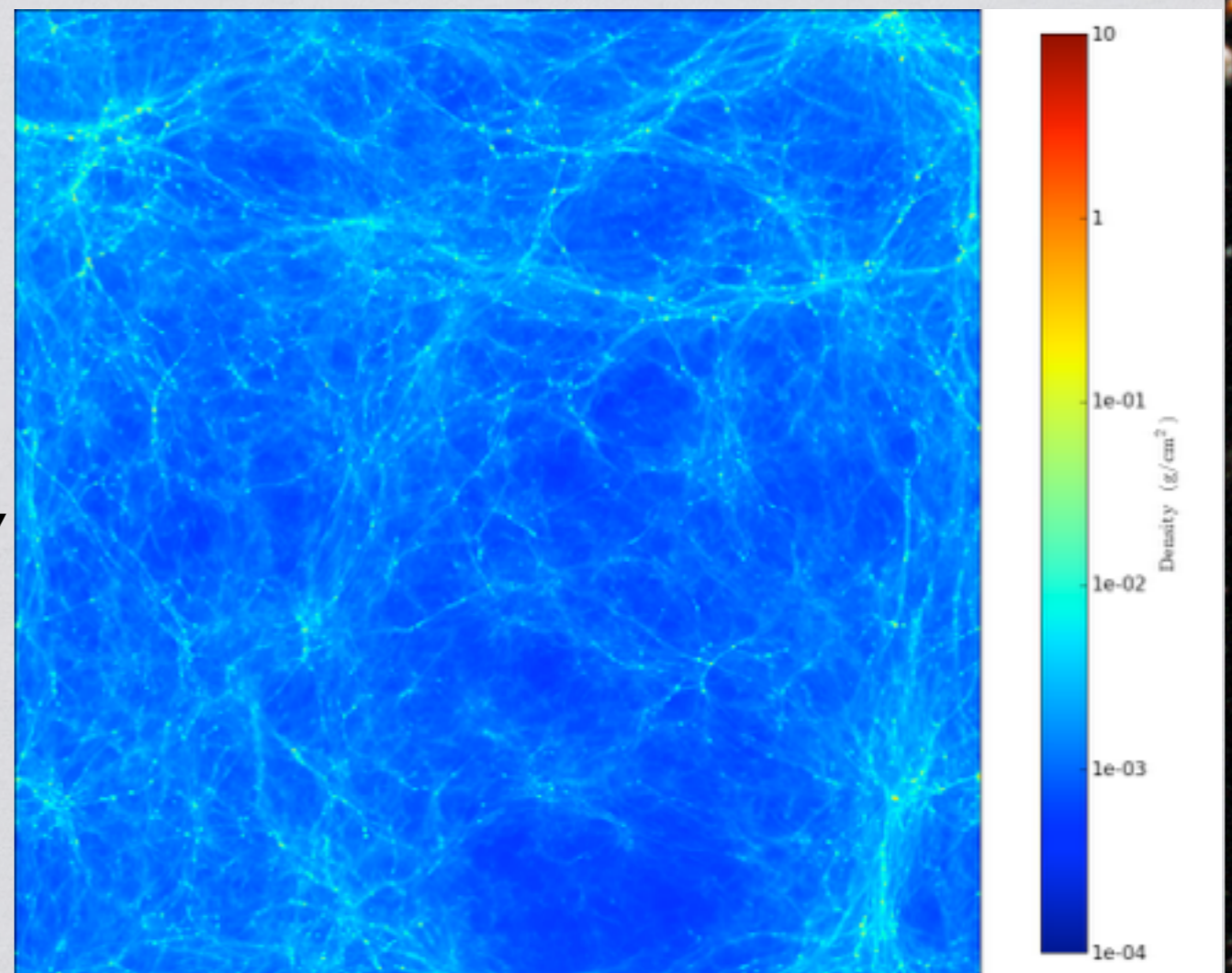
★ Star formation rate, and therefore ionization fraction, increases with decreasing redshift



# Clustering of First Galaxies

- ★ Formation of first galaxies (**ionizing sources**) is spatially biased
- ★ Large scale structure (cosmic web) already present at  $z \sim 6-10$
- ★ Overdensities: Locations of first galaxies

Structure at early times: density projection



$10^3 \text{ Mpc}^3$  box,  $N=2 \times 10^{24}$ ,  $z_{\text{end}}=6$

Trenti, Stiavelli & Shull (2009)

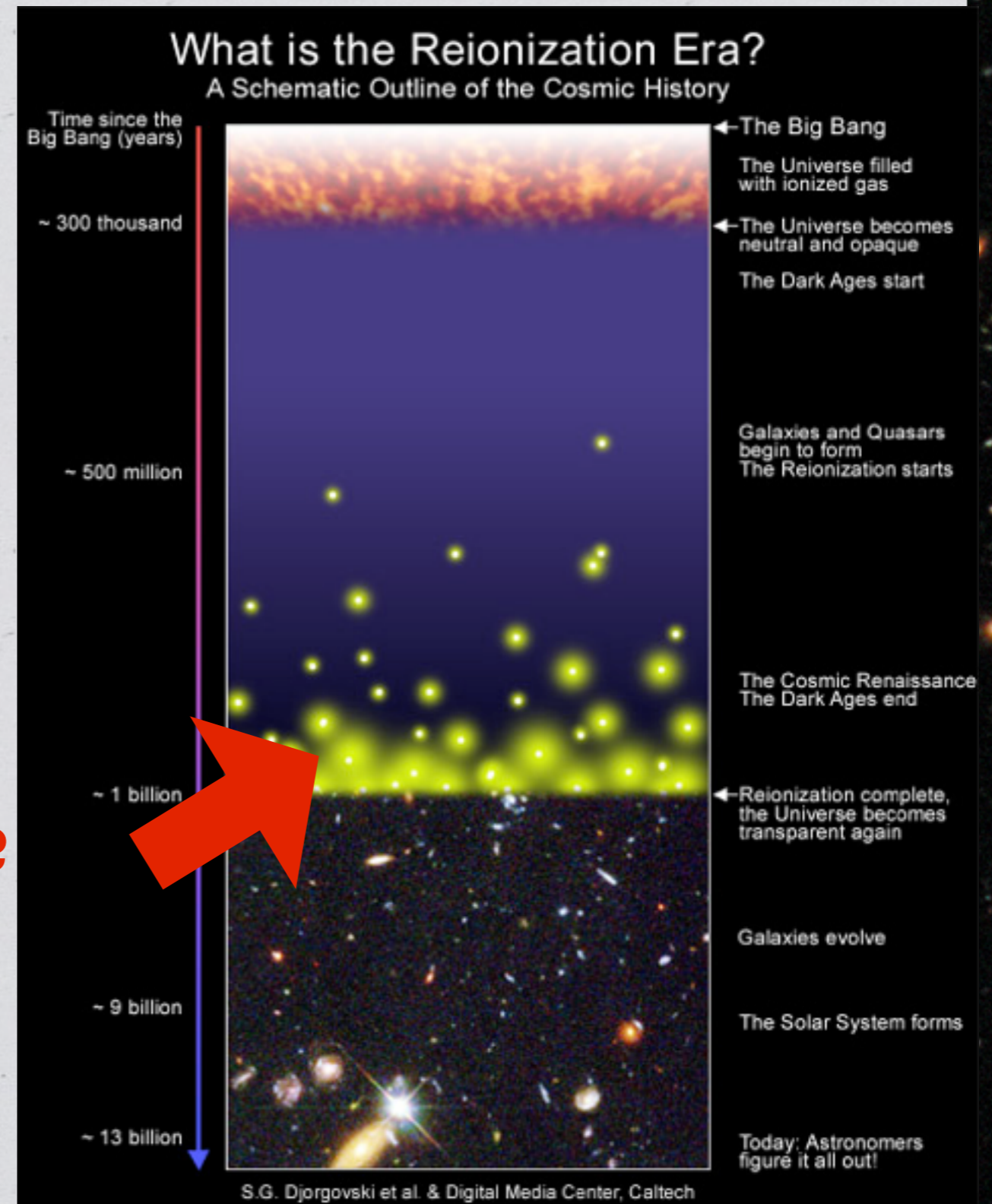
# The end of reionization

★ By  $z \sim 6$  [ $10^9$  yr] hydrogen reionization is completed:

★ In fact, the Universe is observed to be mostly transparent to ionizing photons

★ How does the process proceed from  $z \sim 30$  to  $z \sim 6$ ? What is its topology?

★ What are the sources responsible? And their properties?



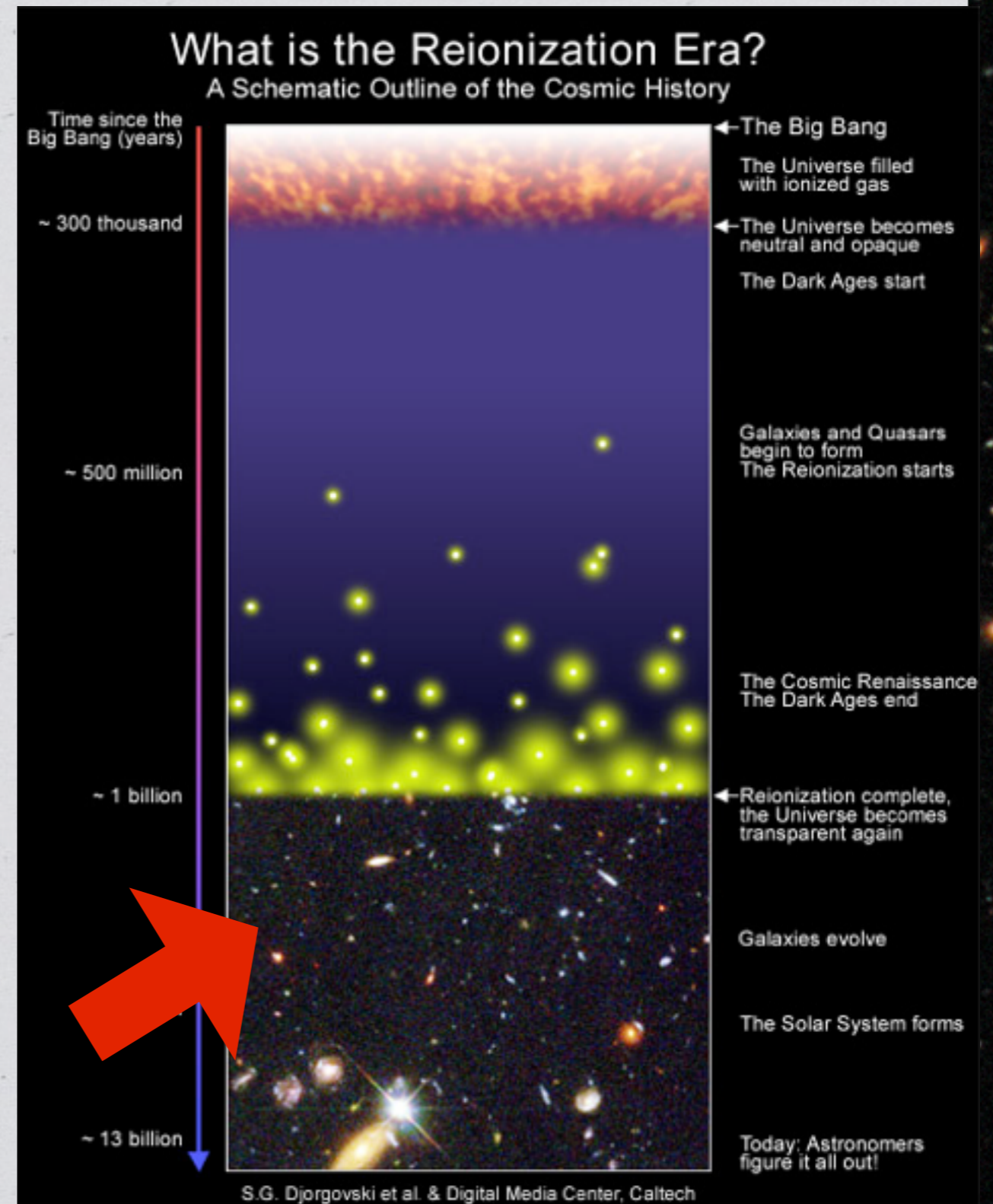
# The golden age of galaxies

★  $z \sim 6$  [1 Gyr] to  $z \sim 2$  [3 Gyr]:

★ Star formation rate increases with decreasing redshift

★ Galaxies are assembled

★ Heavy chemical elements ("metals") produced in good numbers by SNe



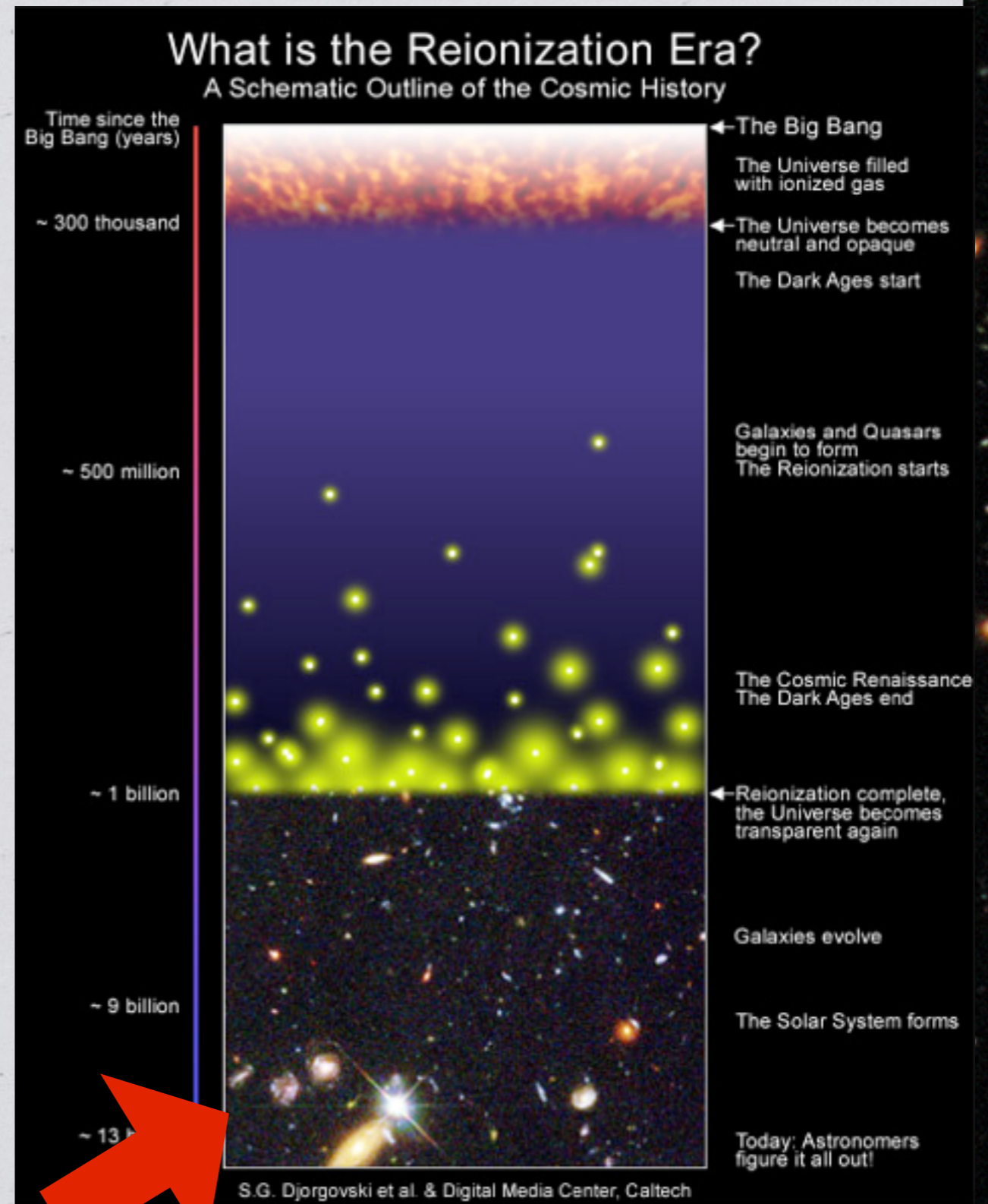
# The golden age of galaxies

★  $z < 1$  [ $t \sim 8 \text{Gyr}$ ]:

★ Star formation rate decreases steadily with decreasing redshift

★ Galaxies become progressively passive

★  $z = 0$ :



# What is next?

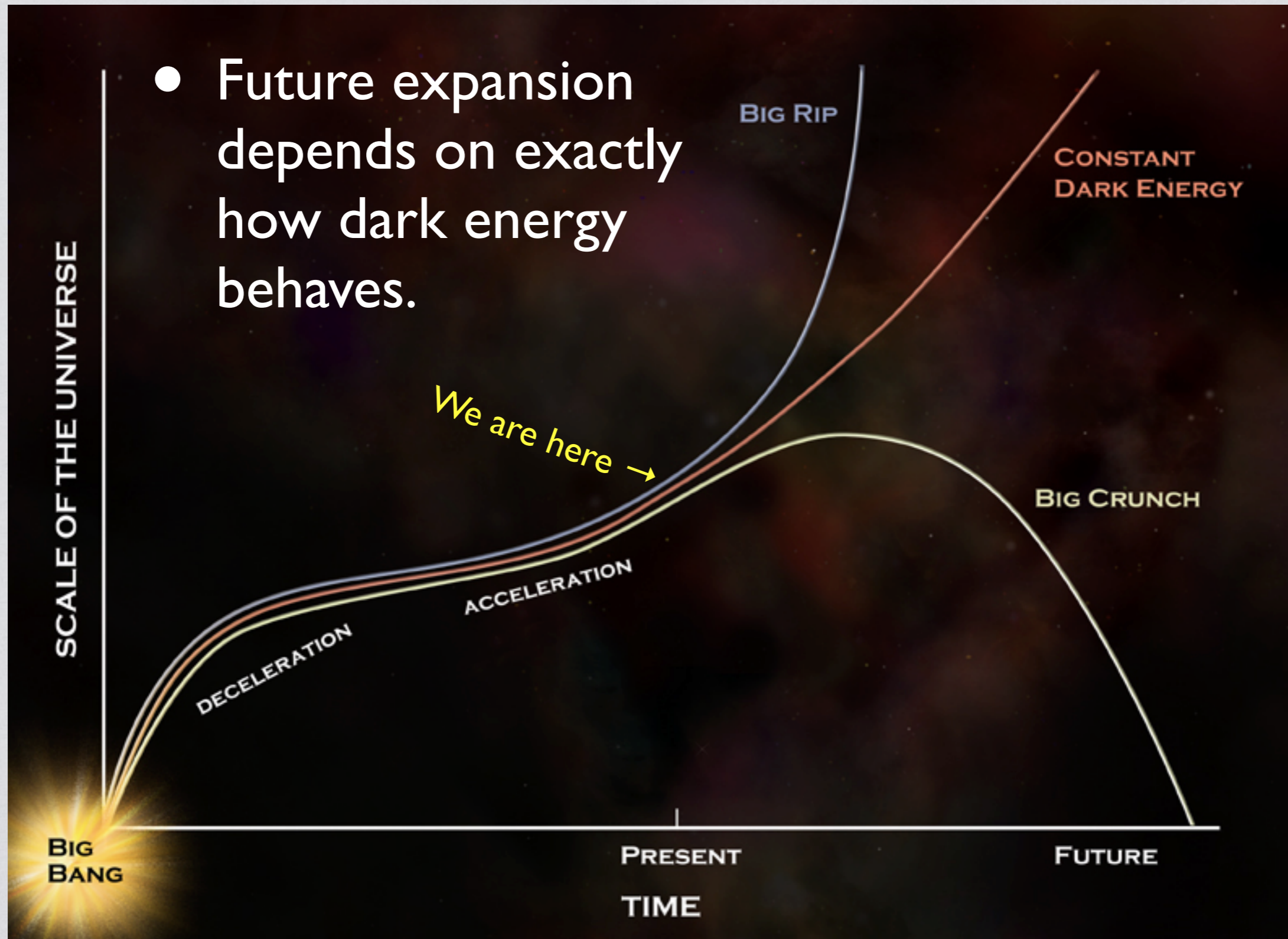
*It's difficult to make predictions, especially about the future.*

*- Yogi Berra*

- Universe is expanding now and that expansion is speeding up because of Dark Energy
  - *But will expansion continue to speed-up?*
  - *Or will the Universe stop expanding and re-collapse?*
- *How long do we have?*

# What is next?

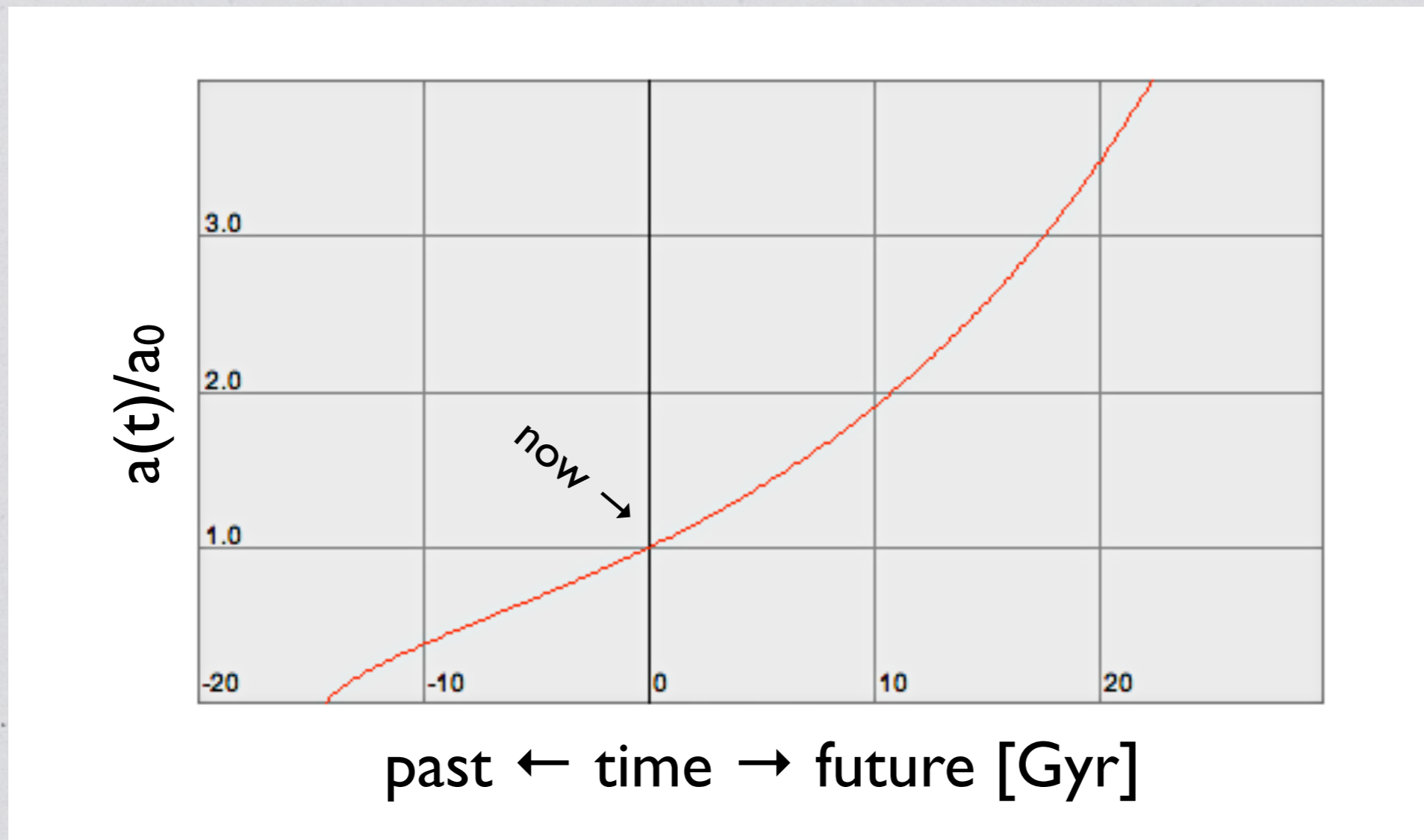
- Future expansion depends on exactly how dark energy behaves.



# A simple possibility - Heat Death

- Constant Dark Energy continues to accelerate the universe

★ What are the consequences?



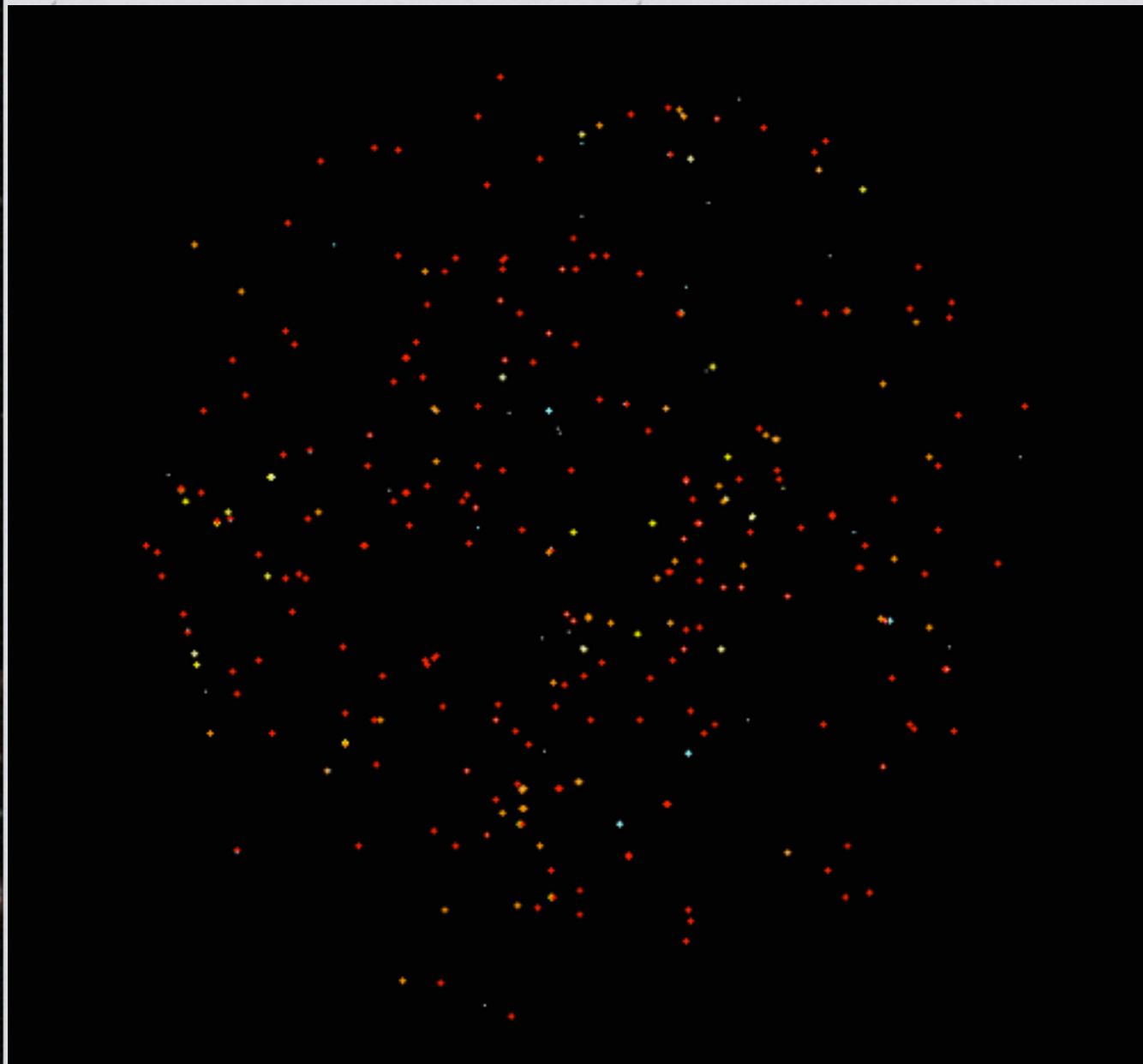
*How does it end?*



~2-4 Gyr: Milky Way and Andromeda collide,  
become a single elliptical galaxy

# How does it end?

~5 Gyr: Sun becomes red giant, planetary nebula, white dwarf



- ~100 Gyr: Expansion accelerated so fast that all other galaxies beyond our horizon
- Only red dwarf stars remain
- Not much to see

- $\sim 10^{12}$  years: end of the stellar era.  
All stars have evolved into their end stages (WD, NS, BH).  
Universe is dark. Proton decay?
- $\sim 10^{37}$  years: Only black holes remain and they are evaporating.
- $\sim 10^{100}$  years: Even the black holes are gone. Only electrons, neutrinos, proton decay products, and photons exist.

Temperature  $\rightarrow$  0 K.

**It is over.**



# Summary

- ★ Homogenous, Isotropic Universe (FRW model)
- ★ Some measurements of cosmological parameters ( $H_0$ ,  $\Lambda$ )
- ★ Expansion history of the Universe

# Readings/useful material

- ★ "Foundations of Astrophysics" B. Ryden & B.M. Peterson, Addison-Wesley
- ★ "An introduction to modern cosmology" A. Liddle
- ★ "Distance Measures in Cosmology" D. Hogg, 1999,  
<http://arxiv.org/abs/astro-ph/9905116>
- ★ Cosmology calculator by Nick Gnedin  
<http://home.fnal.gov/~gnedin/cc/>
- ★ Next class: Dark Matter