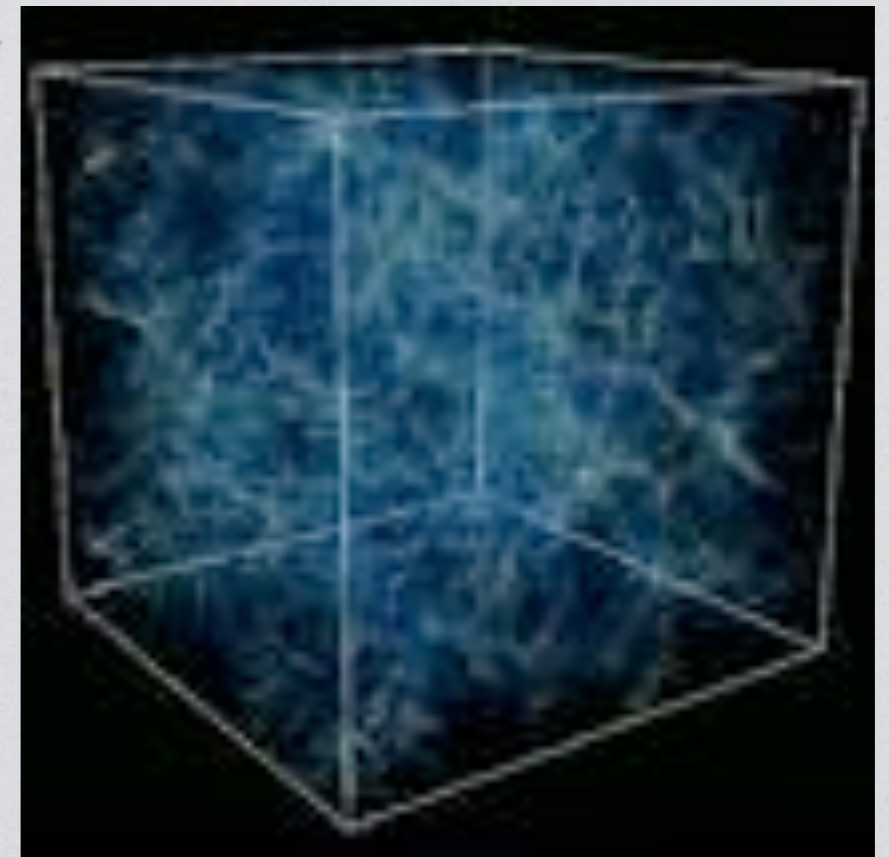


Star Formation



Dark Matter and Baryons

- ★ Gravity (DM) defines large scale structure of the Universe
- ★ Baryons are mostly hitchhiking a ride
- ★ Yet, their physical interactions are far richer
 - ★ "Gastrophysics"

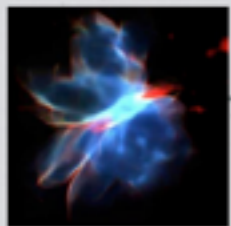


★ **How are stars formed?**

Before starting:

Stellar population classification

For astronomers: Metals == Chemical elements heavier than Helium



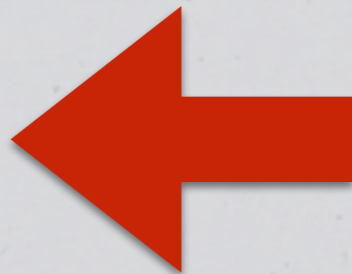
Population III stars:

metal-free, massive (but no direct observations), first stars formed in the universe



Population II stars:

low-metallicity stars (lets say $<1\%$ solar), normal mass function (typical mass $<M_{\text{sun}}$), old stars (globular clusters, galactic nuclei)



Population I stars (like the Sun):

high-metallicity, young and hot, normal mass function, found preferentially in spiral arms

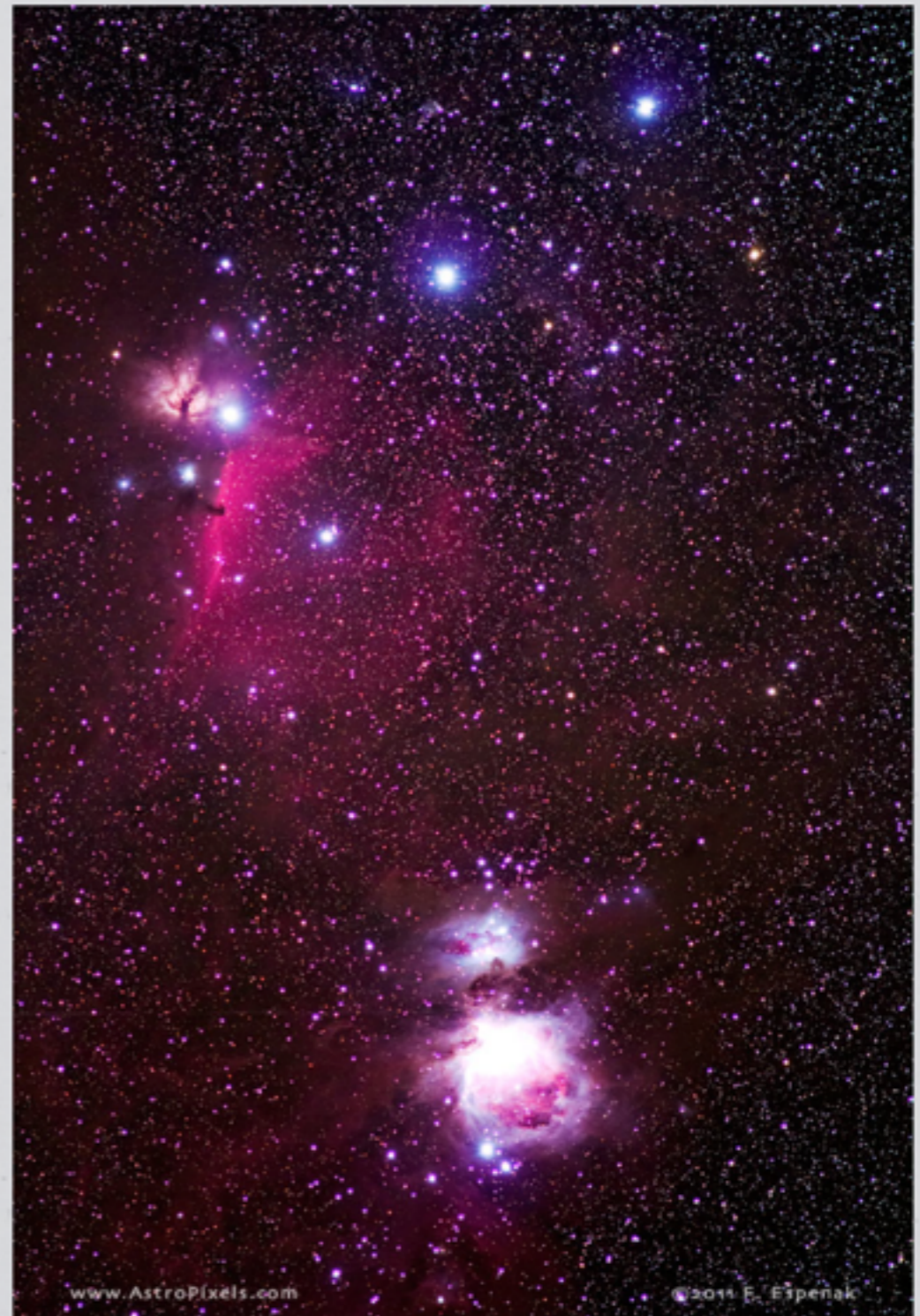
Let's start from observations!

- ★ Stars form out of cold, dense, dusty molecular gas
- ★ Figure shows clumpy star formation in spiral arm
- ★ Gas in arms is compressed, first step toward star formation



Let's start from observations!

- ★ On smaller scales:
 - ★ Giant Molecular Clouds
 - ★ $M \sim 10^6 M_{\text{sun}}$; $R \sim 10 \text{ pc}$
 - ★ **STAR CLUSTERS**
 - ★ Molecular cloud cores
 - ★ $M \sim \text{few } M_{\text{sun}}$; $R \sim 0.1 \text{ pc}$
 - ★ **STARS**



Outline

- ★ Basic Physics of star formation
 - ★ Jeans Mass
 - ★ Cooling
- ★ Forming the first stars in dark-matter halos
- ★ From the first stars to the first galaxies

Basic physics of star formation

★ Star forming regions experience struggle between:

★ Gravity

- acts to collapse the cloud

★ Pressure

★ Magnetic fields

★ "Bulk motions"



- sources of support preventing collapse

If gravity wins, on what timescale is the collapse happening?

Basic physics of star formation

★ Star forming regions experience struggle between:

★ Gravity

- acts to collapse the cloud

★ Pressure

~~★ Magnetic fields~~

~~★ "Bulk motions"~~



- sources of support preventing collapse

Collapse is on dynamical gravitational time:

$$t_G \sim \sqrt{\frac{R^3}{2GM}} \sim \frac{1}{\sqrt{G\rho}}$$

The Jeans mass

★ What is the minimum mass for collapse?

★ Gravity - acts to collapse the cloud

★ Pressure - prevents collapse

The Jeans mass

★ What is the minimum mass for collapse?

★ Gravity - acts to collapse the cloud

★ Pressure - prevents collapse

Borderline case is that of hydrostatic equilibrium:

- Gravitational Energy: $E_G \sim -\frac{G M M}{L}$
- =
- Thermal Energy: $E_T \sim N k T$

For volume of linear size L , N gas molecules of mass m

The Jeans mass/length

★ Gravitational/Thermal energy:

$$\frac{|E_G|}{E_T} \sim \frac{G M^2}{L N k T} \sim \frac{G (\rho L^3) m}{L k T}$$

The Jeans mass/length

★ Gravitational/Thermal energy:

$$\frac{|E_G|}{E_T} \sim \frac{G M^2}{L N k T} \sim \frac{G (\rho L^3) m}{L k T}$$

★ Length at which they are equal is Jeans length:

$$L_J \sim \left(\frac{k T}{G \rho m} \right)^{1/2}$$

Jeans mass is then simply ρL_J^3

Timescales (another derivation)

★ Collapse time vs. sound crossing time:

$$t_G = \frac{1}{\sqrt{G \rho}} \quad t_S = \frac{L}{c_S} \quad c_S \sim \left(\frac{k T}{m} \right)^{1/2}$$

Timescales (another derivation)

★ Collapse time vs. sound crossing time:

$$t_G = \frac{1}{\sqrt{G \rho}} \quad t_S = \frac{L}{c_S} \quad c_S \sim \left(\frac{k T}{m} \right)^{1/2}$$

★ Let's take the ratio and see when they are equal:

$$\frac{t_S}{t_G} \sim \frac{L \sqrt{G \rho}}{c_S} \sim L \left(\frac{G \rho m}{k T} \right)^{1/2}$$

Jeans length (again)!

$$L_J \sim \frac{c_S}{\sqrt{G \rho}}$$

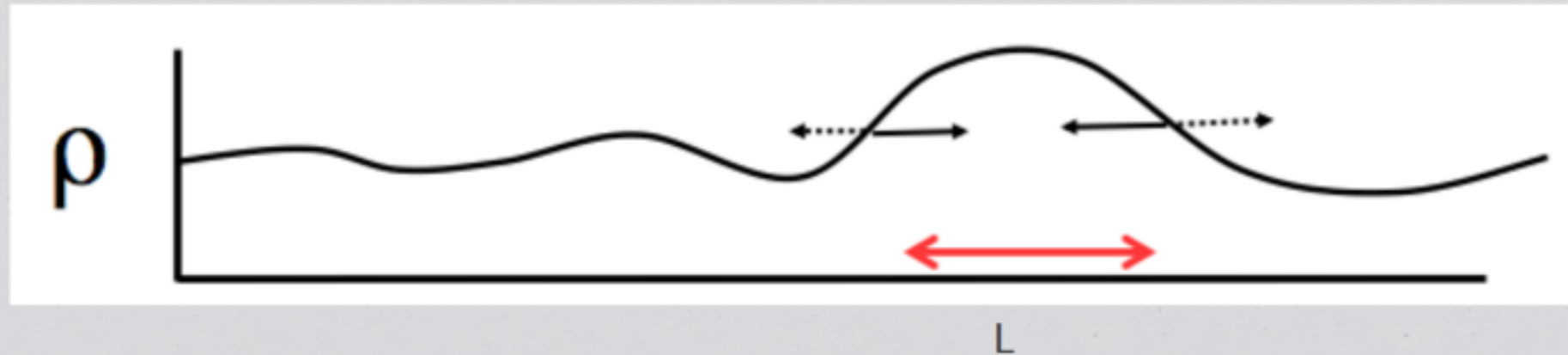
The Jeans mass/length



$$L_J \sim \left(\frac{k T}{G \rho m} \right)^{1/2}$$

- ★ $L > L_J$: gravity wins
- ★ $L < L_J$: pressure wins

The Jeans mass/length



$$L_J \sim \left(\frac{k T}{G \rho m} \right)^{1/2}$$

- ★ $L > L_J$: gravity wins
- ★ $L < L_J$: pressure wins

Why and how cooling is tilting the balance?

A consistency check:

★ Lets take molecular clouds in the local Universe:

★ $\rho \sim 10^{-19} \text{ g cm}^{-3}$

★ $T \sim 10 \text{ K}$

$$M_j \sim 8 \times 10^{32} \text{ g} \sim 0.4 M_{\text{sun}}$$

$$R_j \sim 10^4 \text{ AU}$$

★ Typical mass and length scales for star formation
about right

The importance of cooling

★ How do we get the right conditions for star formation?

★ Gas in the Interstellar Medium is not dense enough

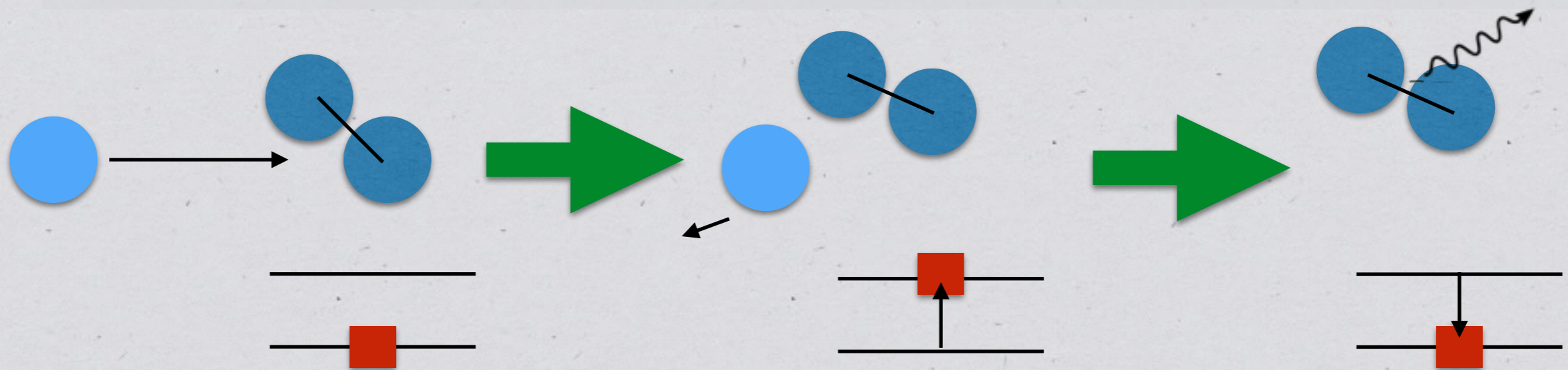
★ Gas after a dark-matter halo virializes is too hot (shock heated to halo T_{vir})

★ How can gas cool?

Radiative cooling

★ Collisions in gas excite atomic/molecular levels

★ Return to ground state by γ emission



★ How do you expect cooling to depend on metallicity of gas?

Radiative cooling and “metals”

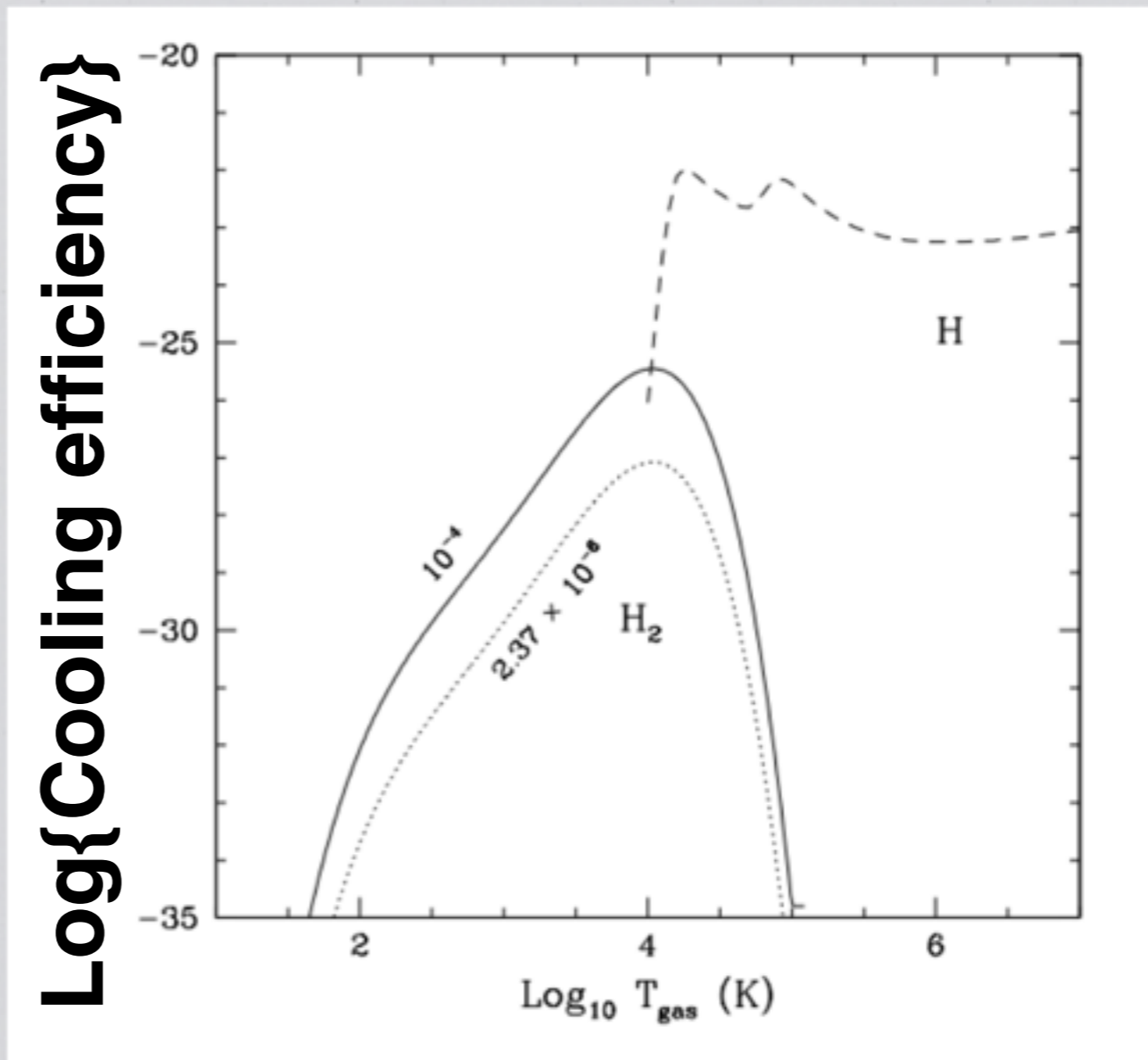
- ★ The more “metals” the more efficient the cooling:
many energy levels available
- ★ Simple atoms and molecules are inefficient at radiative cooling
- ★ Metal-free gas ($Z < 10^{-3.5} Z_{\text{Sun}}$) hard to cool
- ★ What is your expectation for the Jeans mass in first gas clouds?

Metal-free gas

★ Cooling below $10^{-3.5} Z_{\text{sun}}$ relies on $\text{Ly}\alpha/\text{H}_2$:

★ Inefficient!

★ But cooling efficiency grows with temperature



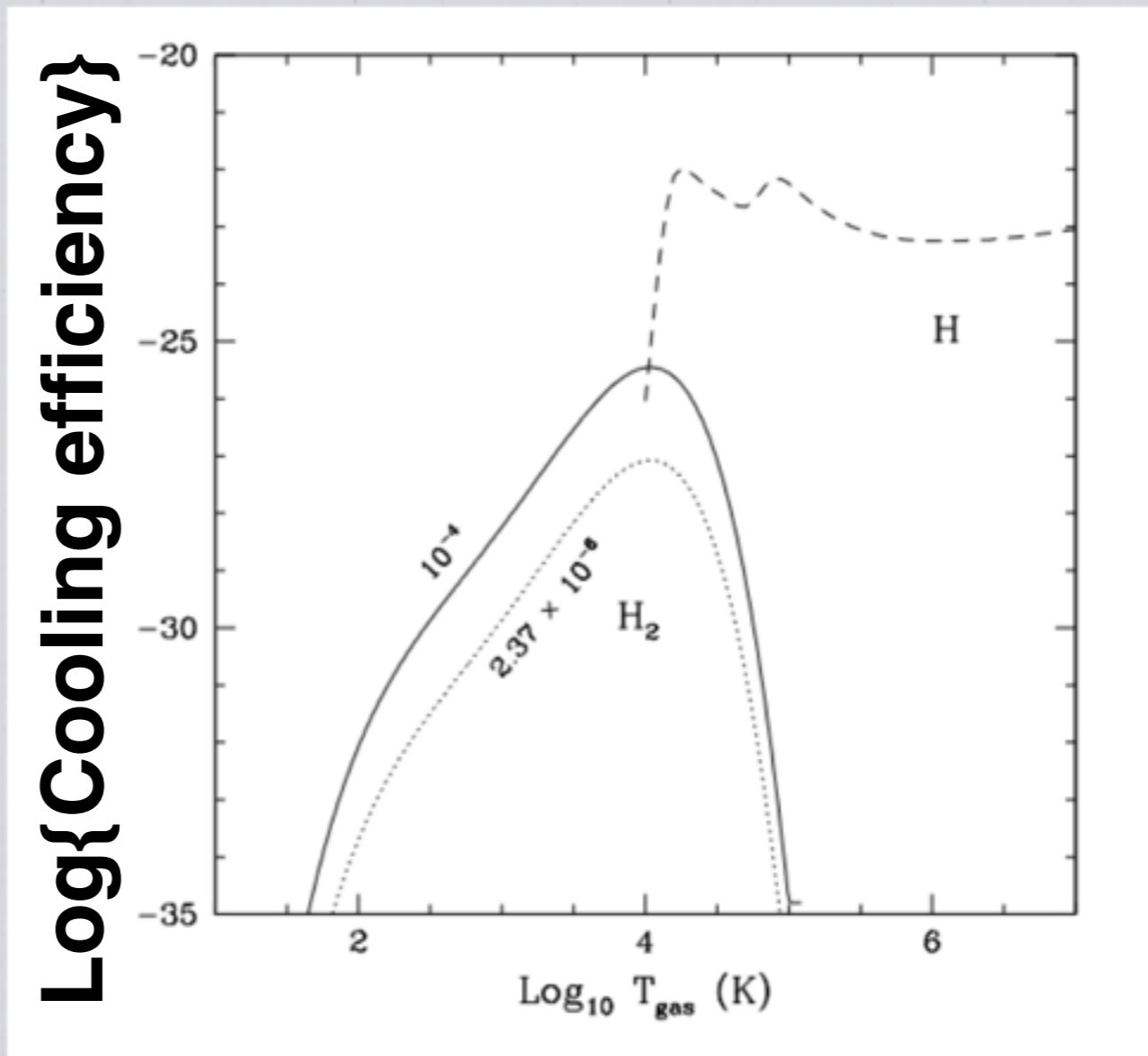
Metal-free gas

★ Cooling below $10^{-3.5} Z_{\text{sun}}$ relies on $\text{Ly}\alpha/\text{H}_2$:

★ Inefficient!

★ But cooling efficiency grows with temperature

★ WHY?



DM halos and cooling of gas

- ★ Temperature of gas in DM halos depends on halo mass and redshift

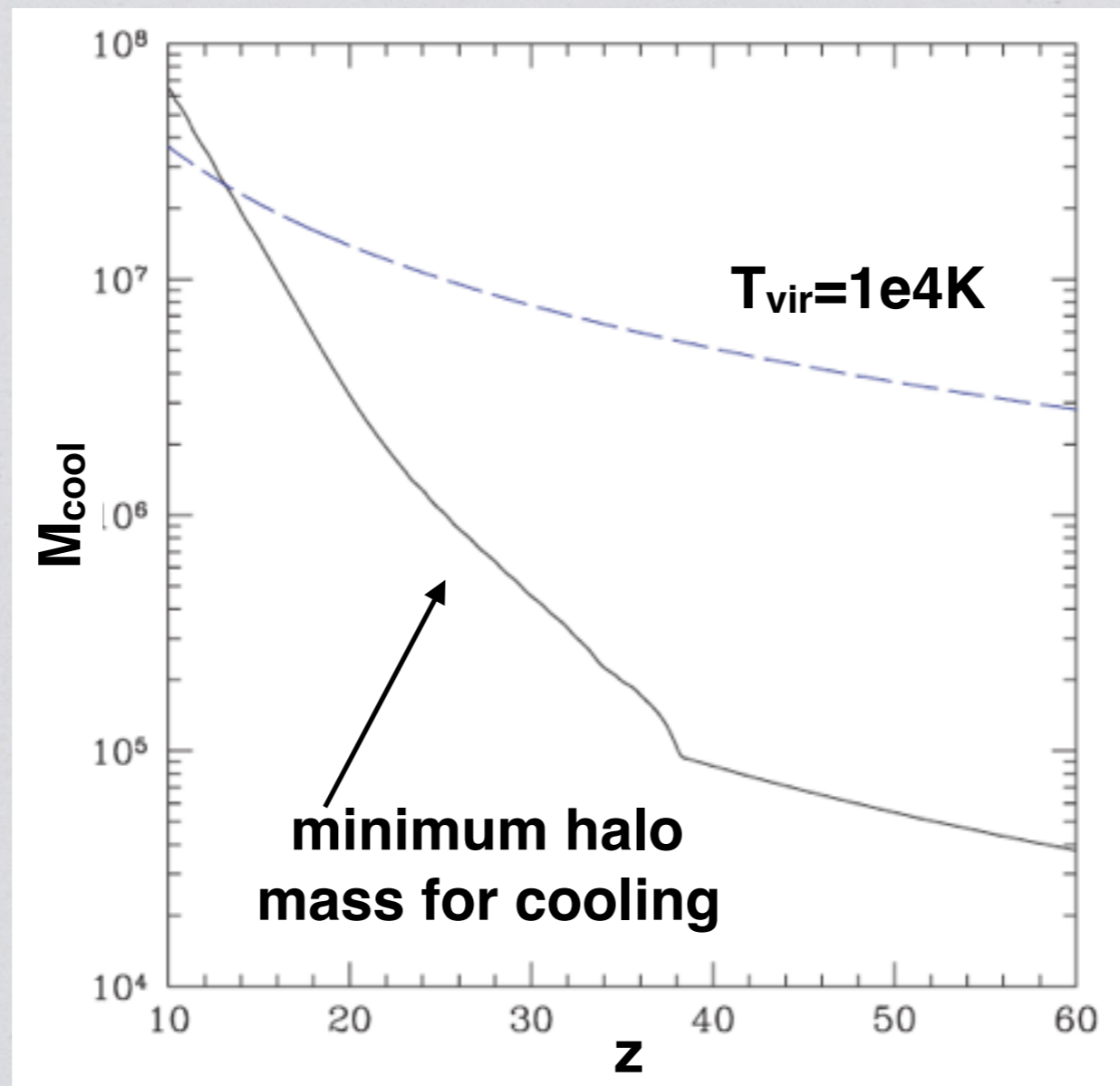
$$T_{\text{vir}}(M, z) \simeq 2554 \text{ K} \left(\frac{M}{10^6 M_{\odot}} \right)^{2/3} \left(\frac{1+z}{31} \right).$$

- ★ There is a minimum halo mass for which cooling is efficient (cooling time less than Hubble time)

$$M_{t_H\text{-cool}} \simeq 1.54 \times 10^5 M_{\odot} \left(\frac{1+z}{31} \right)^{-2.074}.$$

Minimum halo for cooling

Minimum mass for H₂ cooling increases with redshift:
Combination of expansion and radiation



Trenti & Stiavelli (2009)

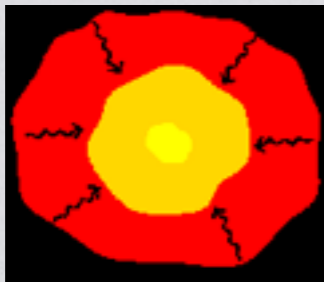
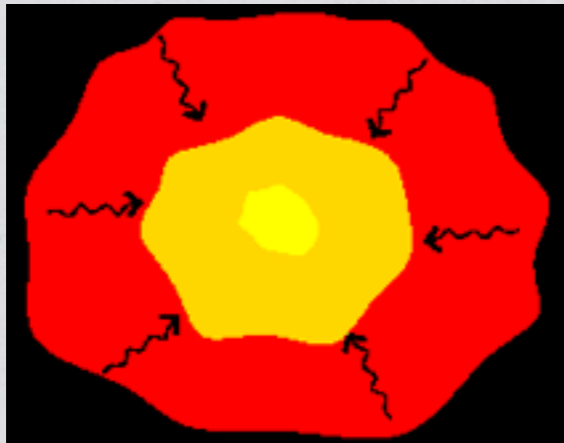
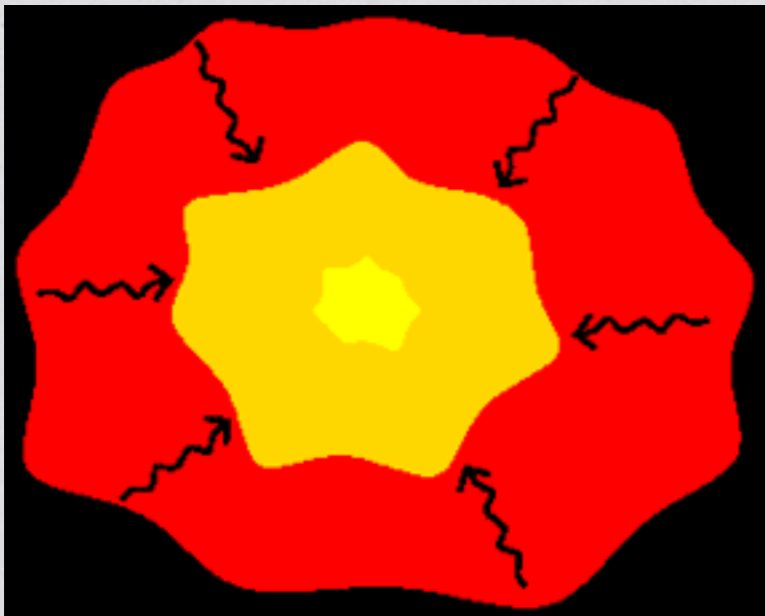
The simple picture

Gas cloud starts to contract

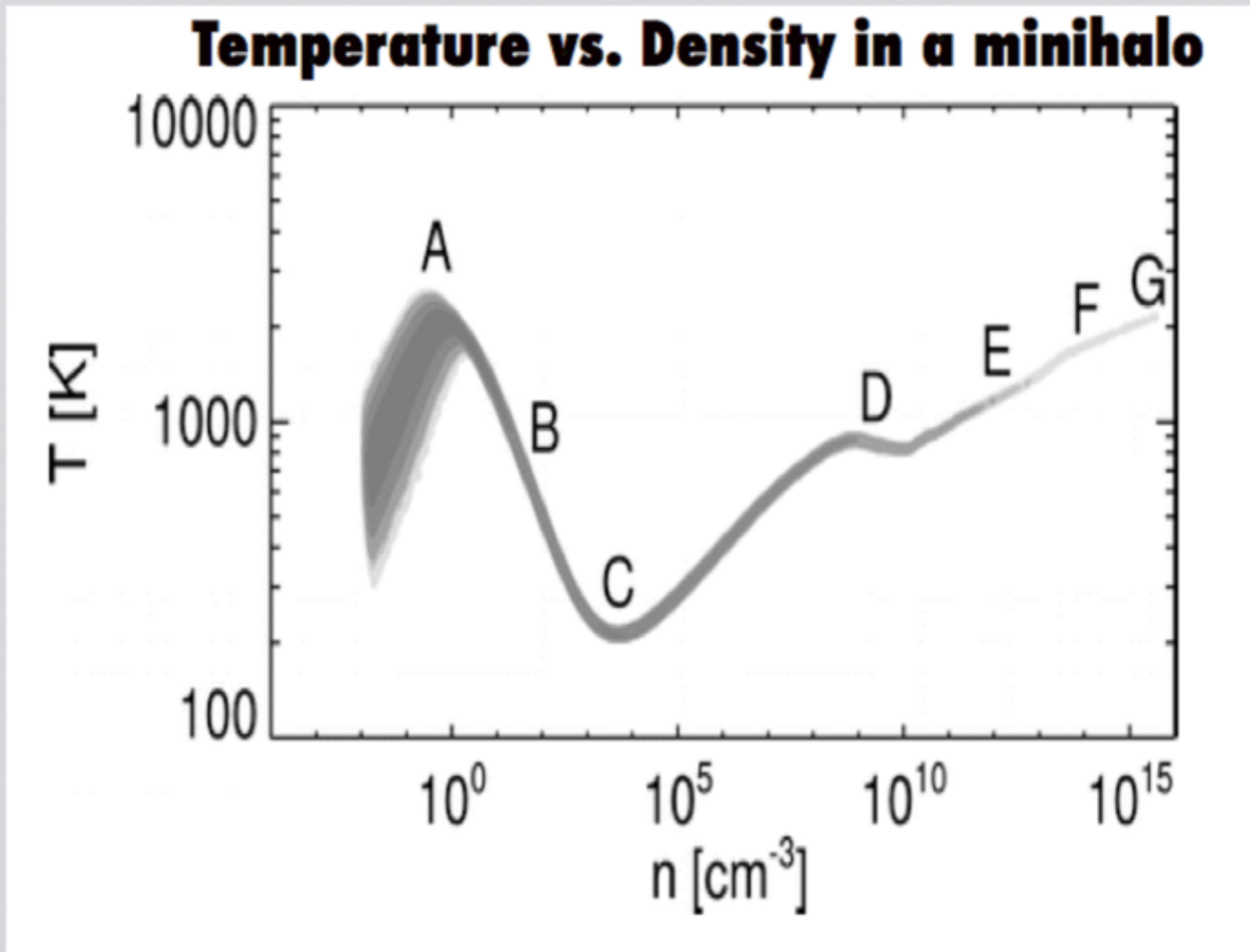
It gets smaller and denser

And smaller...

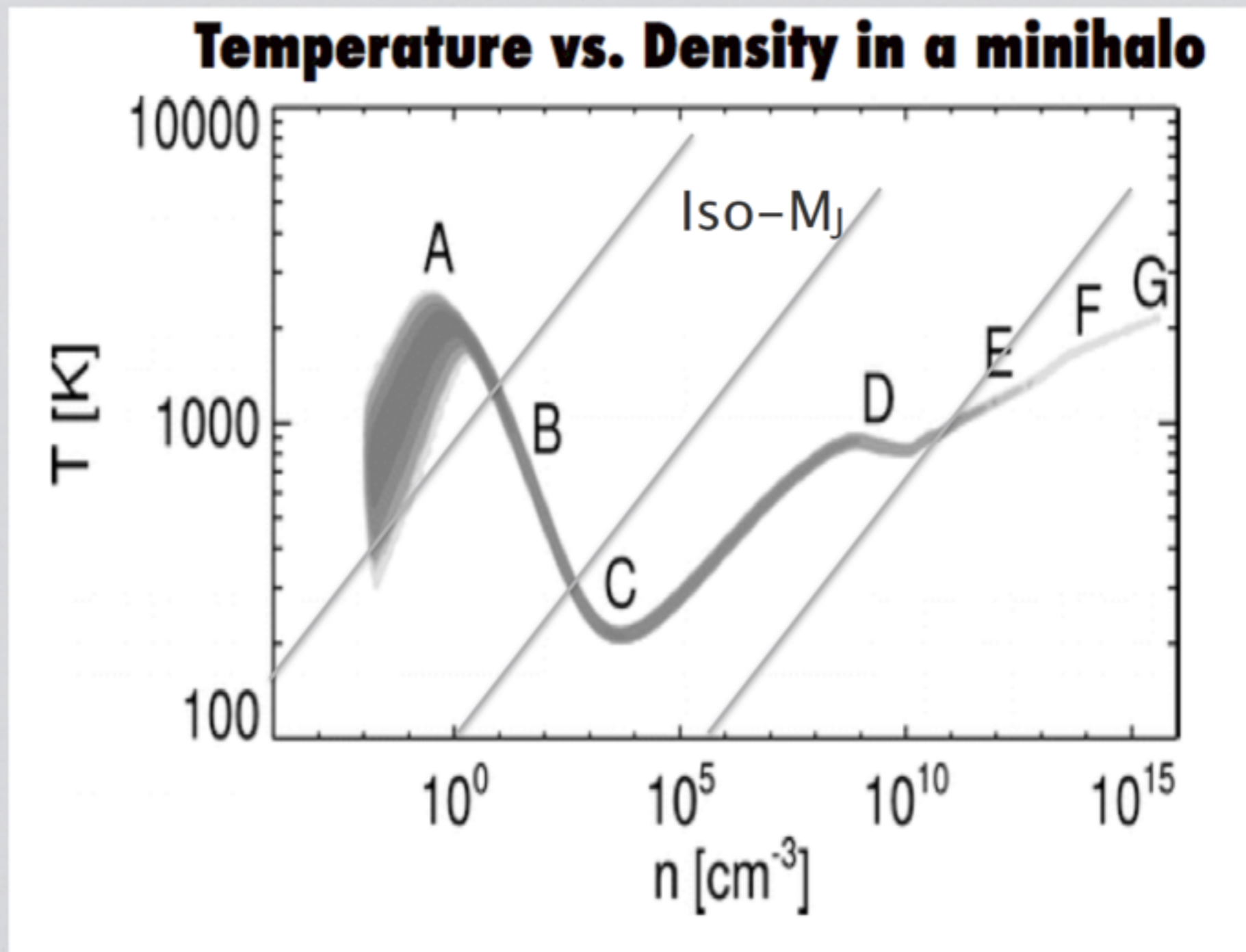
Denser, Hotter until H-fusion begins: A star is born!



Evolution of a minihalo



Evolution of a minihalo



The birth of the first stars

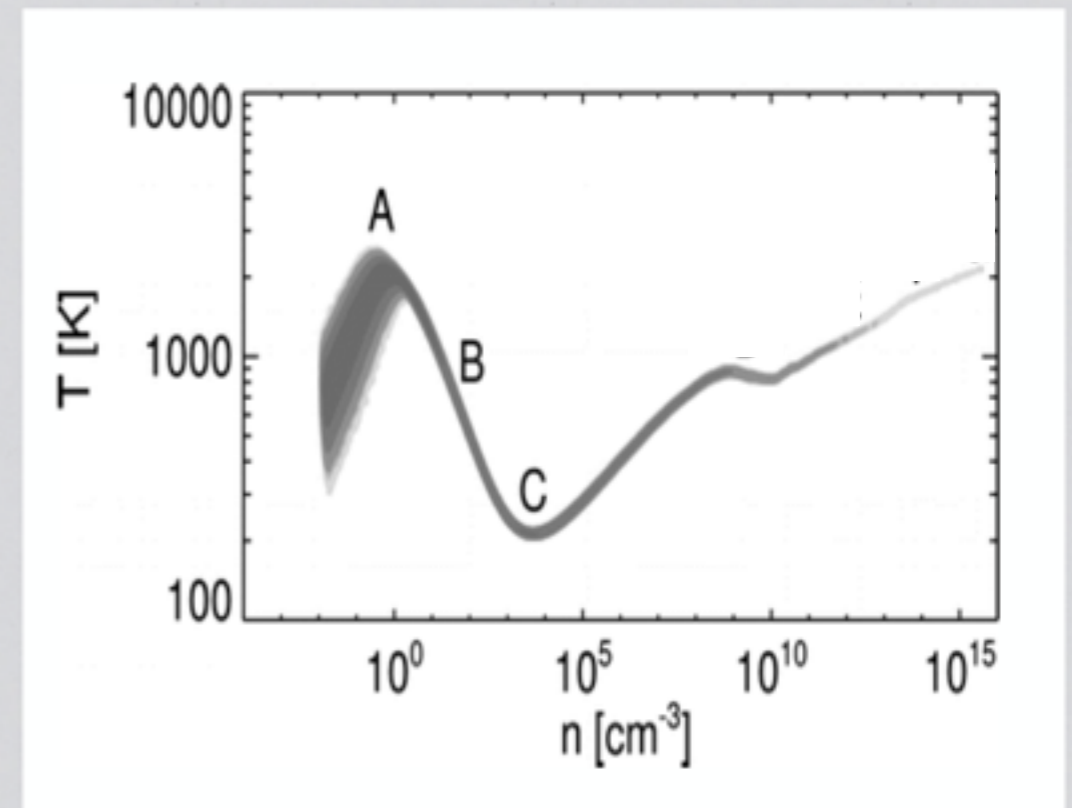
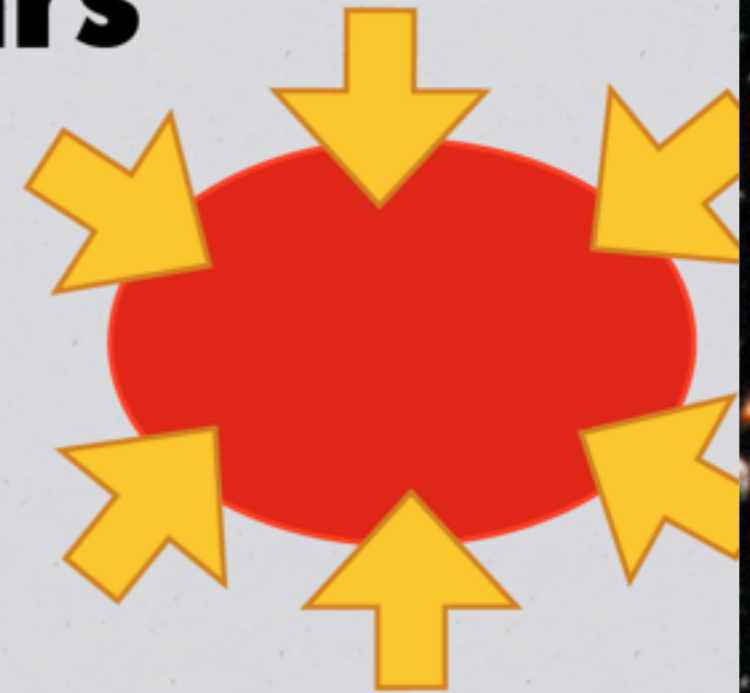
[The minihalo collapses and its gas (hydrogen+helium) reaches equilibrium between gravity and pressure support [A]

[Radiative cooling reduces temperature and rises density [B]

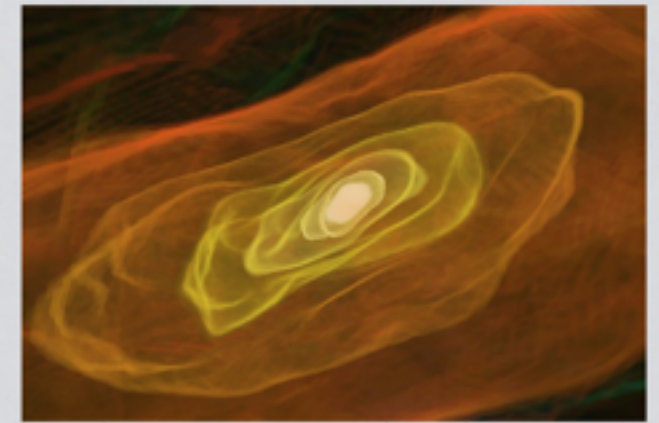
[Critical density for gravitational (Jeans) instability is reached [C]

— Gravity dominates over pressure

— Collapse of $\sim 10^{3-4} M_{\text{sun}}$ of gas



First Star: life & death

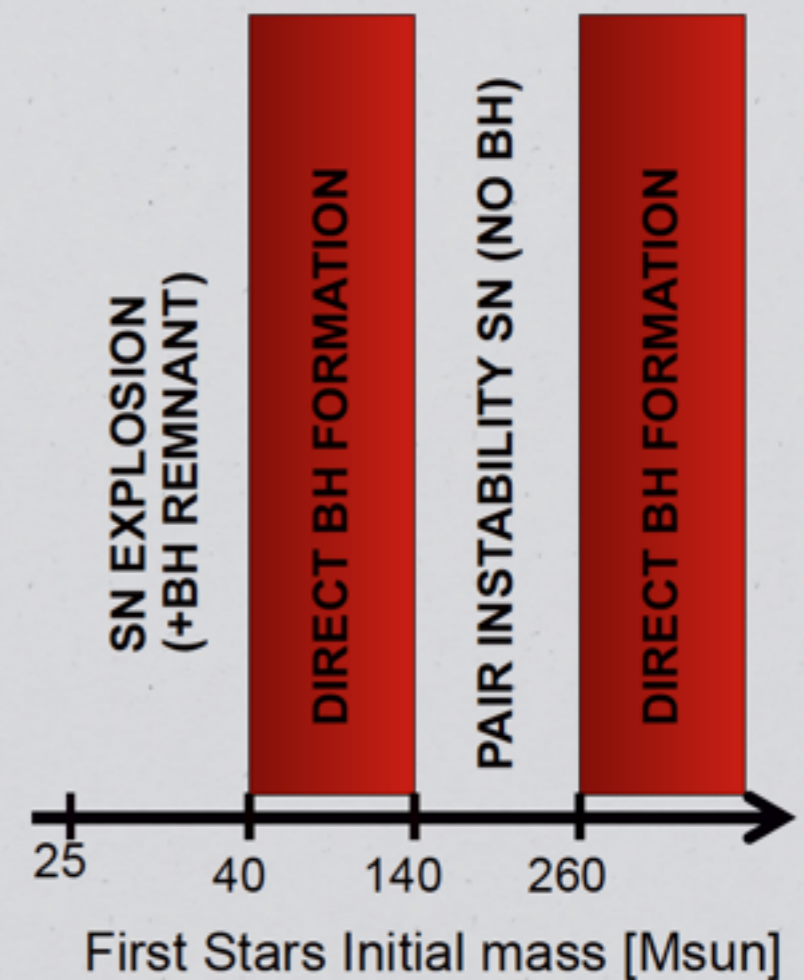


Simulations predict one (or two) stars per minihalo, with heavy masses [$\sim 10-100 M_{\text{sun}}$]

Heavy masses imply short lifetimes (a few Myr)

Supernova explosion can release heavy elements into the interstellar medium

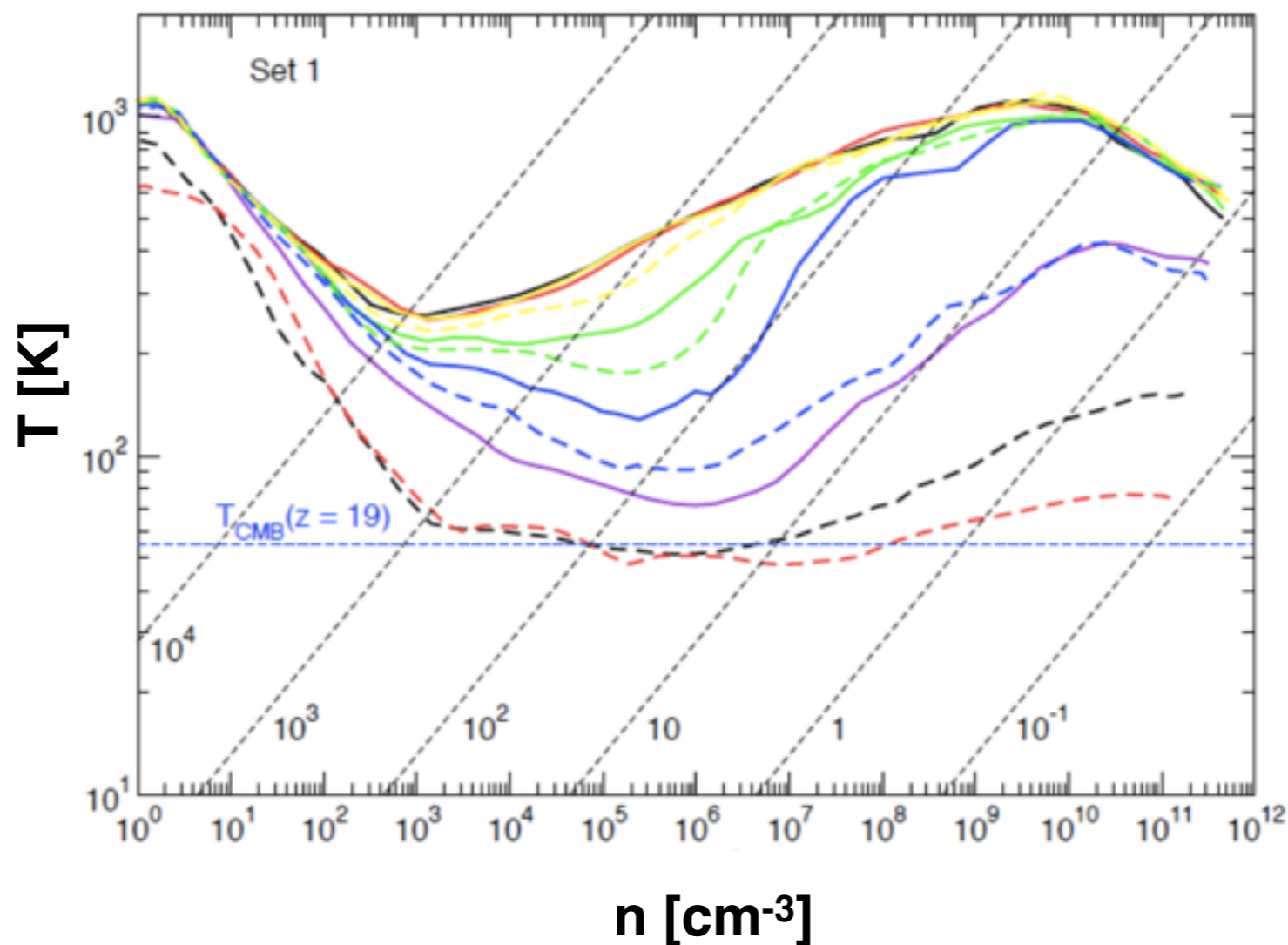
Or... direct black hole formation, possibly providing the first seeds that later grow into supermassive black holes



from Heger et al. (2003)

Metal cooling: transition to PopII

At $Z \sim 10^{-3.5} Z_{\text{sun}}$ Transition from PopIII to PopII



Smith et al. (2009)

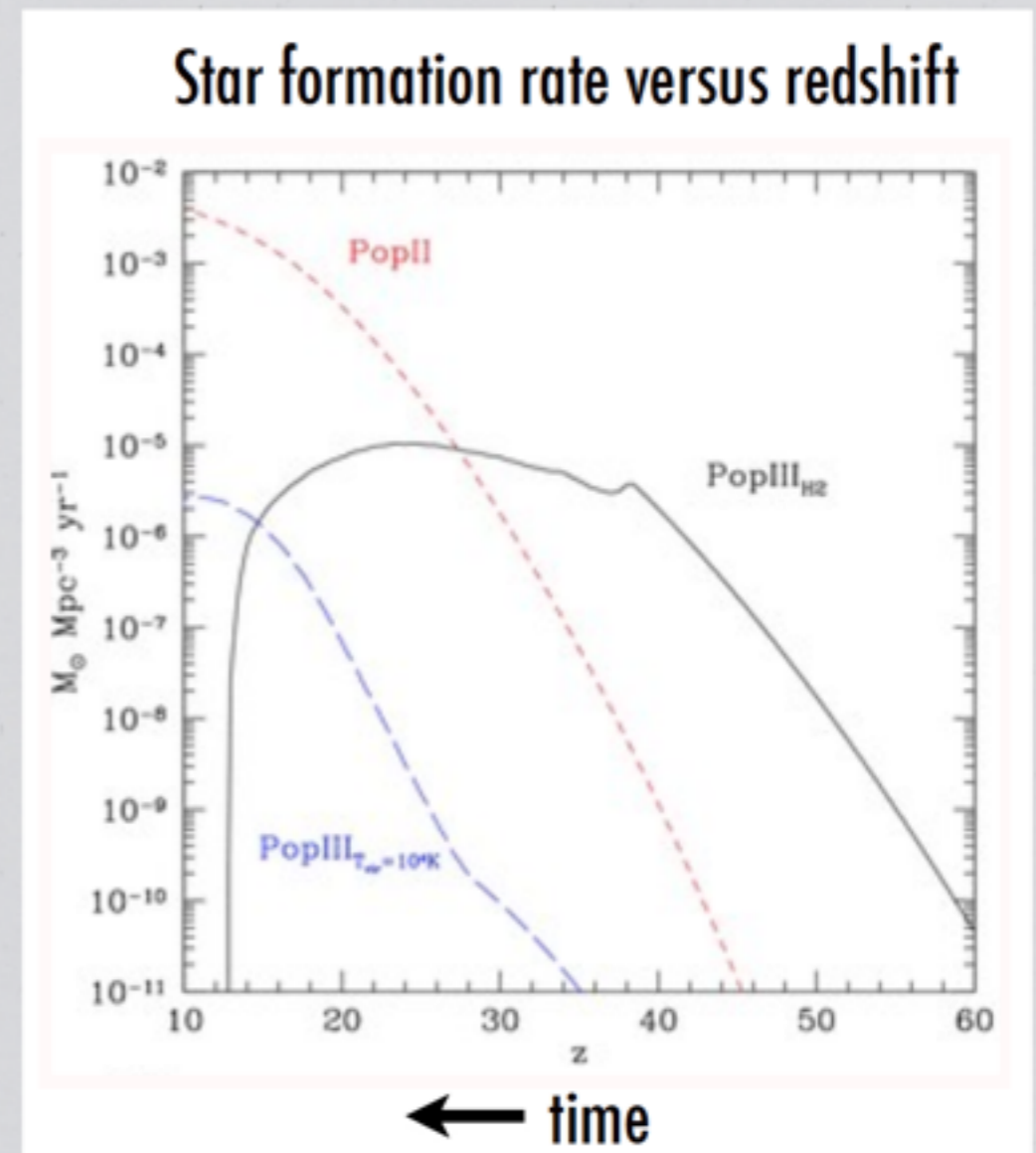
Early Star Formation history

Star formation history evolution:

PopIIIs begin forming very early on ($z > 60$, or $t < 40 \text{ Myr}$) in minihalos ($M_h < 10^{5-6} M_{\text{sun}}$)

Radiative feedback self-regulates their formation rate after $z \sim 35$ ($t \sim 80 \text{ Myr}$), suppressing cooling of gas in minihalos

PopII stars become dominant at $z < 25$ ($t > 150 \text{ Myr}$)



Trenti & Stiavelli (2009)

Summary

- ★ Addition of gas physics to dark-matter dynamics:
 - ★ How can gas cool and form stars?
- ★ Jeans mass (gravity overcome pressure)
- ★ Cooling in the early Universe
- ★ Formation of first stars (PopIII, metal free)
- ★ Transition to first galaxies (metal enriched)

Suggested readings

★ Tegmark et al. (1997), ApJ, 474, 1

★ How small were the first cosmological objects?