

# Order of Magnitude Icebreaker



**How many galaxies in the Universe?**



# Order of magnitude modeling: The basics

★ Goal:

★ Understand the basic **but key** ingredients

★ Obtain quick but reasonable answer

★ Approach:

★ Simplify as much as possible  
“Spherical Horse”



★ Identify scaling relations and use known anchors

★ Take (informed) guesses if needed

# **A very simple example: How many galaxies in the Universe?**



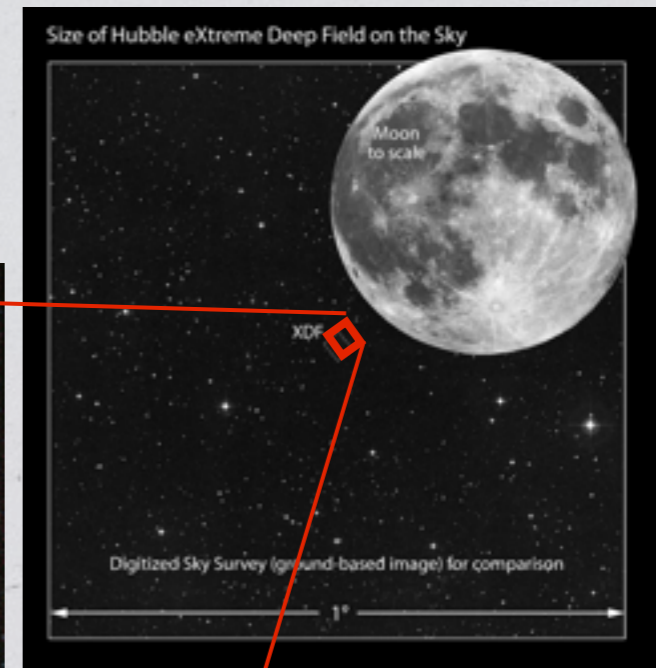
- ★ Think for 3 minutes about how to proceed
  - ★ Don't discuss with other students (yet)
  - ★ Use your physical intuition, not google!
  - ★ Remember: Multiple approaches possible!
- ★ Now discuss for 2 minutes with your neighbour

# How many galaxies in the Universe?



- ★ Let's collect ideas and discuss them!
- ★ Estimate from small area ultradeep observations
- ★ Estimate from Local Group galaxy density
- ★ Estimate from baryonic content in the Universe
- ★ .....

# Estimate from ultradeep observations



- We can count galaxies from Hubble *eXtreme Deep Field* [*~23 days of exposure time*]

# Estimate from ultradeep observations

- ★ This image contains ~5000 galaxies
- ★ Area ( $4 \text{ arcmin}^2$ ) is one part in 13 million of the full sky
- ★  $N_{\text{gal}} \sim 5000 \times 1.3 \times 10^7$



$$N_{\text{gal}} \sim 65 * 10^9$$

NASA/ESA, XDF team

# Estimate from Local Group density

★ Idea:

$$★ N_{\text{gal}} = N_{\text{gal}}^{\text{(LocalGroup)}} * \text{Volume} / \text{Volume}^{\text{(LocalGroup)}} / \eta$$

$$★ N_{\text{gal}}^{\text{(LocalGroup)}} \sim 100$$

$$★ \text{Volume: } r \sim 4 \text{ Gpc sphere } (r_{\text{eff}} \sim r/2) \sim 3 * 10^{10} \text{ Mpc}^3$$

$$★ \text{Volume}^{\text{(LocalGroup)}} \sim 4 \text{ Mpc}^3$$

$$★ \eta \sim 10 \text{ [Local group overdensity]}$$

$$N_{\text{gal}} \sim 80 * 10^9$$

# Estimate from baryonic content of the Universe

★ Idea:

$$\star N_{\text{gal}} = \text{Volume} * \langle \rho \rangle_{\text{gas}} * \text{Efficiency}_{\text{star formation}} / M_{\text{gal}}$$

$$\star \text{Volume: } r \sim 4 \text{ Gpc sphere } (r_{\text{eff}} \sim r/2) \sim 3 * 10^{10} \text{ Mpc}^3$$

$$\star \langle \rho \rangle_{\text{gas}} \sim 10^{11} M_{\text{sun}} / \text{Mpc}^3 * \Omega_b / \Omega_{\text{DM}}$$

$$\star \text{Efficiency}_{\text{star formation}} \sim 0.1$$

$$\star M_{\text{gal}} \sim 10^9 \text{ Sun}$$

$$N_{\text{gal}} \sim 70 * 10^9$$

# Order of magnitude estimates

## Ideas to bring home



- ★ Multiple pathways, depending on available information
  - ★ Good illustration of what research is about
- ★ Do not hesitate to simplify as much as possible
- ★ Rescale to situations you are familiar with
- ★ Basic physics can give good insight on many problems!

**Next: Problems for this week**

# Order of Magnitude Group Projects



## ★ Basic goals:

- ★ Experience a simple but interesting research project
- ★ Learn to apply in practice what you learned at the University
- ★ Learn to collaborate with peers
- ★ Learn to present results effectively

# Order of Magnitude Group Projects



★ Nine projects proposed, with variety of

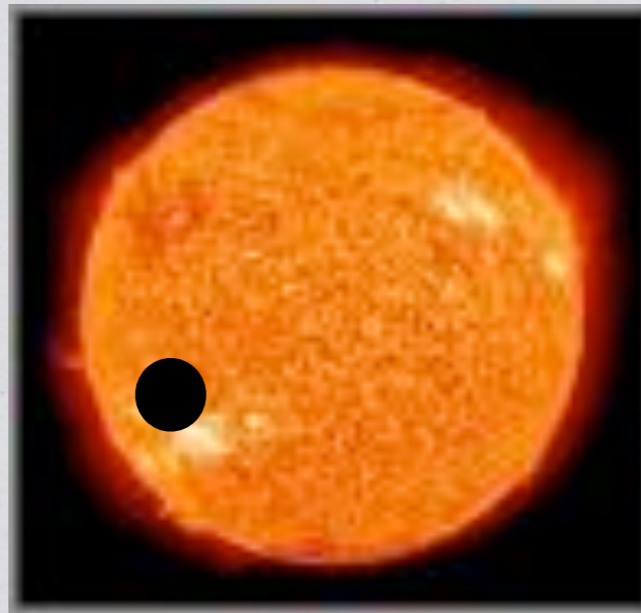
★ Topics

★ Level of difficulty

★ Type of skills needed to work on them

**Let's briefly look at them!**

# A black hole collides with the Sun!



★ Imagine that a black hole of mass  $M_{\text{BH}} < M_{\text{Sun}}$  collides with the Sun

★ What is the minimum  $M_{\text{BH}}$  that we can detect?

# Formation of life in the Universe



★ Is life likely to emerge at the present time around a star like the Sun?

# A starship drifting in a globular cluster



★ What is the probability of colliding with a star in a globular cluster?

# The luminosity density in the Universe



★ Which type of galaxies dominate the luminosity density in the Universe?

# Limits on the mass of stars



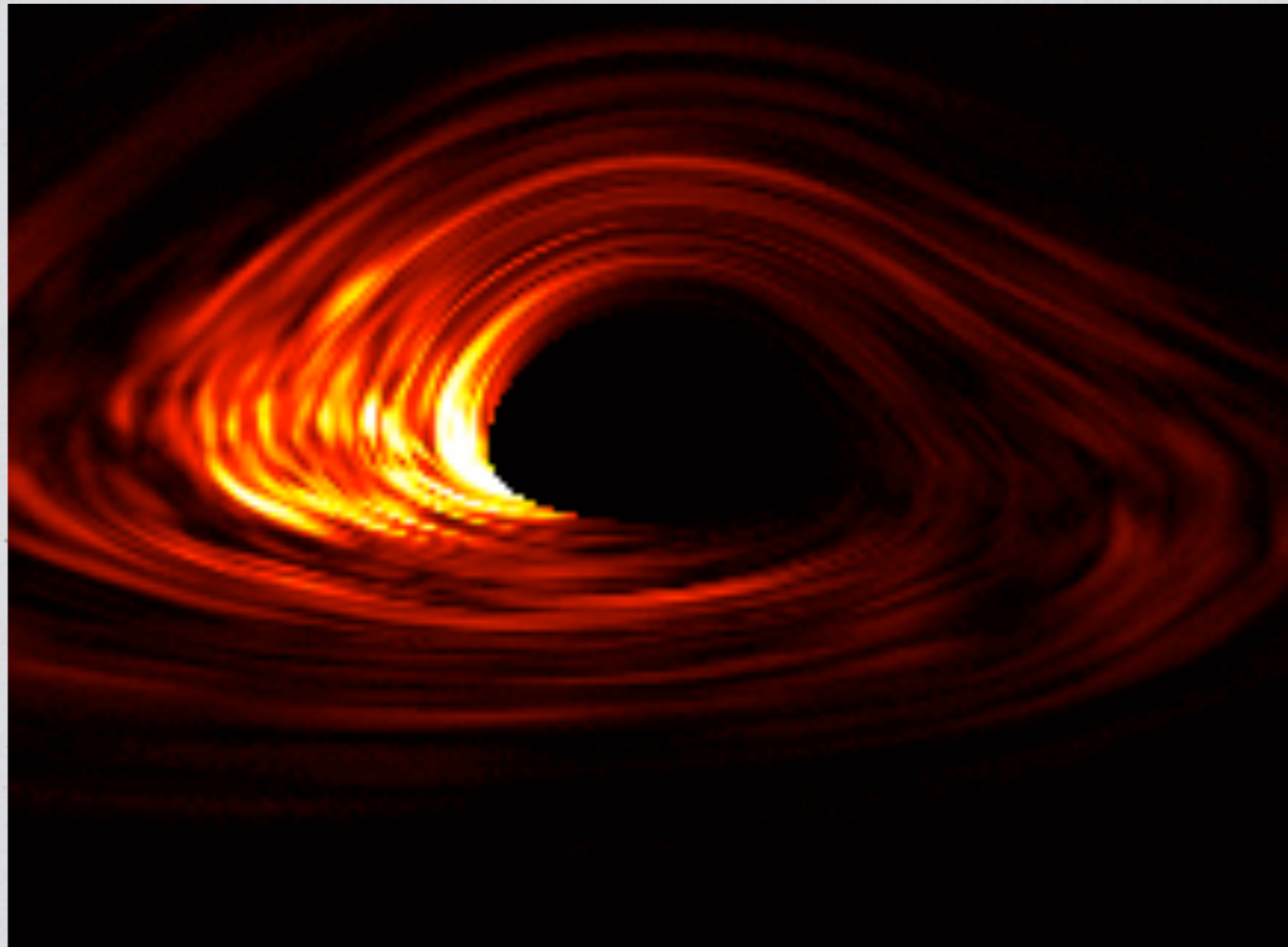
★ What are the upper and lower mass limits for a star?

# The growth of supermassive black holes



★ How quickly can a supermassive black hole reach  $10^9 M_{\text{sun}}$ ?

# Accretion on black holes



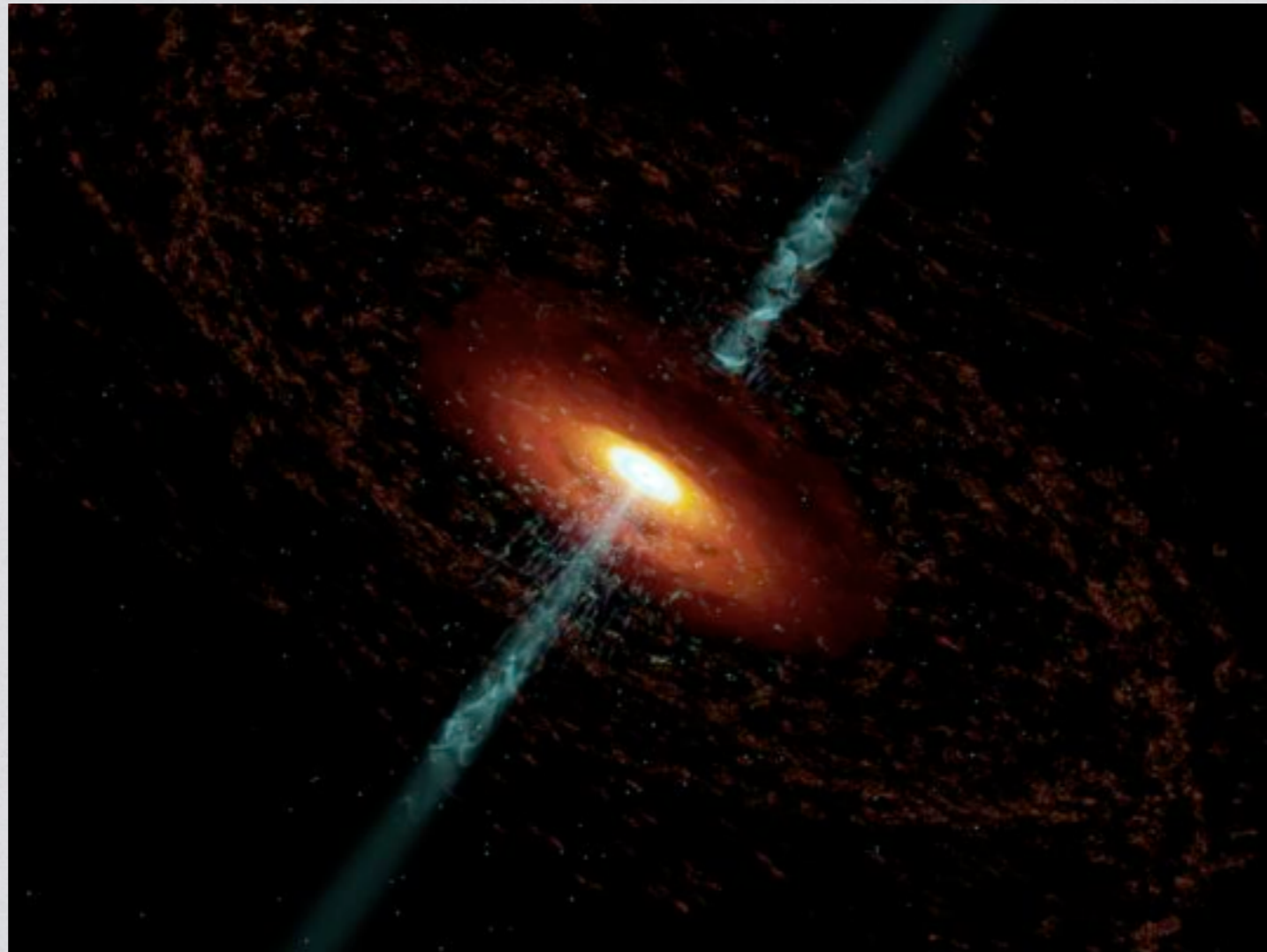
★ Derive the maximum rate for black hole growth

# Radiation from accreting black holes



★ Characterize radiative processes in black hole jets

# Black hole jets: Superluminal motion



★ Is it possible to observe apparent velocities exceeding the speed of light in blazars?

# Organization

- ★ Take some time to read the full description of the 2-3 problems that you find most interesting
- ★ Write down your name on the whiteboard for your preferred problem (and for your second choice)
- ★ Start the project (with your team):
  - ★ Two afternoons of team work
  - ★ One afternoon to prepare a presentation
  - ★ Present on Friday