

# STAR CLUSTERS

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## Lecture 4

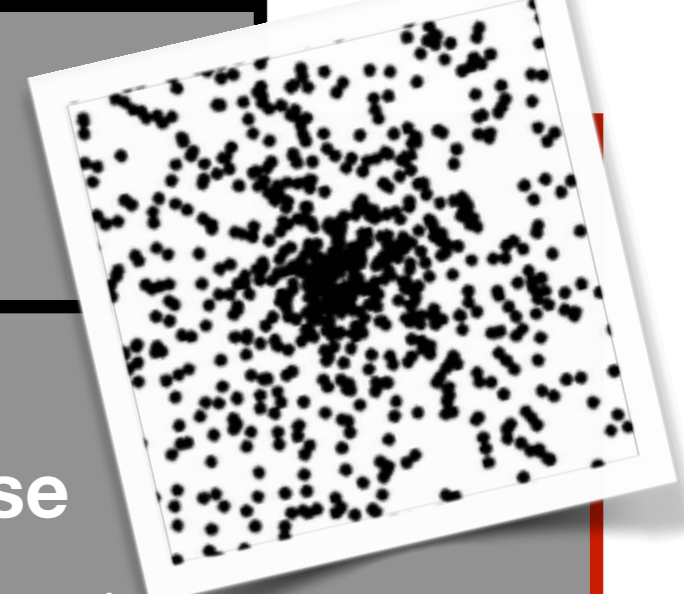
### Intermediate-Mass Black Holes



Nora Lützgendorf (ESA)



# LECTURE 3



## 1. The Gravitational N-body problem

- $N=2$ : exactly solvable
- $N=3$ : approximately solvable
- $N>3$ : only numerical solvable

## 2. Dynamic Equilibrium

- No EXPANSION or CONTRACTION of the system

## 3. Negative Heat Capacity

- Remove energy  $\rightarrow$  hotter
- Gain energy  $\rightarrow$  colder

## 4. Core Collapse

- Very condensed core, steep light profile

## 5. Equipartition of Energies

- All the stars (at radius  $R$ ) have the same kinetic energy
- High-mass stars: slow, low-mass stars: fast

## 6. Mass Segregation

- Mass gradient from center to the outskirts



# Outline

## 1. Introduction

- What, How, Where?

## 2. Observations

- Photometry

- Spectroscopy

## 3. Simulations

## 4. Future



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- What, How, Where?

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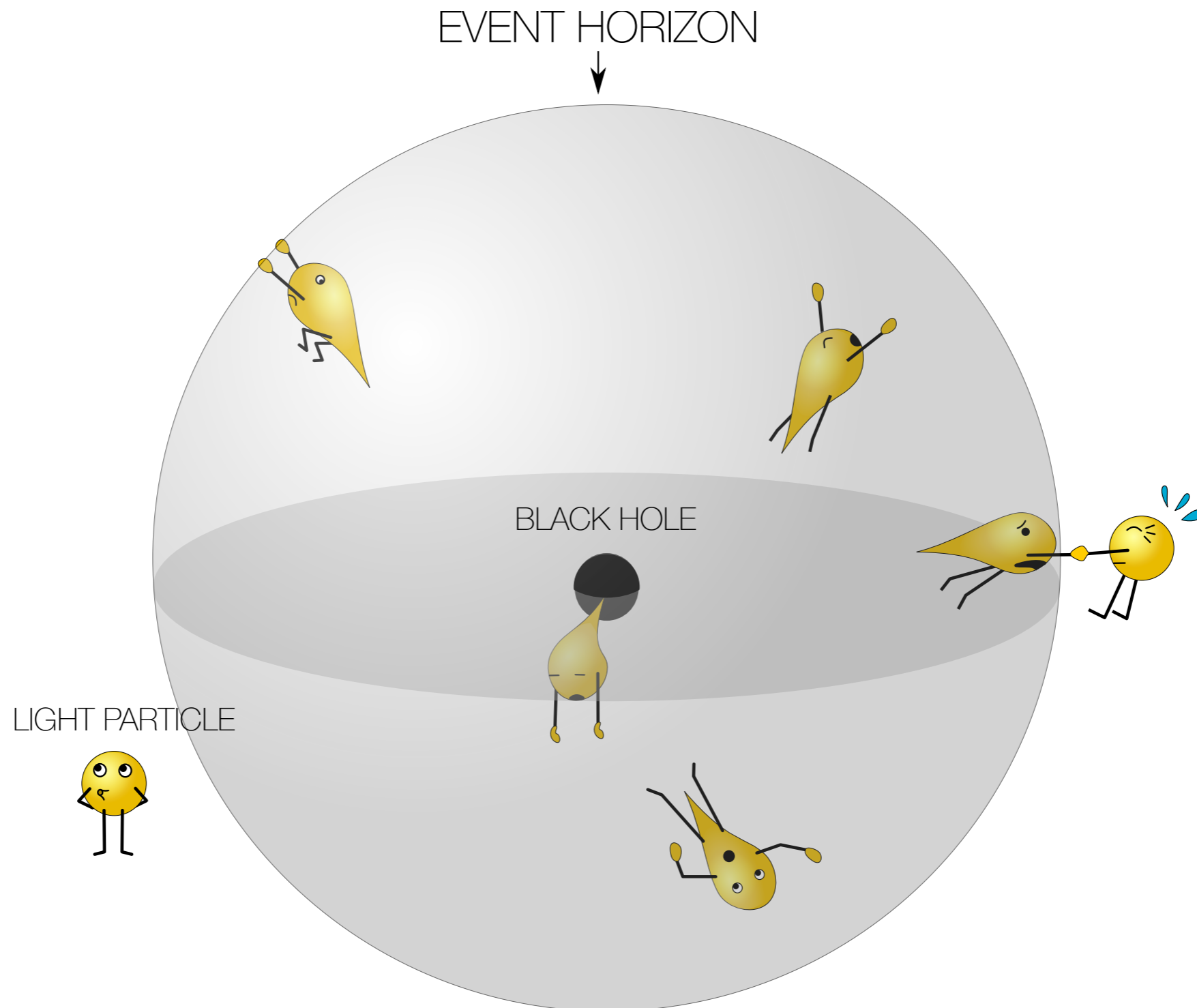
- Spectroscopy

## 3. Simulations

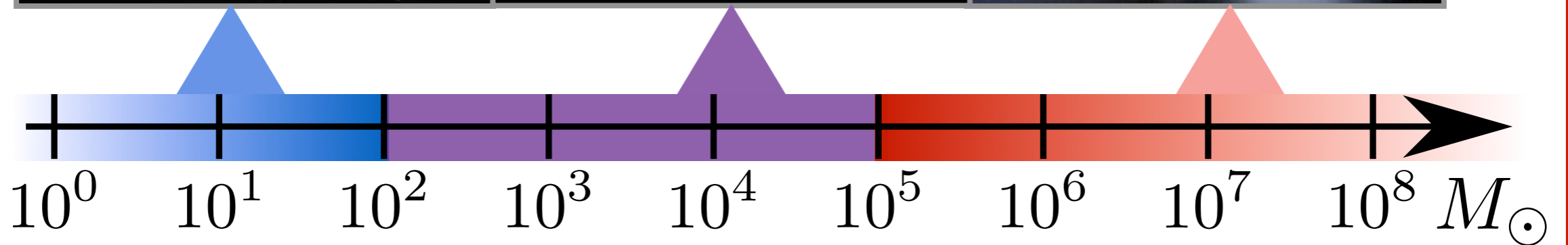
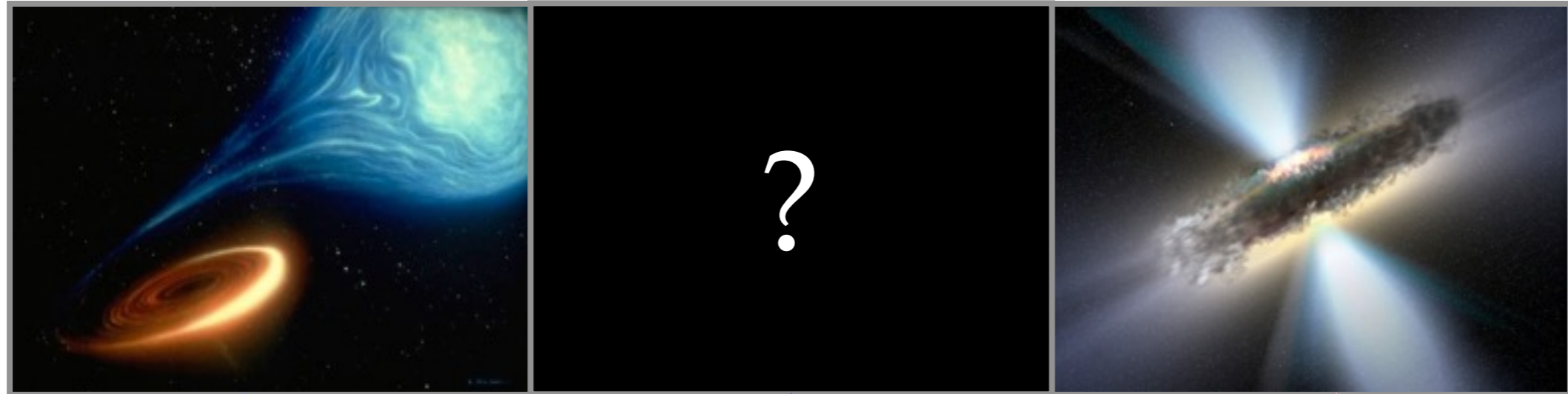
## 4. Future



# What is a Black Hole?



# What are IMBHs?



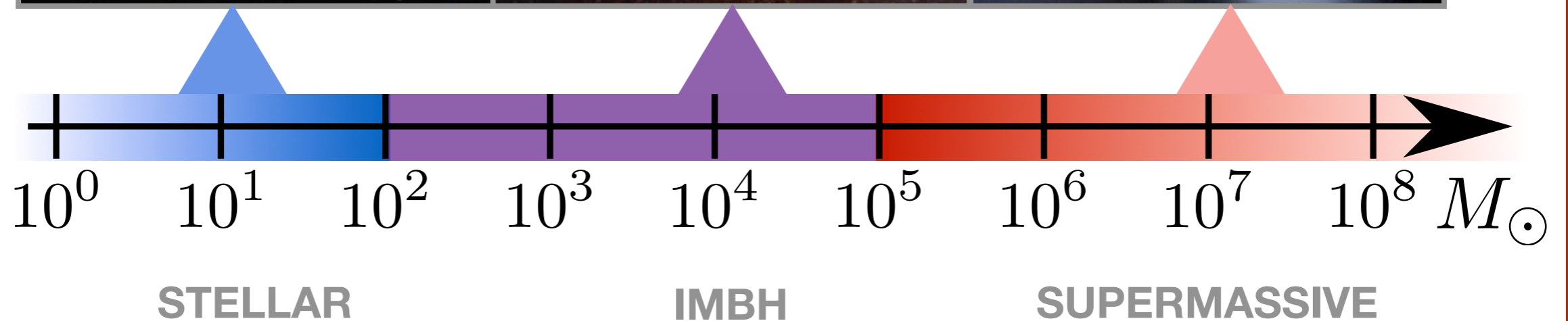
## STELLAR

- Gravitational Collapse of Massive Star
- Supernovae
- Compact X-ray Binaries
- ...

## SUPERMASSIVE

- Centers of Massive Galaxies
- Active Galactic Nuclei
- Quasars
- Center of the Milky Way
- ...

# What are IMBHs?



- Gravitational Collapse of Massive Star
- Supernovae
- Compact X-ray Binaries
- ...

- Centers of Massive Galaxies
- Active Galactic Nuclei
- Quasars
- Center of the Milky Way
- ...

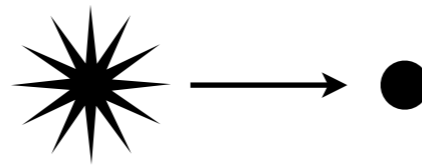
# How do they form?

STELLAR

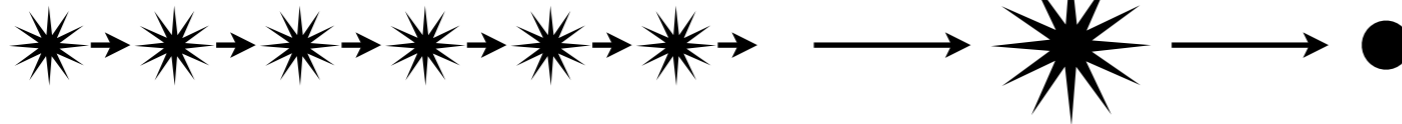
INTERMEDIATE

SUPERMASSIVE

STELLAR REMNANTS



RUNAWAY MERGER



RUNAWAY COLLISIONS



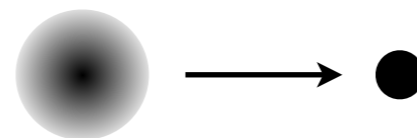
STELLAR GAS ACCRETION



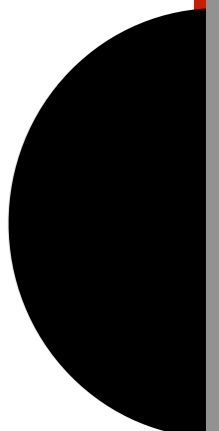
BH GAS ACCRETION



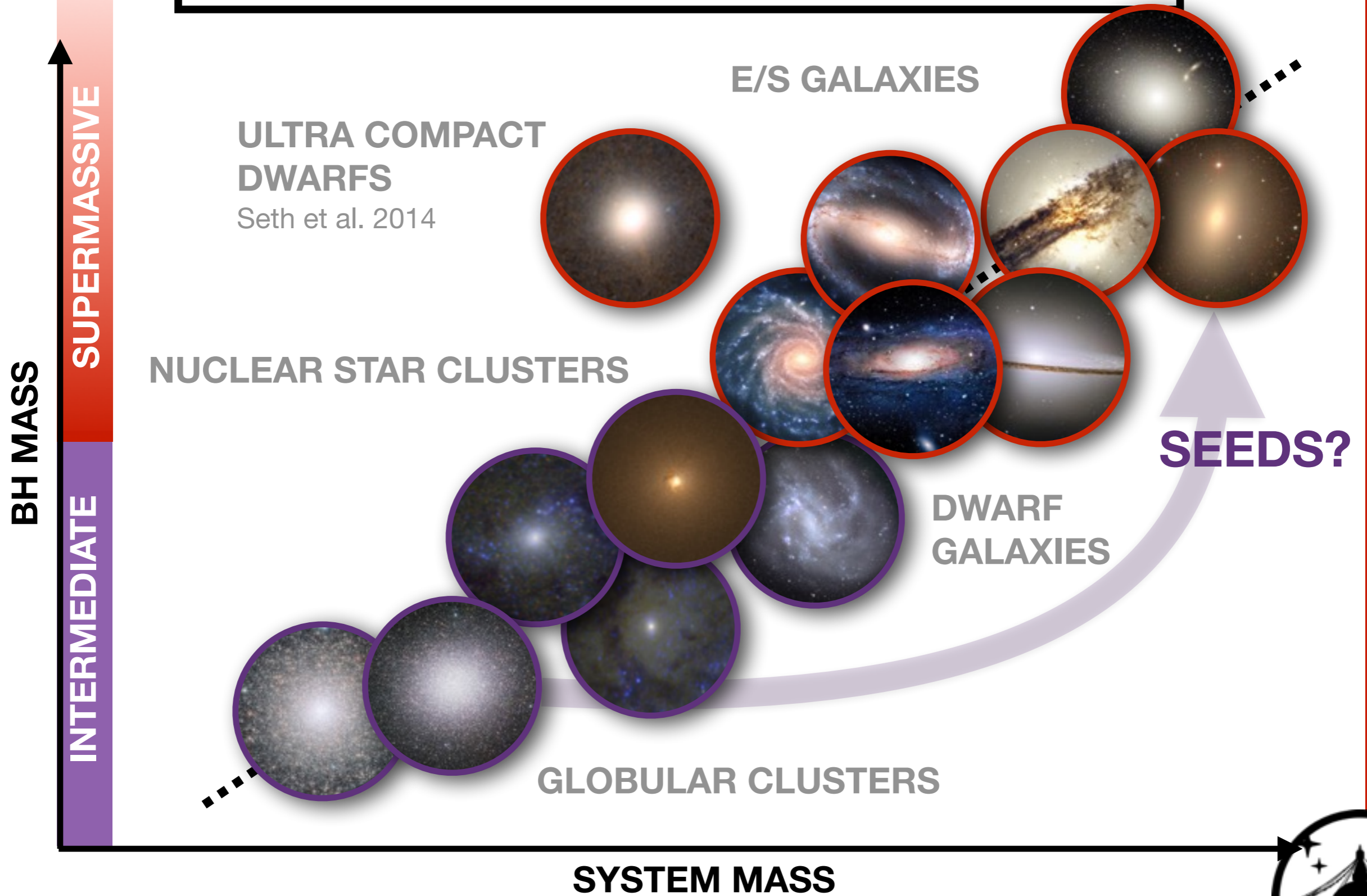
DIRECT COLLAPSE



FURTHER ACCRETION?



# Where do we find them?



# Outline

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- Spectroscopy

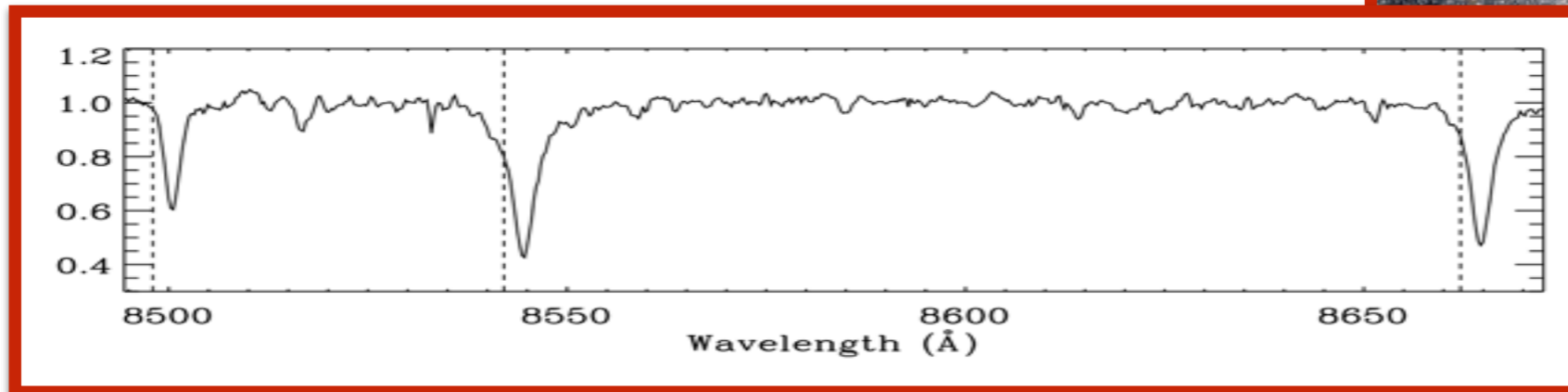
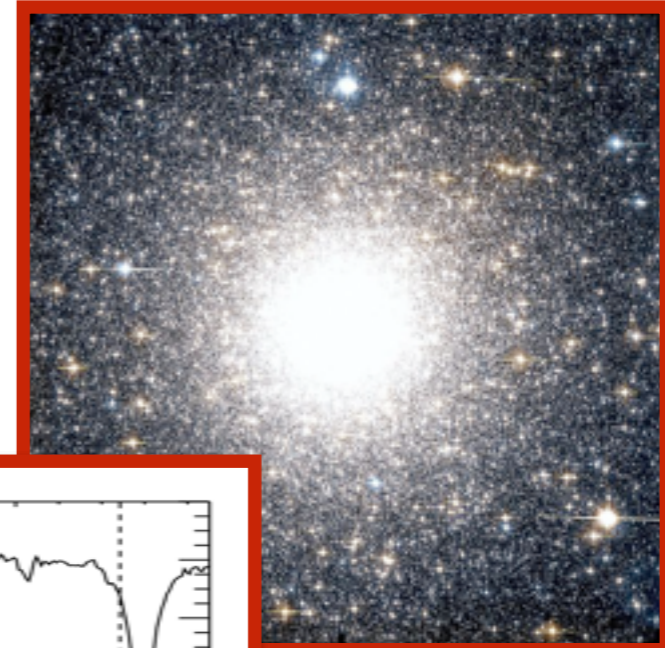
## 3. Simulations

## 4. Future



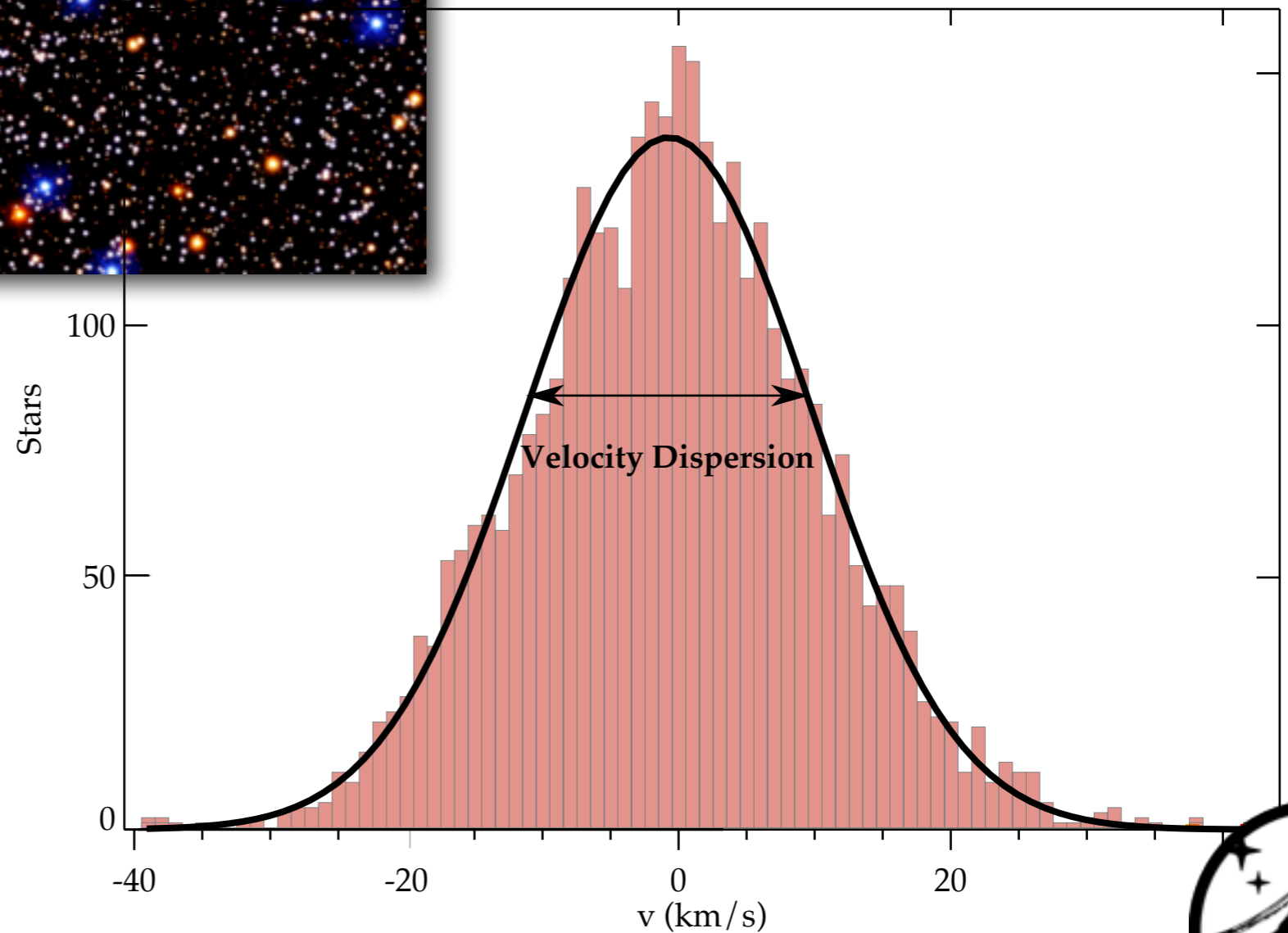
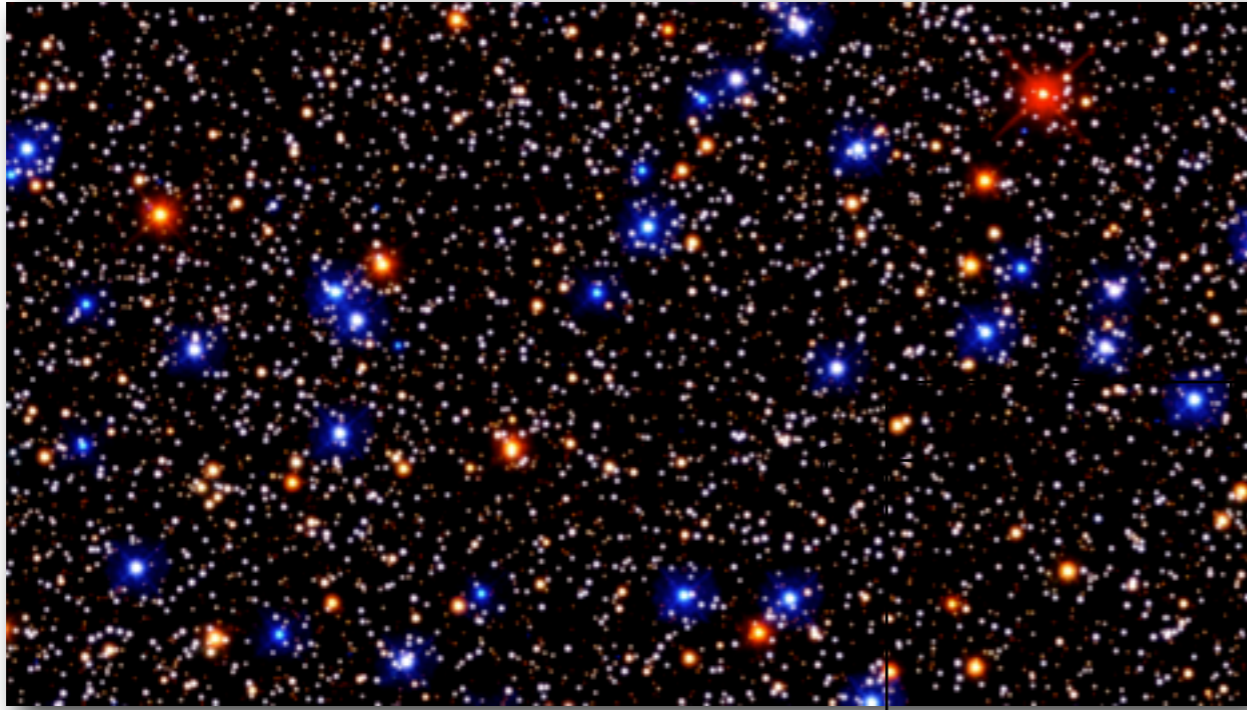
# Observations

1. Measure the **LIGHT**  
➔ **expected** velocities
2. Measure the **KINEMATICS**



- ➔ **true** velocities
3. COMBINE the data
4. COMPARE to **DYNAMICAL MODELS**  
➔ Missing dark mass?

# Excursion: Velocity Dispersion



# Excursion: Jeans Equations

Velocity Dispersion

Surface Brightness Profile

Potential+BH

$$\frac{d(\nu \overline{v_r^2})}{dr} + \frac{2\beta \nu \overline{v_r^2}}{r} = -\nu \frac{d\Phi}{dr}$$

Anisotropy  
( $\beta = 1 - \overline{v_\theta^2} / \overline{v_r^2}$ )

SURFACE BRIGHTNESS  
PROFILE

LIGHT



VELOCITY DISPERSION  
PROFILE

KINEMATICS



# Observations - Photometry



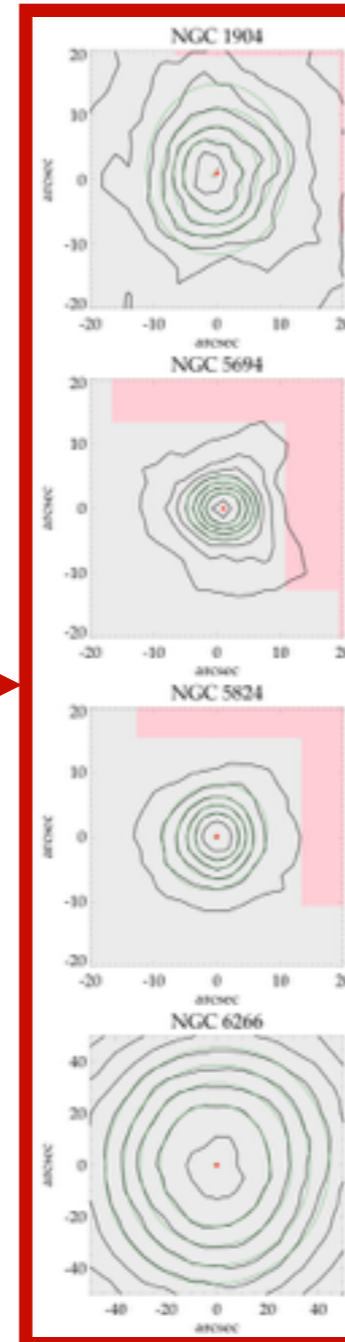
# Observations - Photometry

## 1. HST Image

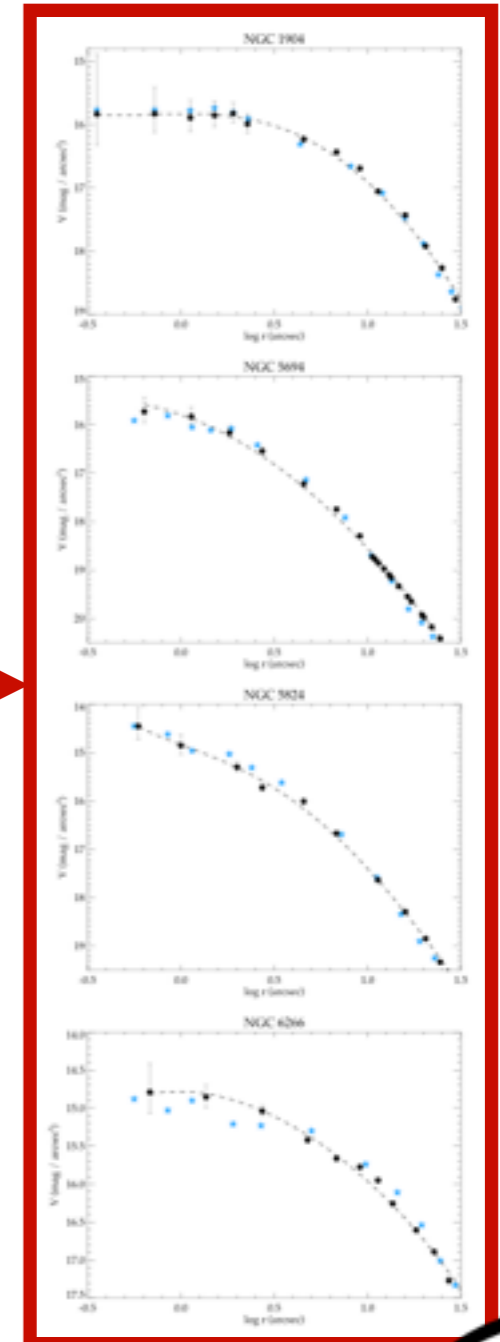


Lützgendorf et al., 2013a

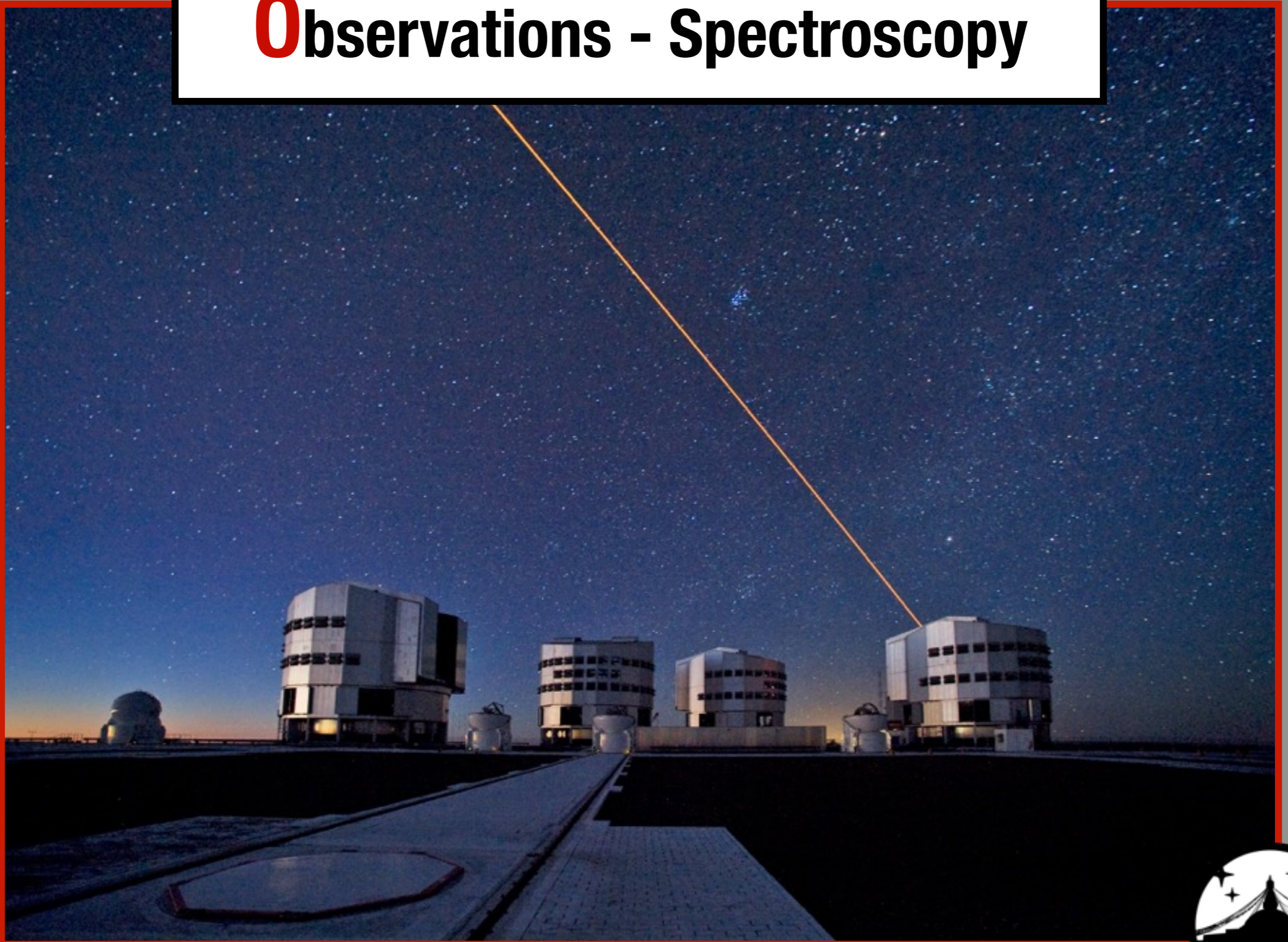
## 2. Center



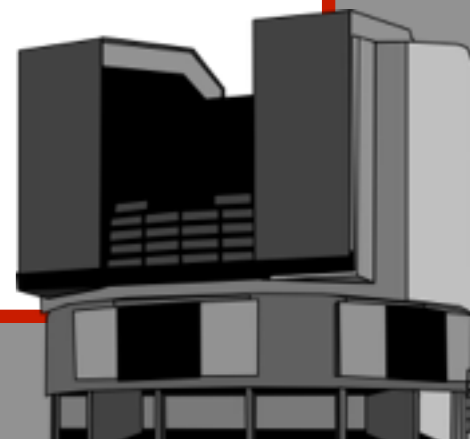
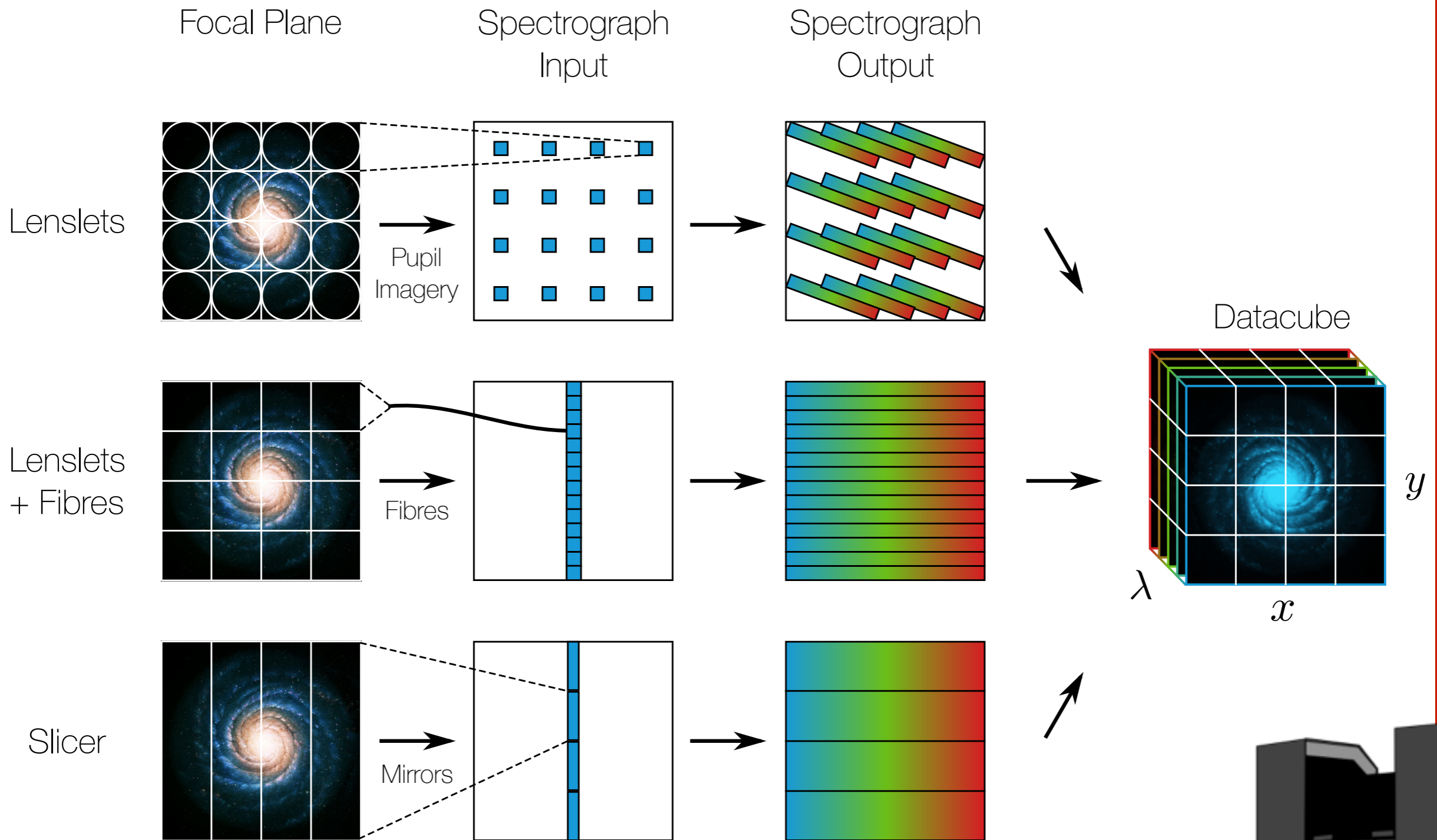
## 3. SB-Profile



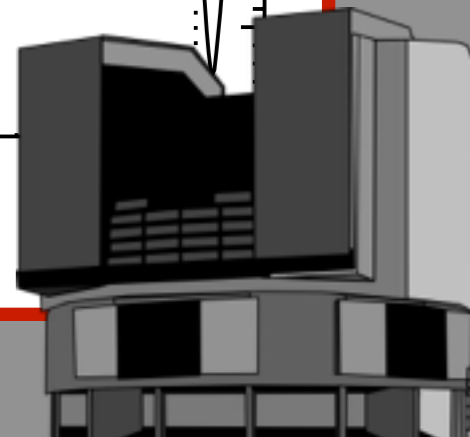
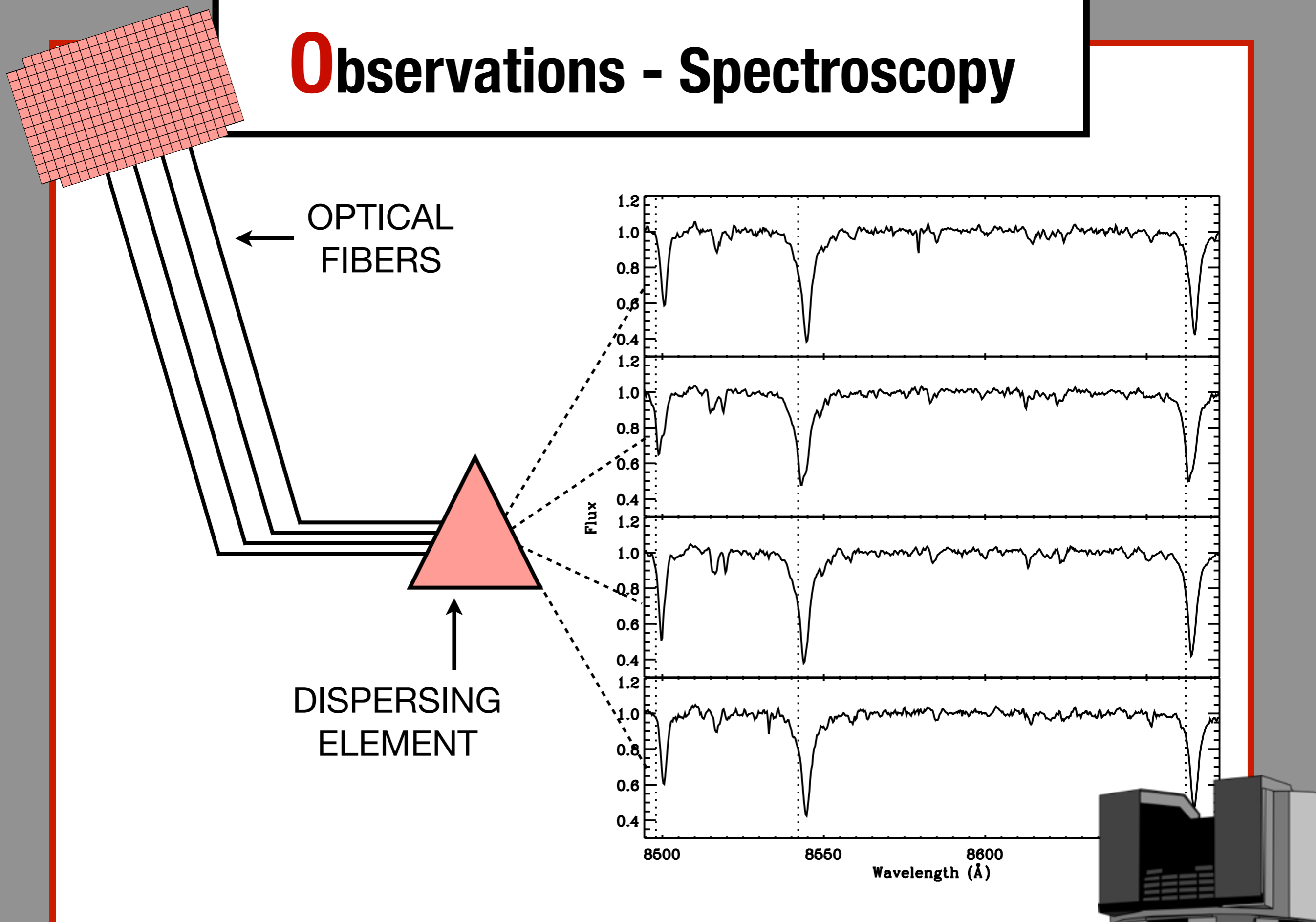
# Observations - Spectroscopy



# Observations - Spectroscopy



# Observations - Spectroscopy

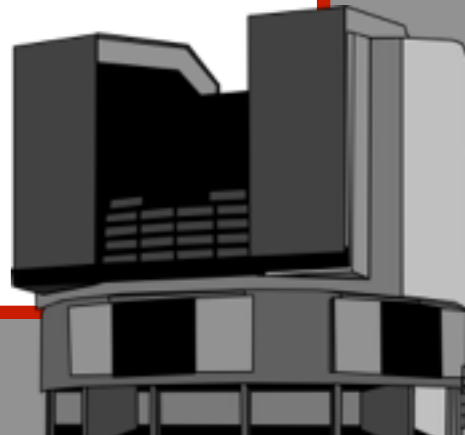
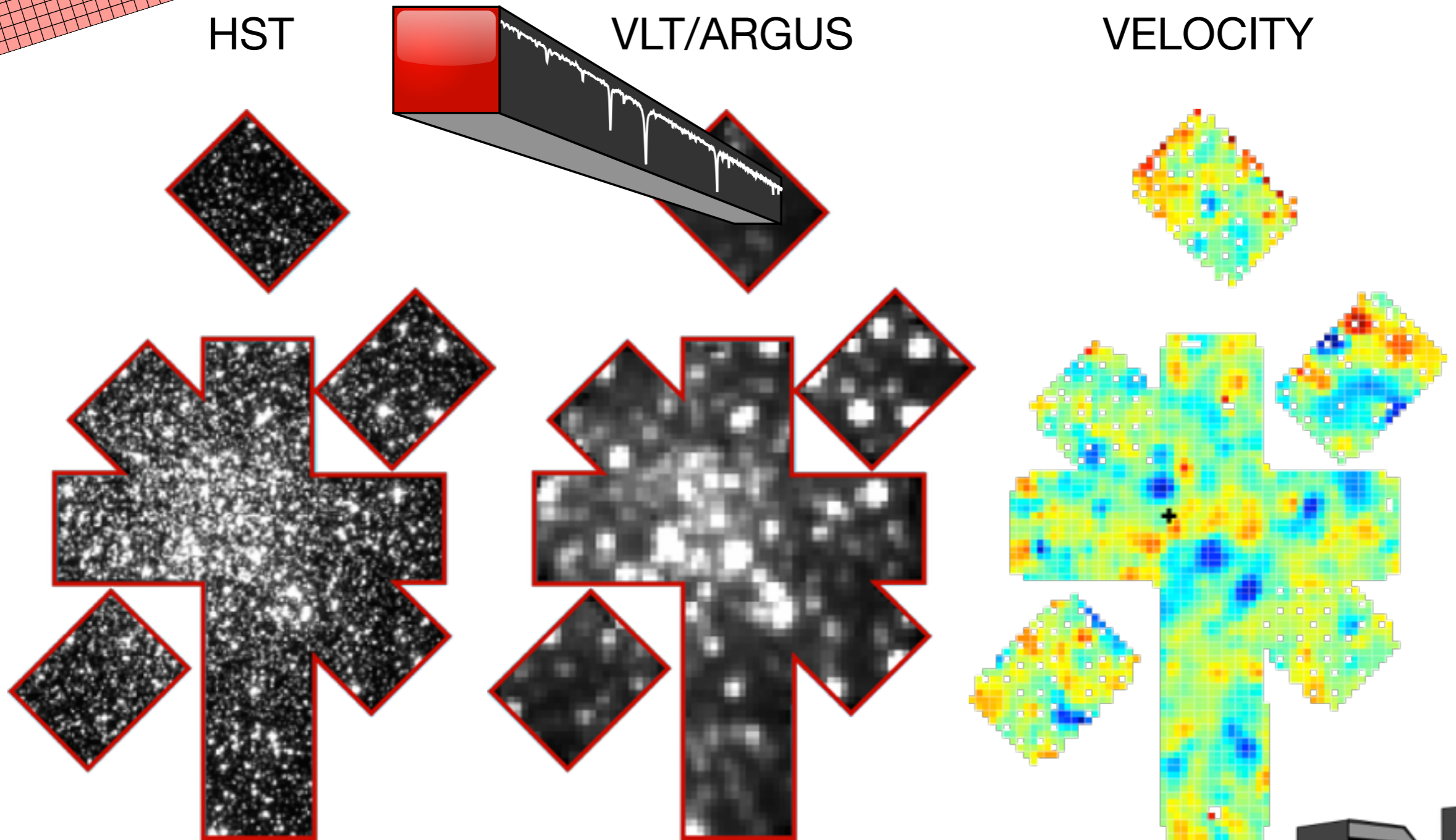


# Observations - Spectroscopy

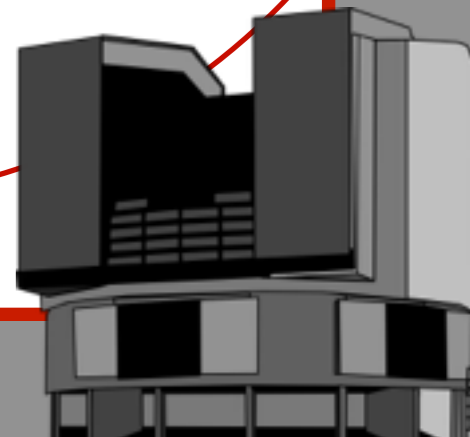
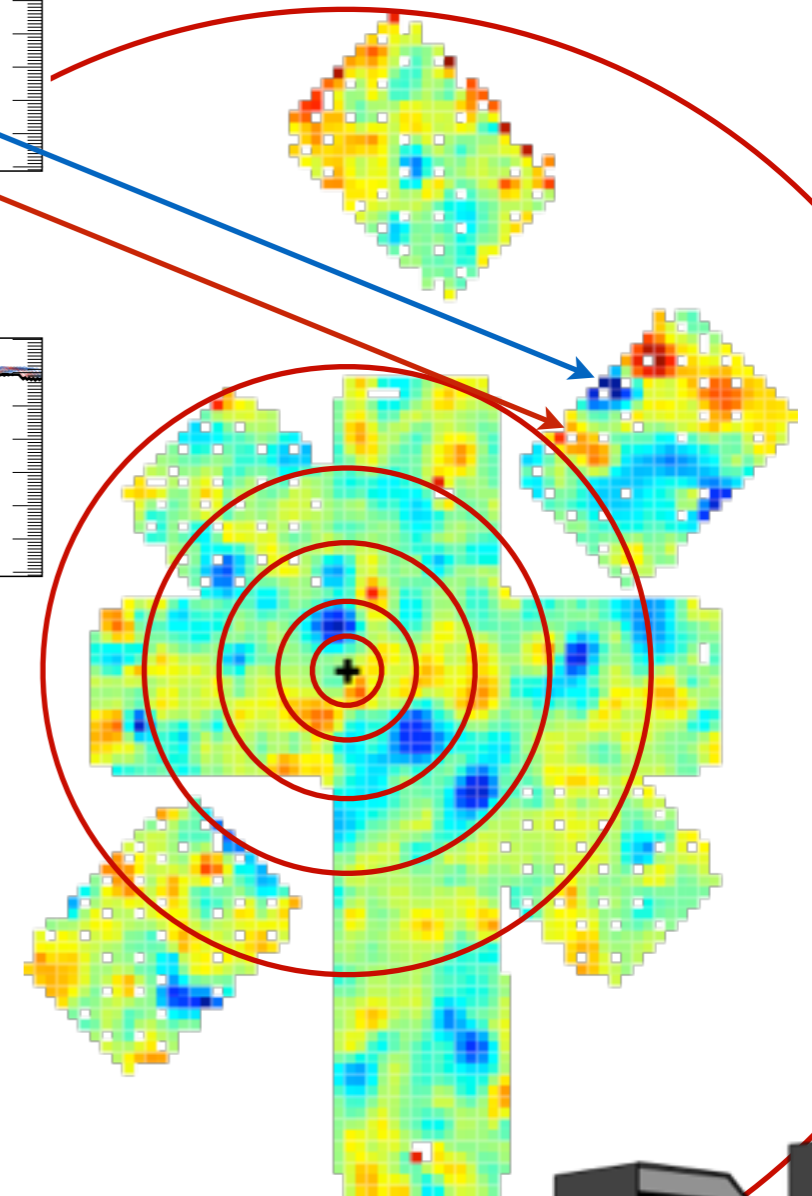
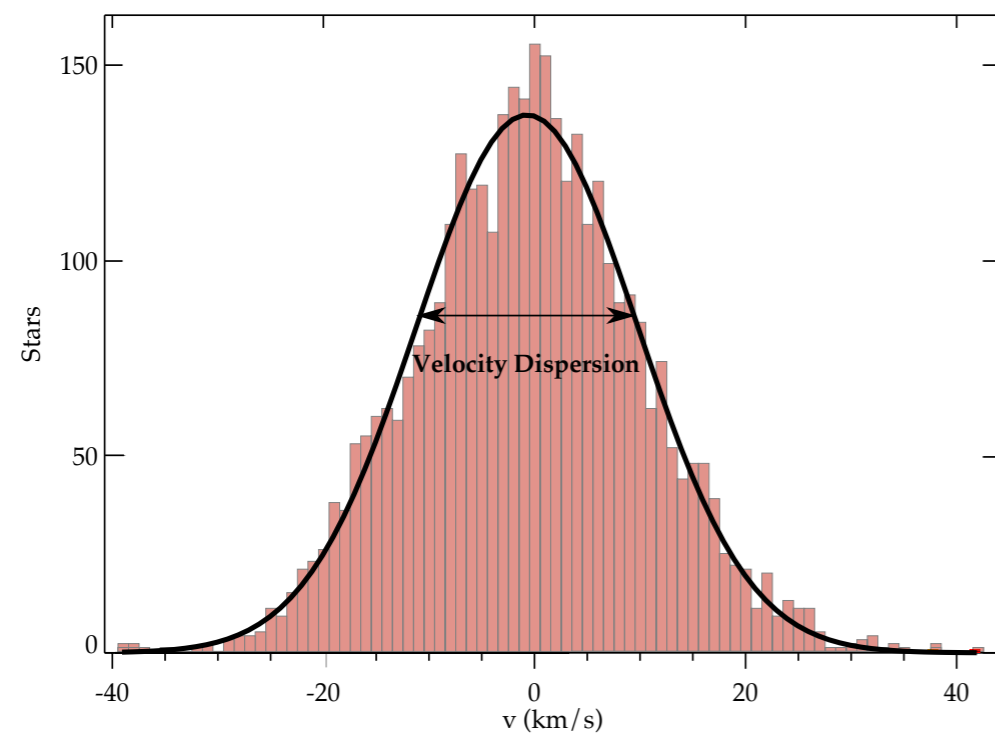
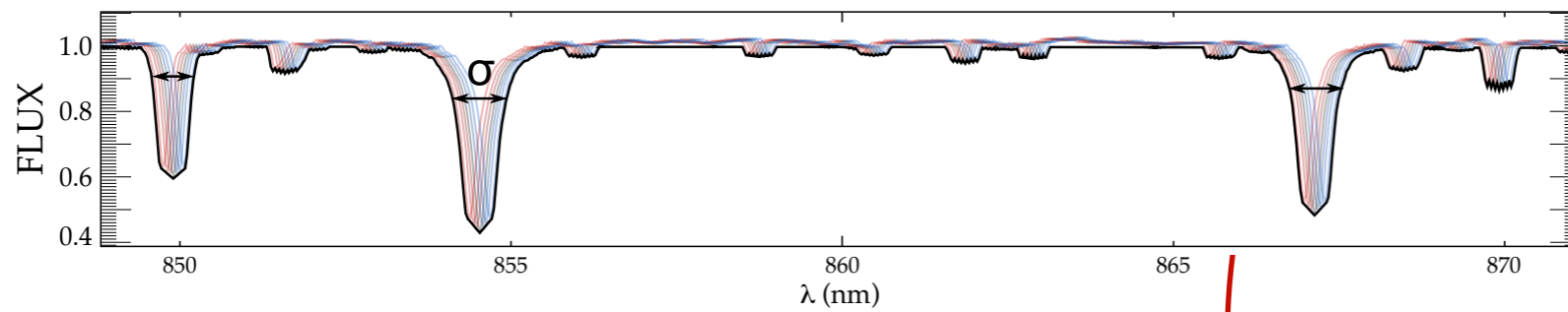
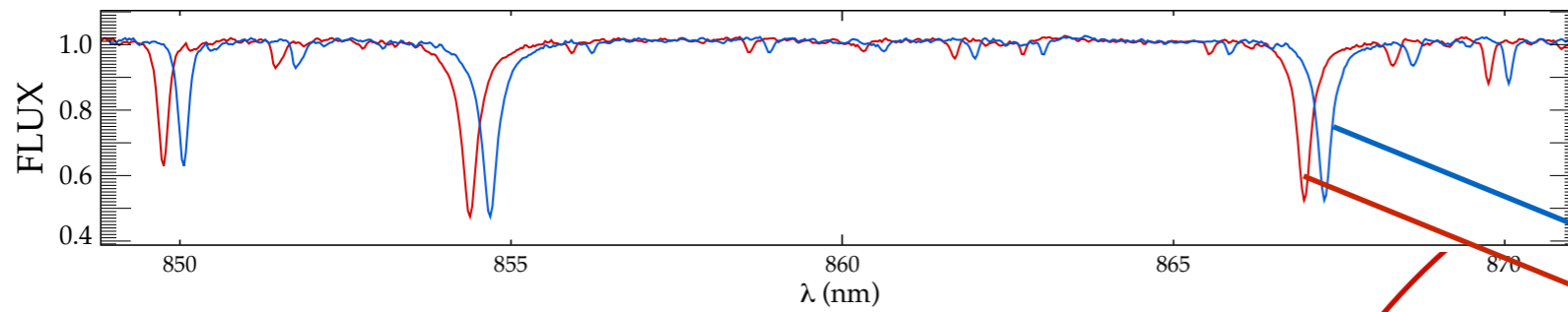
HST

VLT/ARGUS

VELOCITY

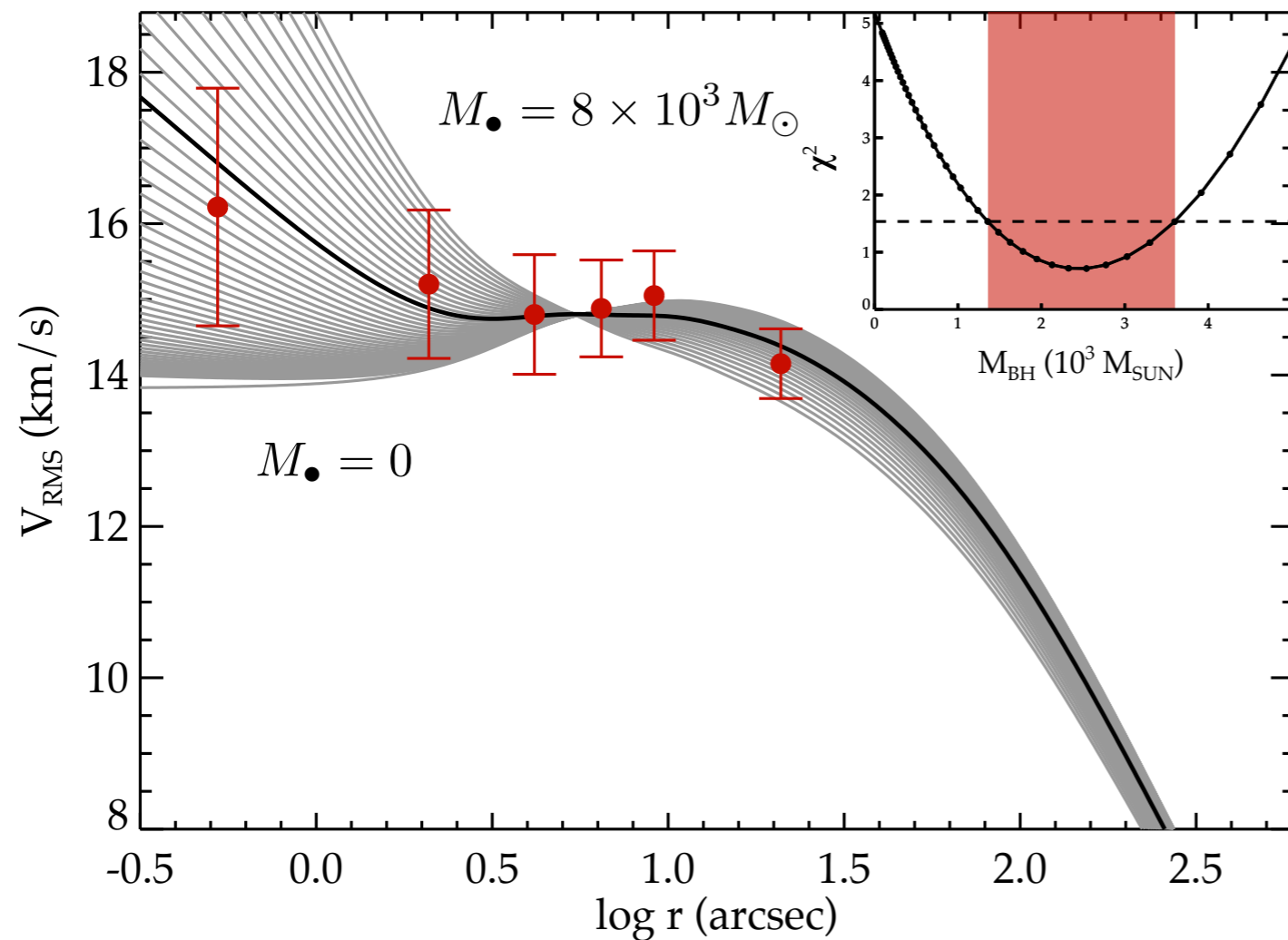


# Observations - Spectroscopy

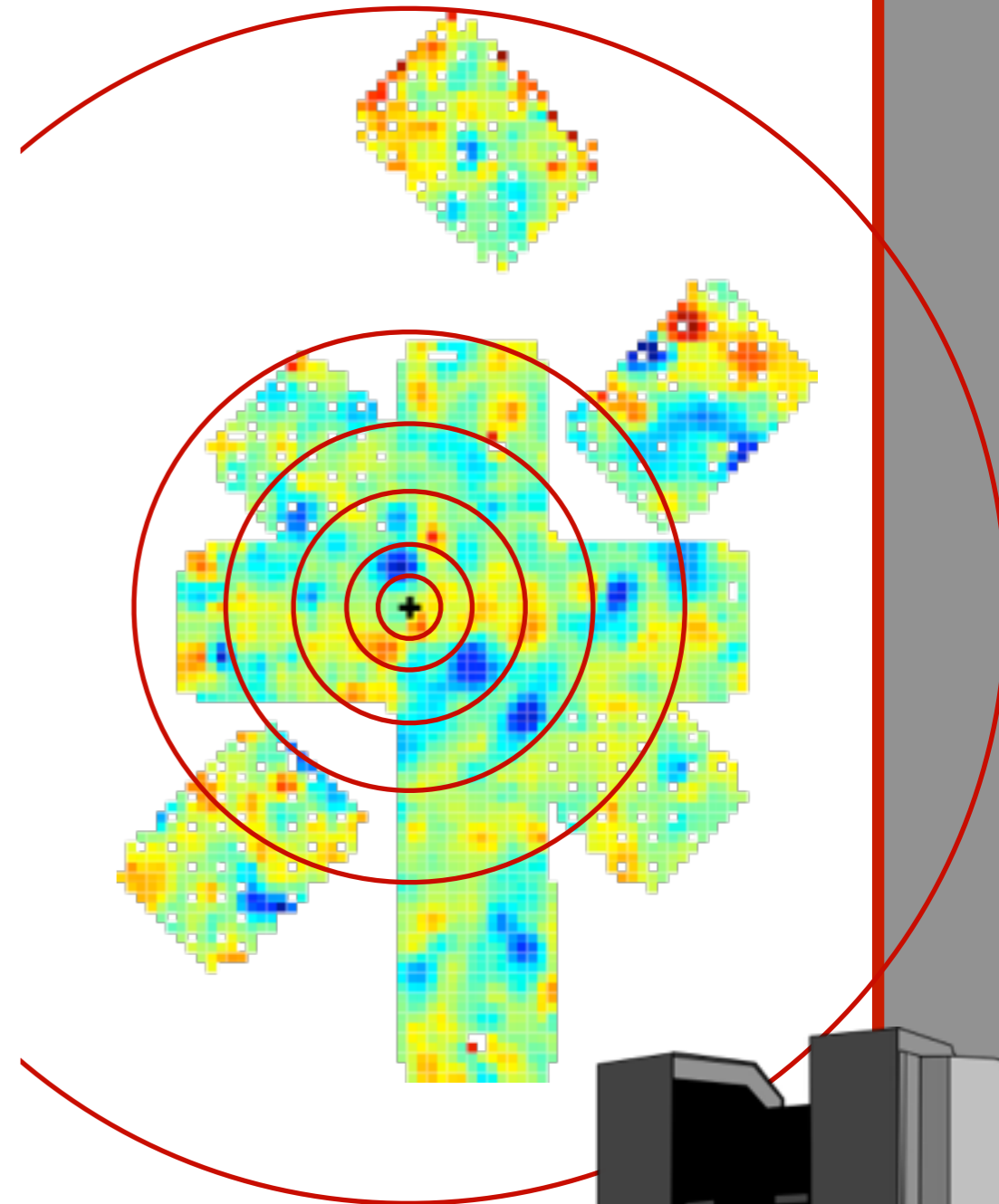


# Observations - Spectroscopy

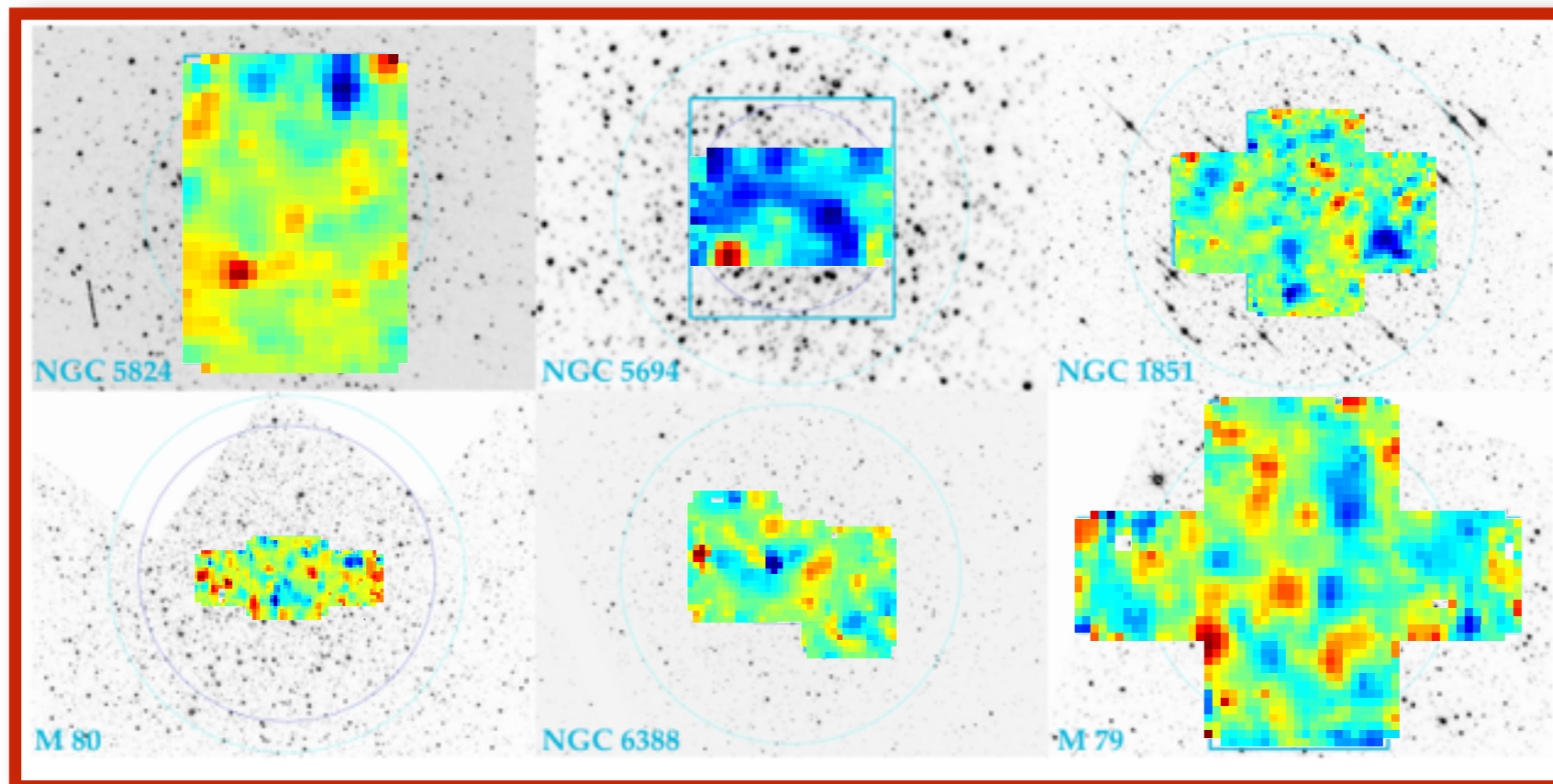
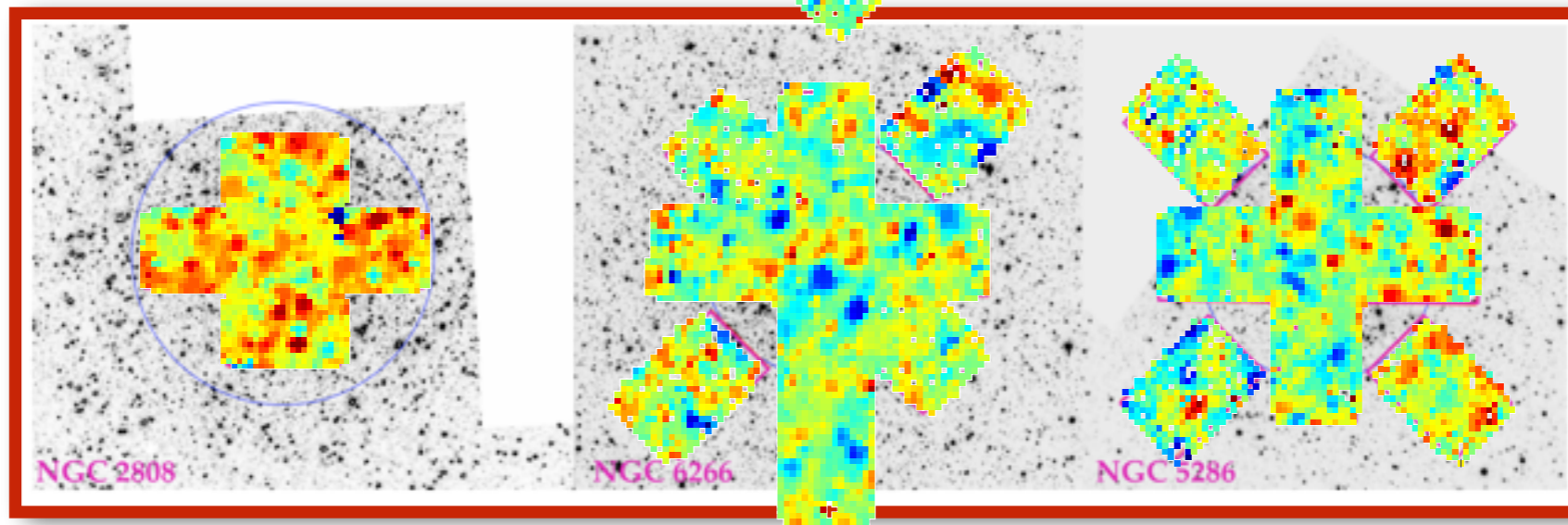
$$M_{\bullet} = (3 \pm 2) \times 10^3 M_{\odot}$$



NGC 6266, Lützendorf et al., 2013a

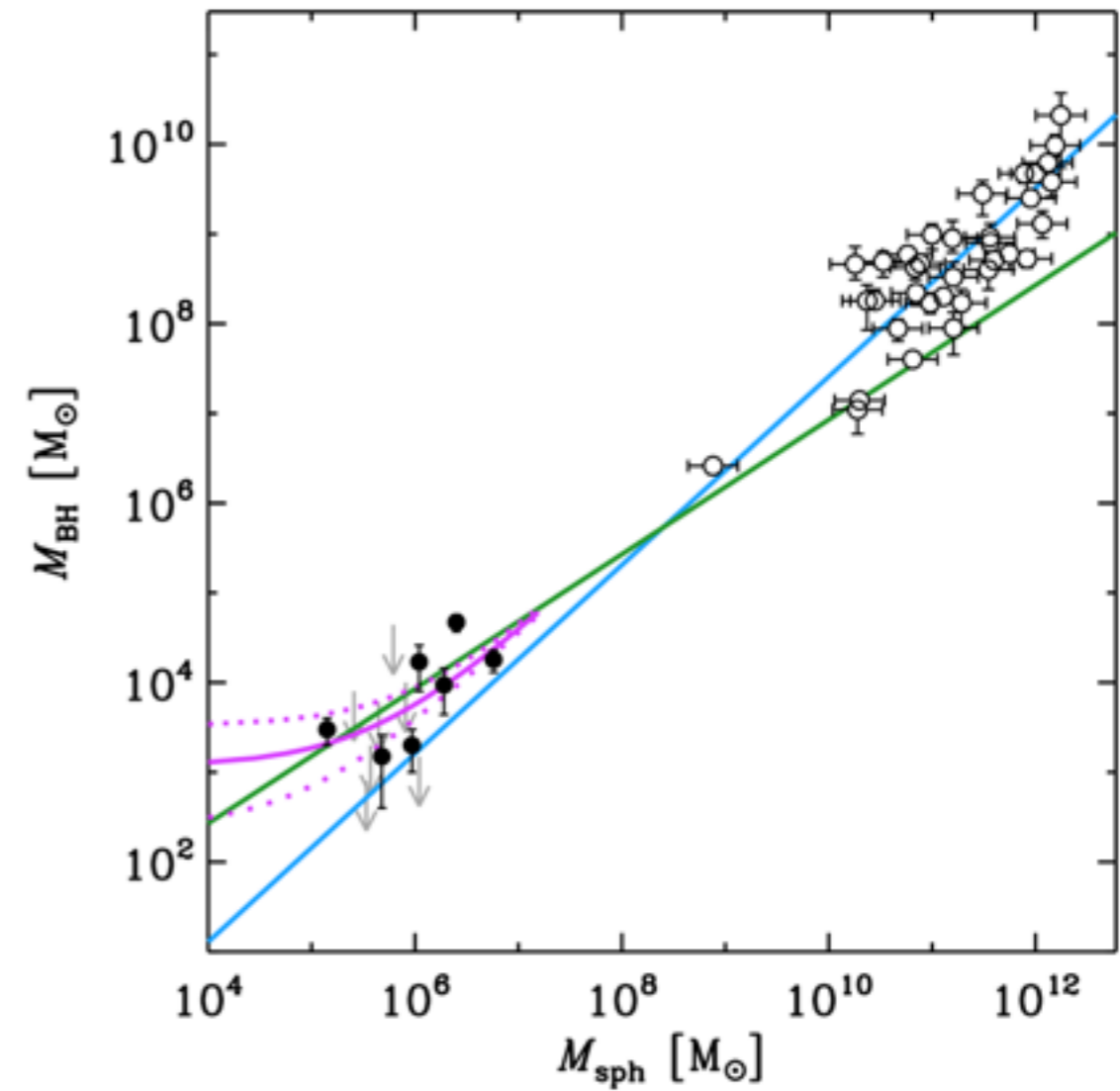
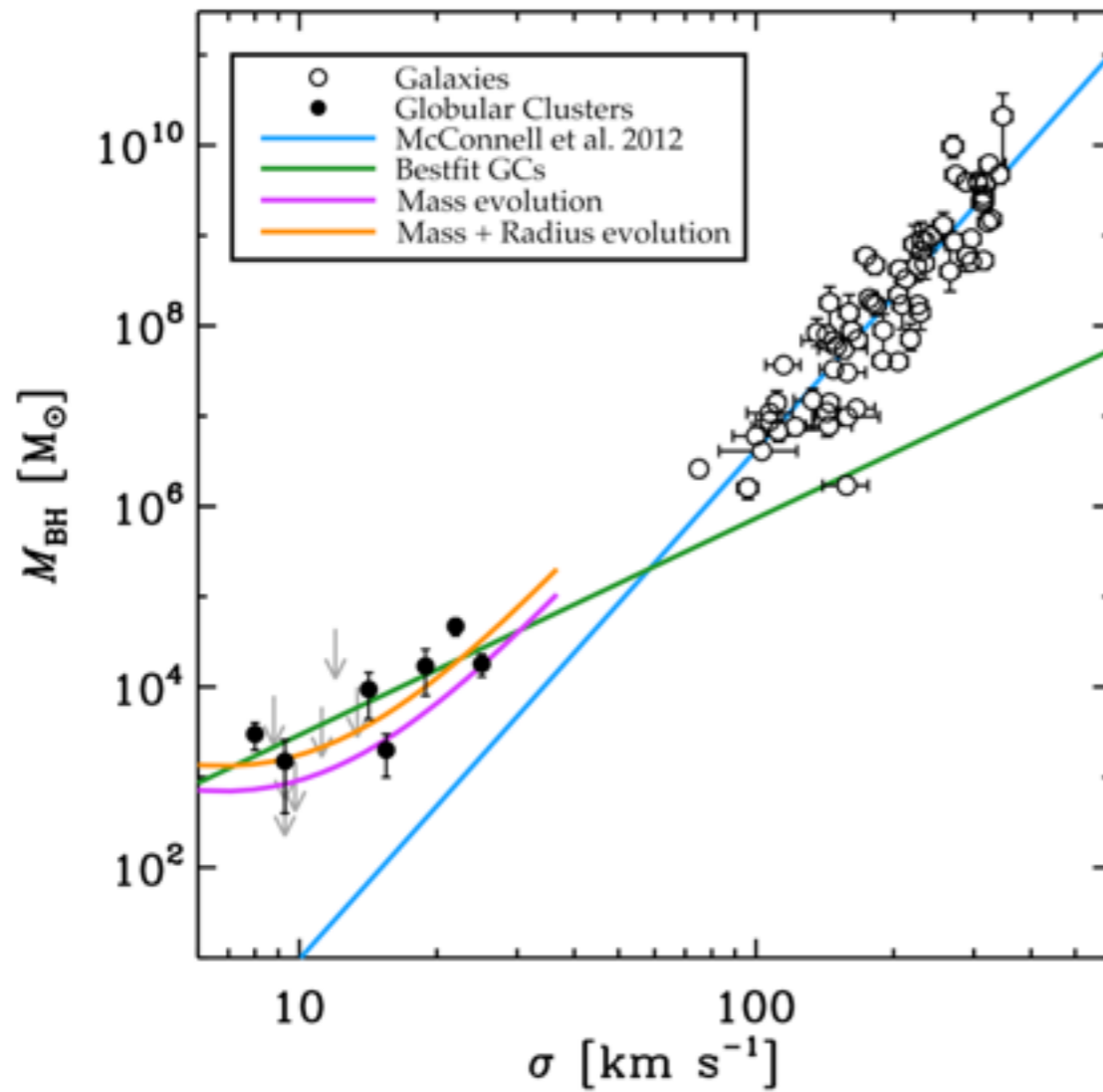


# Observations - Spectroscopy

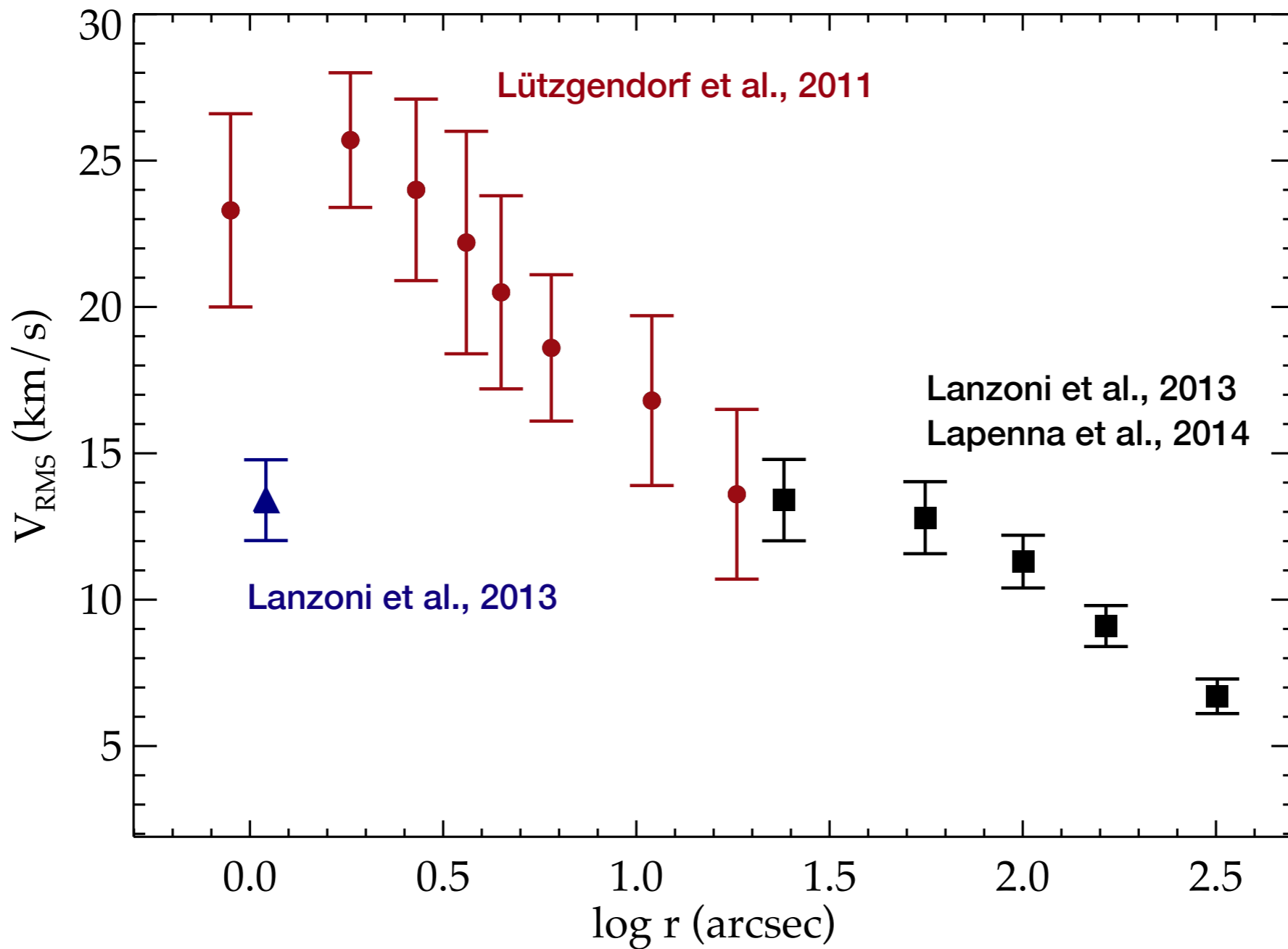


# Observations - Spectroscopy

Lützgendorf et al., 2013b  
Kruijssen & Lützgendorf, 2013



# Observations - Spectroscopy



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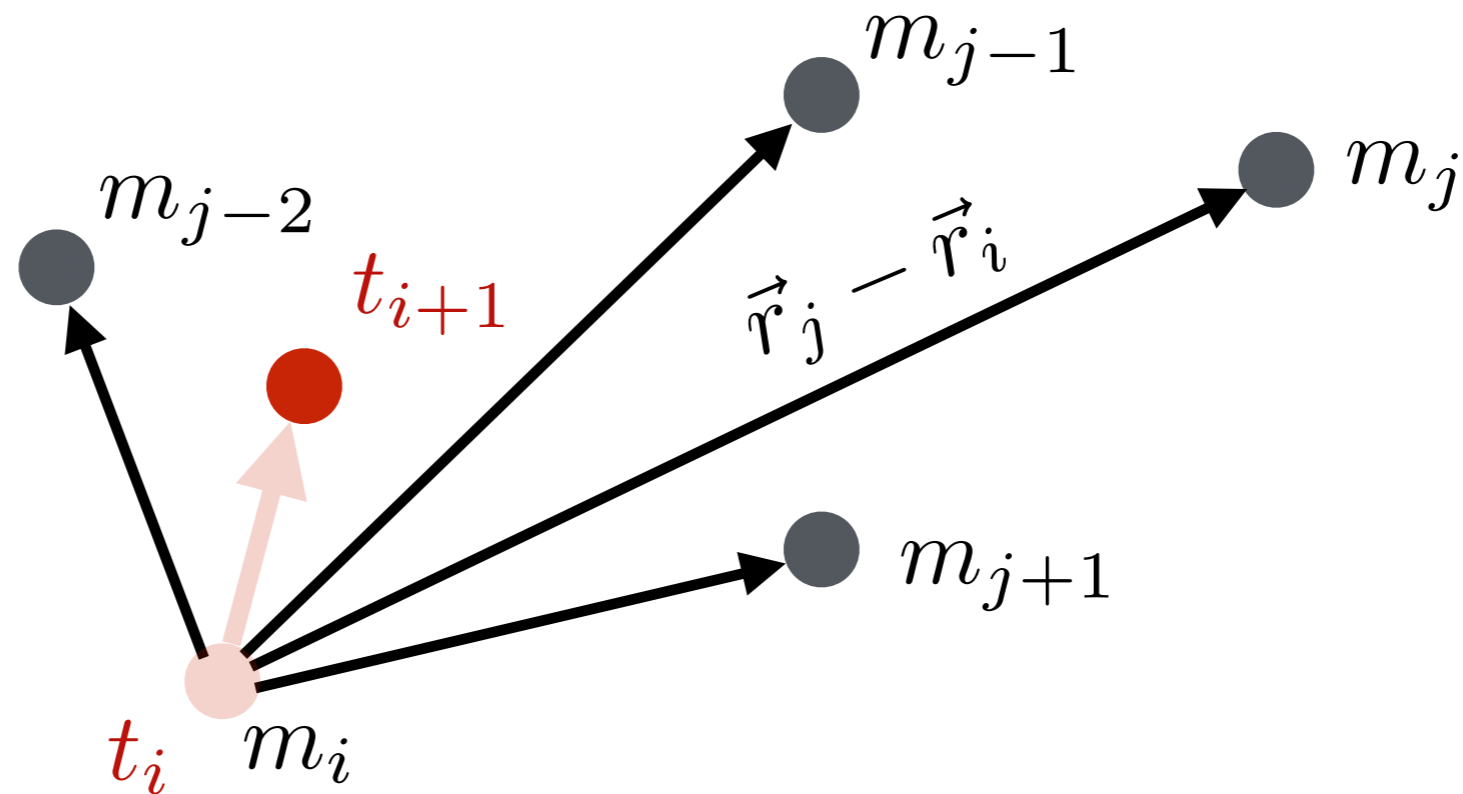
## 3. Simulations

## 4. Future



# N-BODY Simulations

$$\ddot{\vec{r}}_i = -G \sum_{j=1, j \neq i}^N m_j \frac{\vec{r}_j - \vec{r}_i}{|\vec{r}_j - \vec{r}_i|^3}$$



# N-BODY Simulations

$$\ddot{\vec{r}}_i = -G \sum_{j=1, j \neq i}^N m_j \frac{\vec{r}_j - \vec{r}_i}{|\vec{r}_j - \vec{r}_i|^3}$$

## LEAPFROG INTEGRATION



$$x_{i+1} = x_i + v_i \Delta t + \frac{1}{2} a_i \Delta t$$

$$v_{i+1} = v_i + \frac{1}{2} (a_i + a_{i+1}) \Delta t$$

# N-BODY Simulations



## THE ASTROPHYSICAL JOURNAL

AN INTERNATIONAL REVIEW OF SPECTROSCOPY AND  
ASTRONOMICAL PHYSICS

VOLUME 94

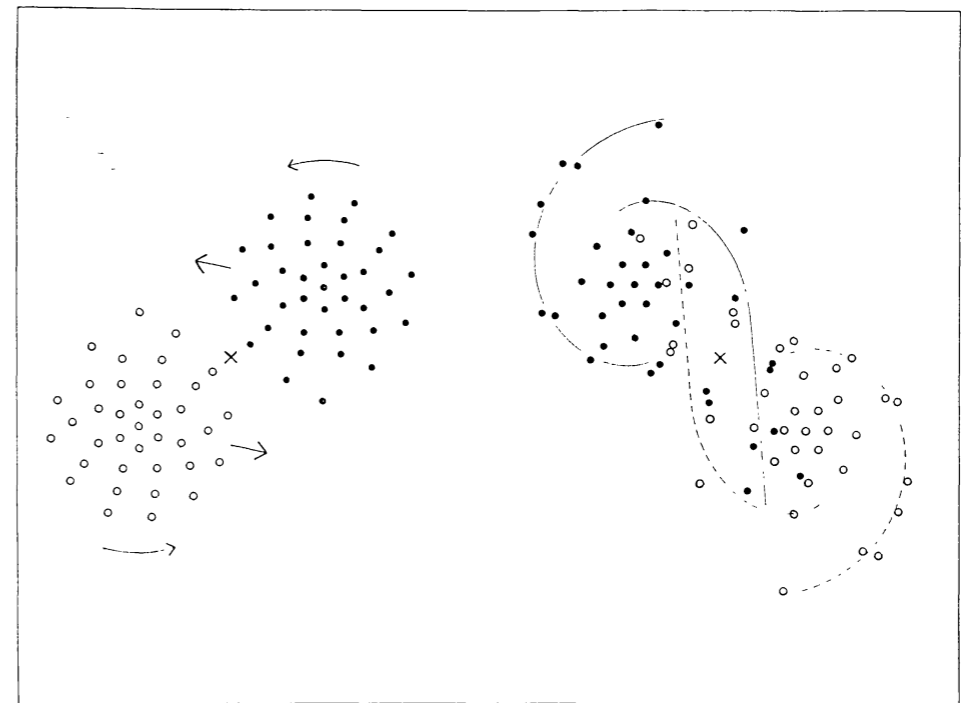
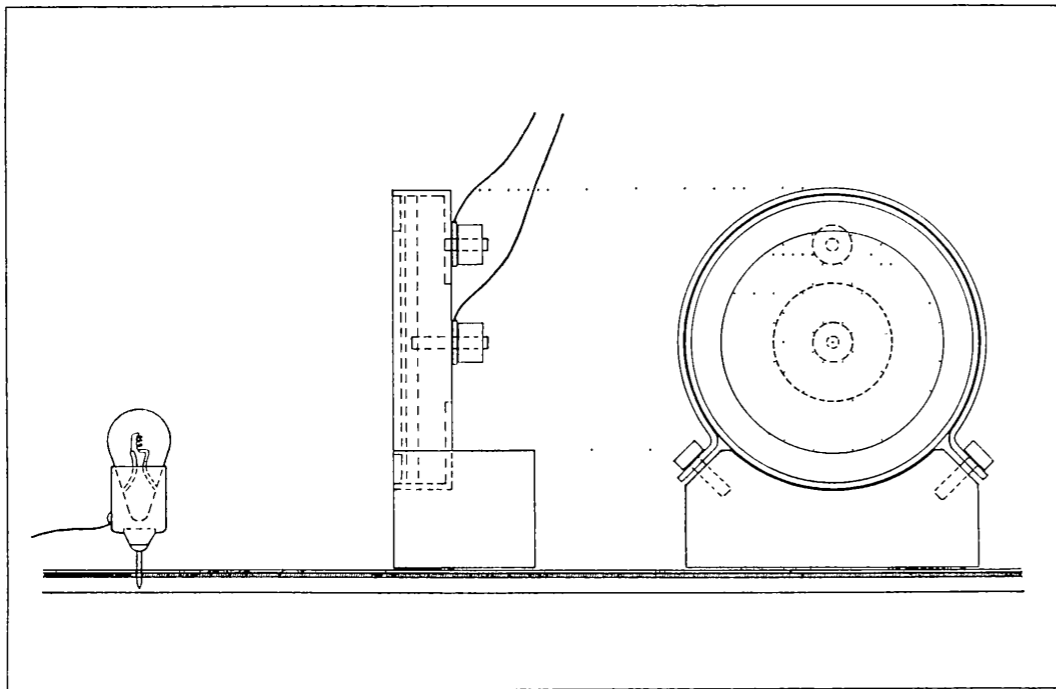
NOVEMBER 1941

NUMBER 3

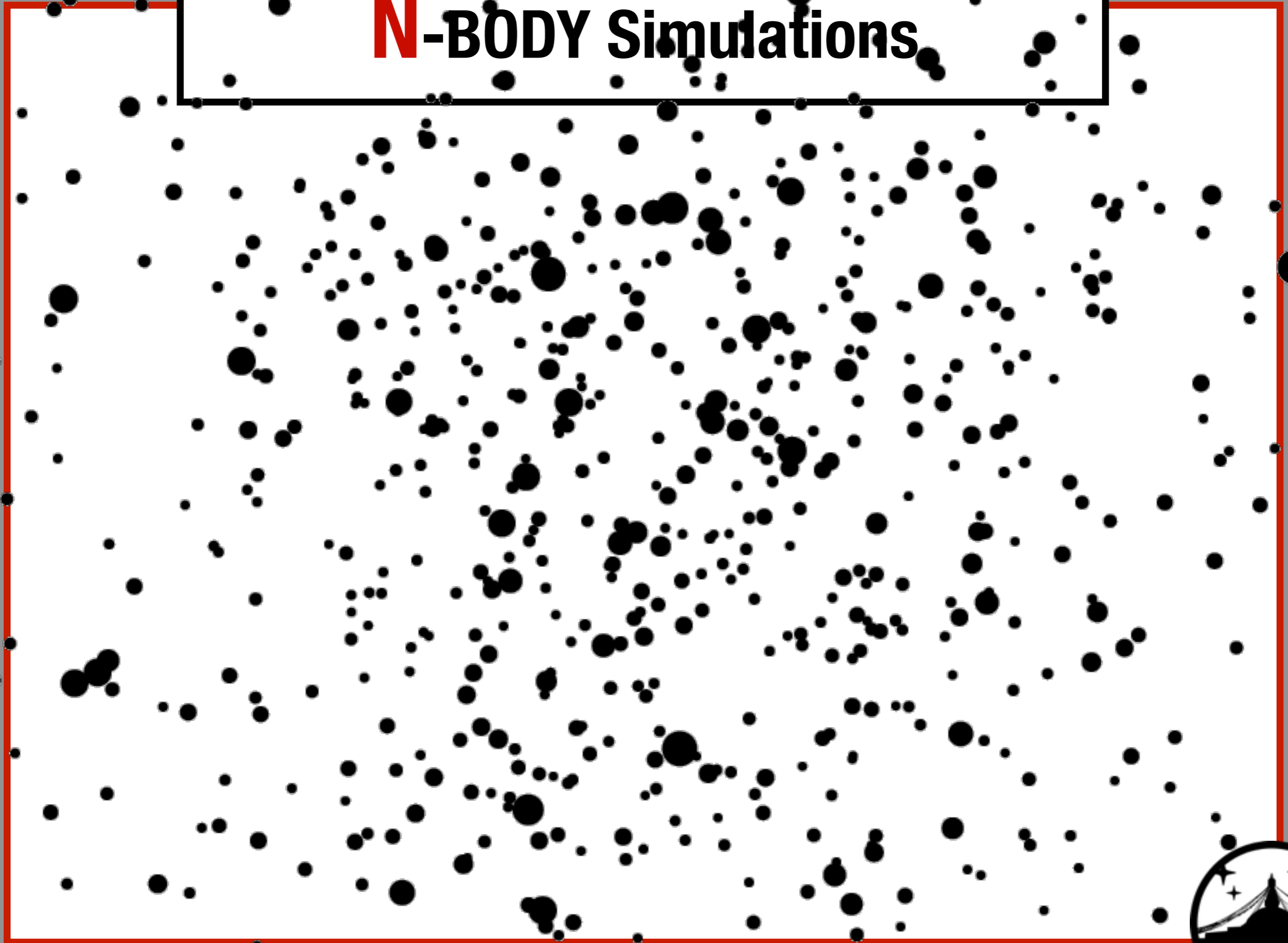
ON THE CLUSTERING TENDENCIES AMONG THE NEBULAE

II. A STUDY OF ENCOUNTERS BETWEEN LABORATORY MODELS OF  
STELLAR SYSTEMS BY A NEW INTEGRATION PROCEDURE

ERIK HOLMBERG

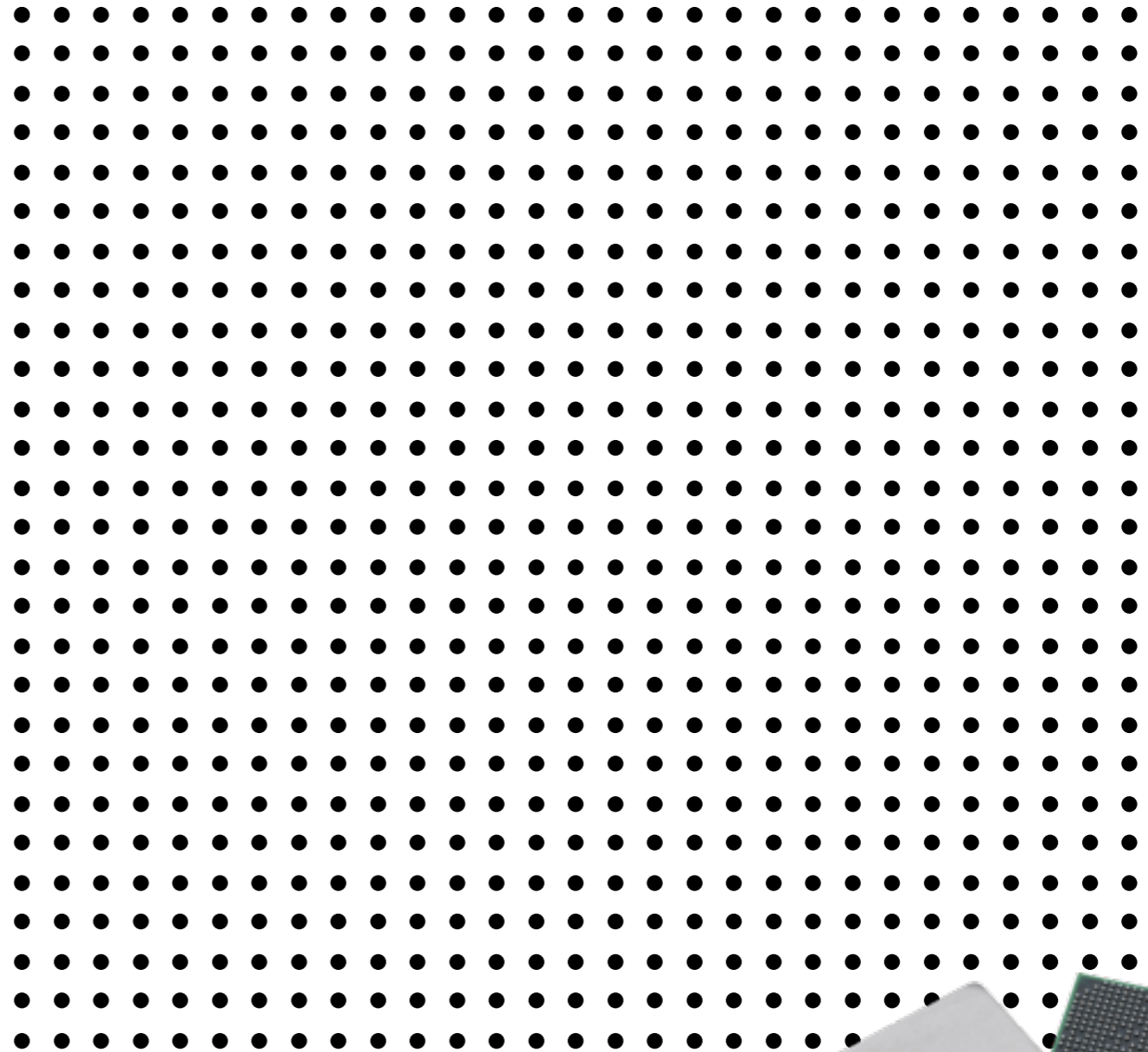


# N-BODY Simulations



# N-BODY Simulations

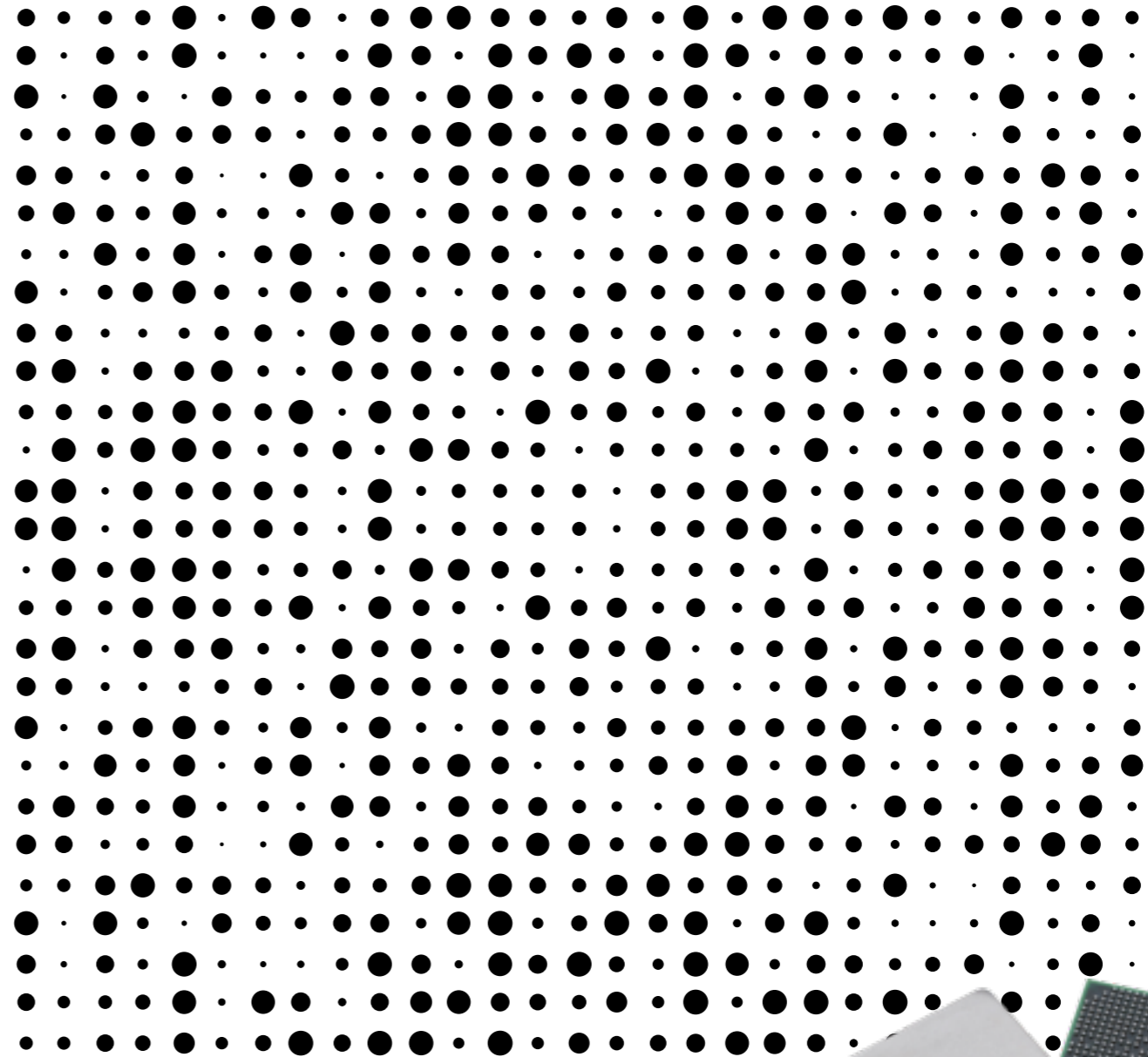
## 1. N Stars



# N-BODY Simulations

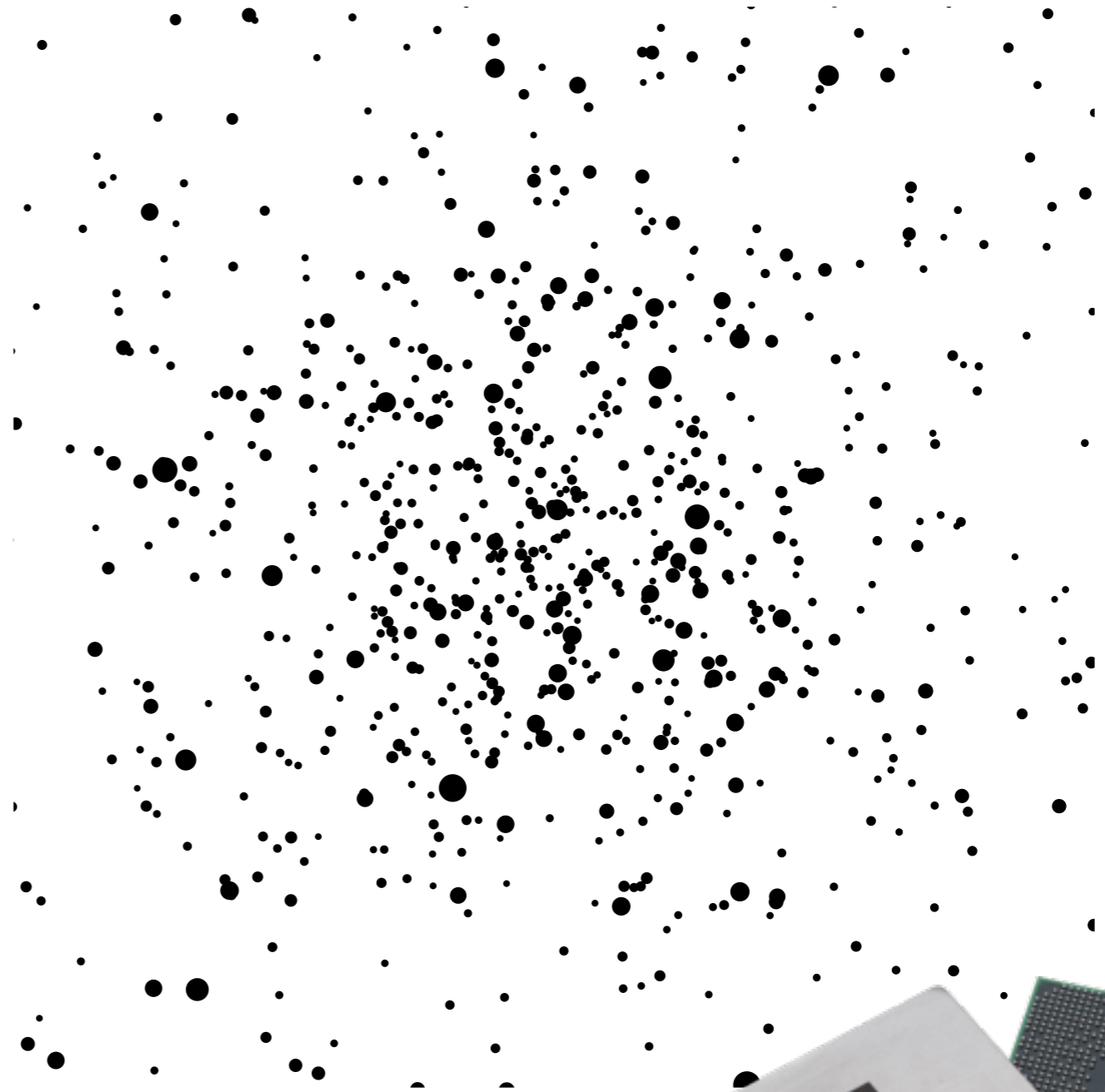
1. N Stars

2. Masses



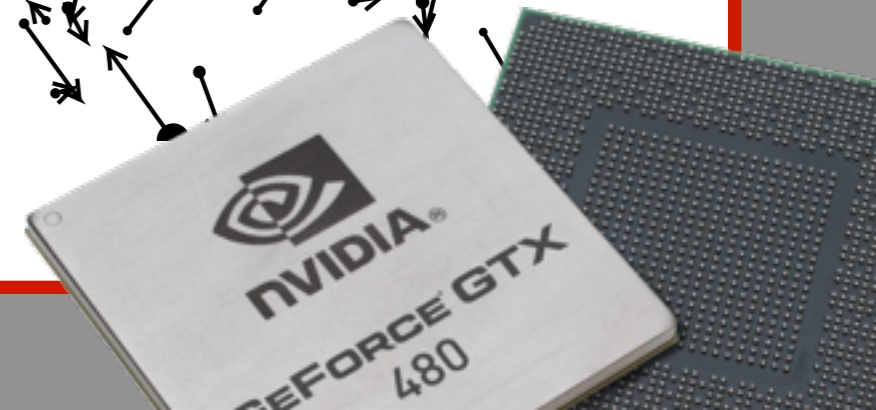
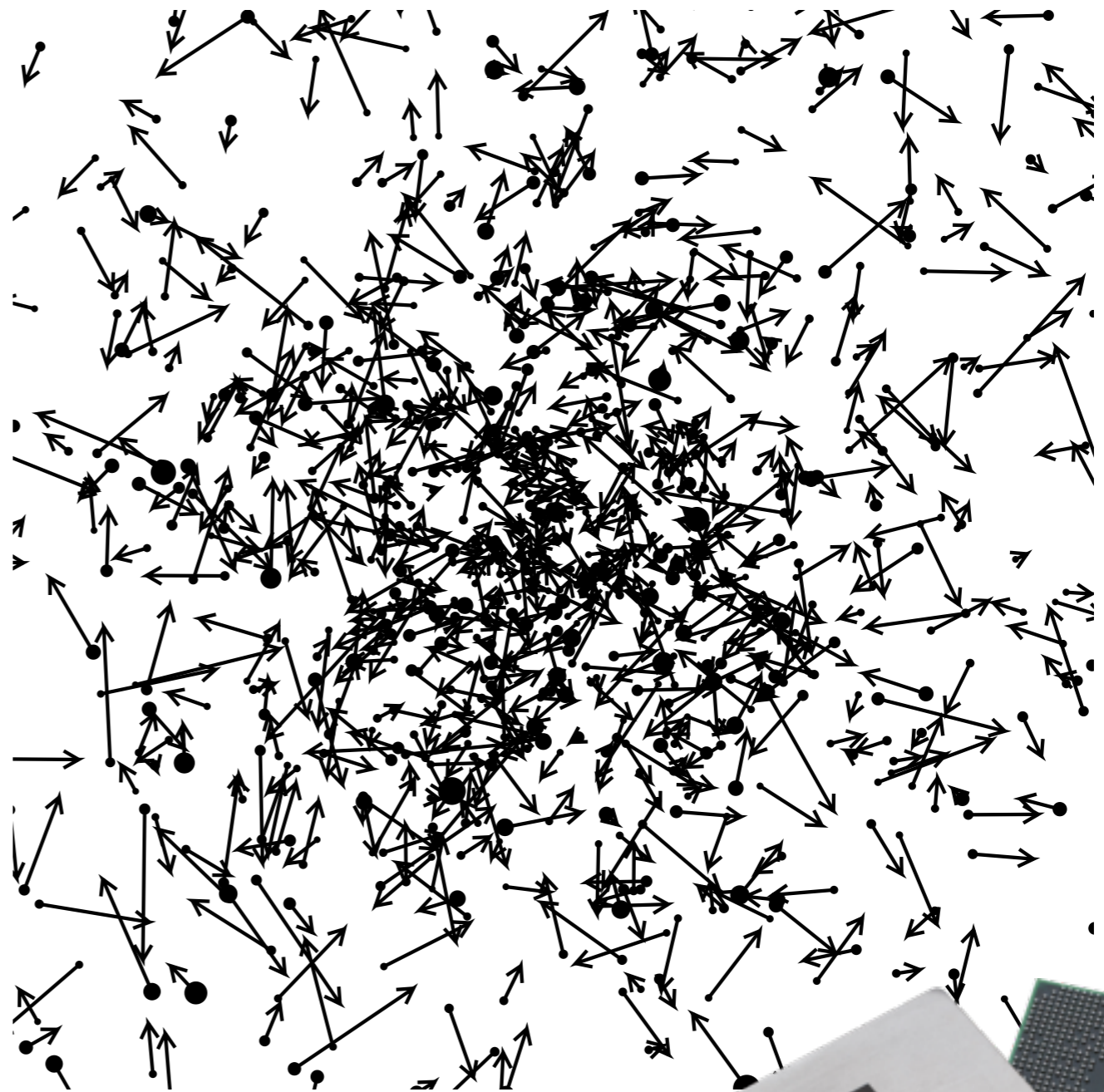
# N-BODY Simulations

1. N Stars
2. Masses
3. Distribution



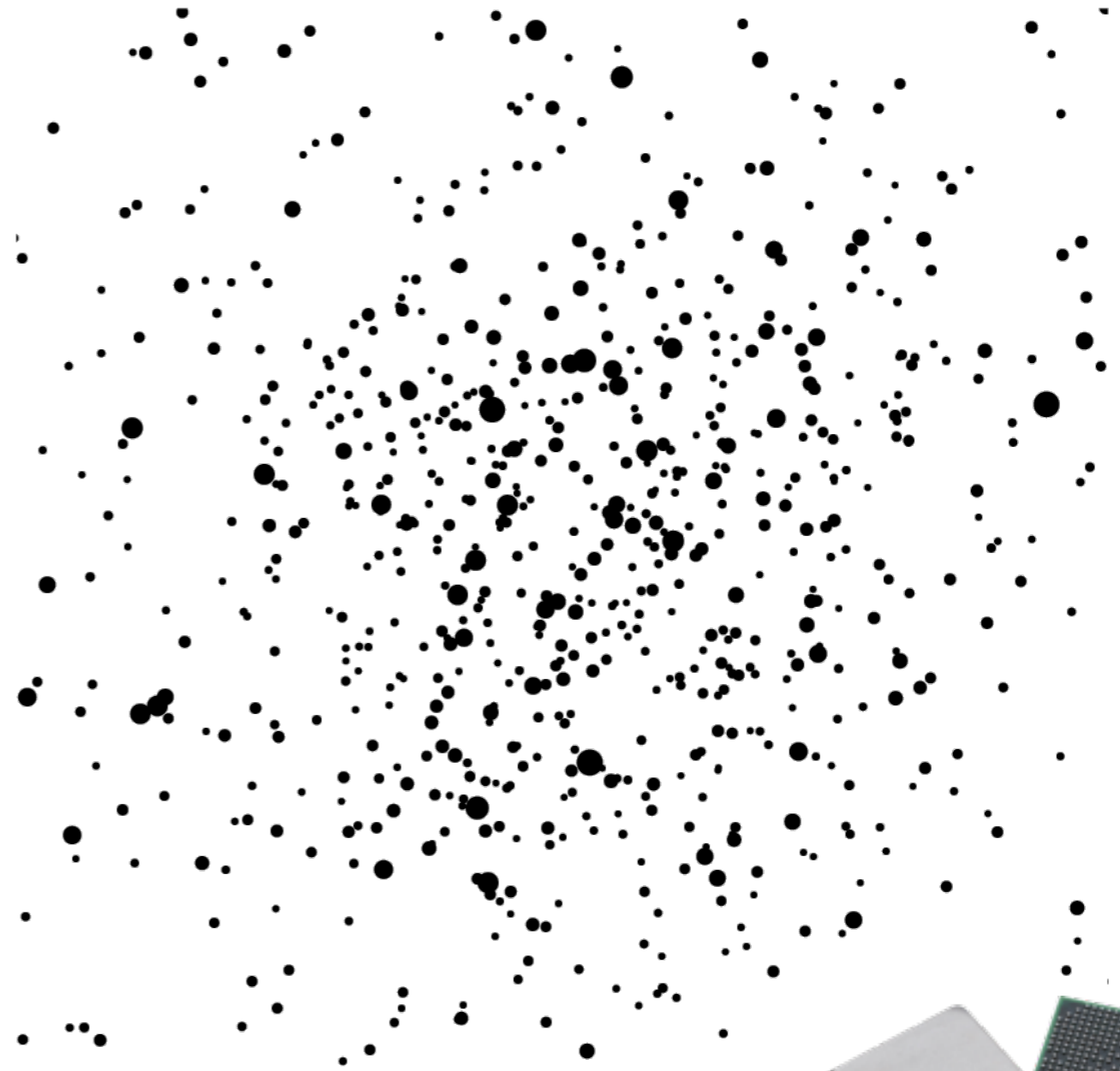
# N-BODY Simulations

1. N Stars
2. Masses
3. Distribution
4. Velocities



# N-BODY Simulations

1. N Stars
2. Masses
3. Distribution
4. Velocities
5. GO



# **N**-BODY Simulations

Applications?

**COMPARE** TO DATA

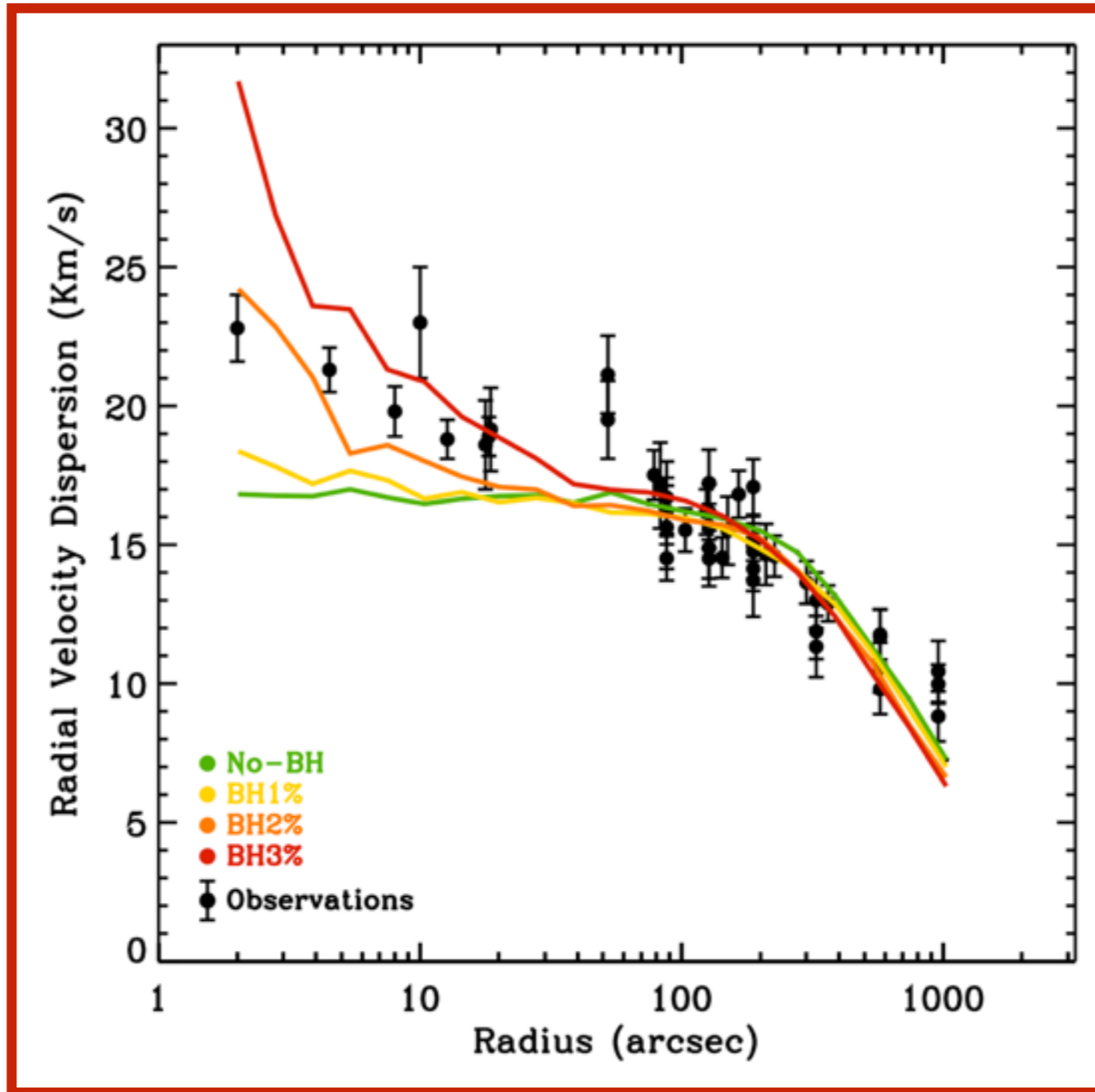
**SIMULATE** DATA

**FIND** NEW OBSERVABLES

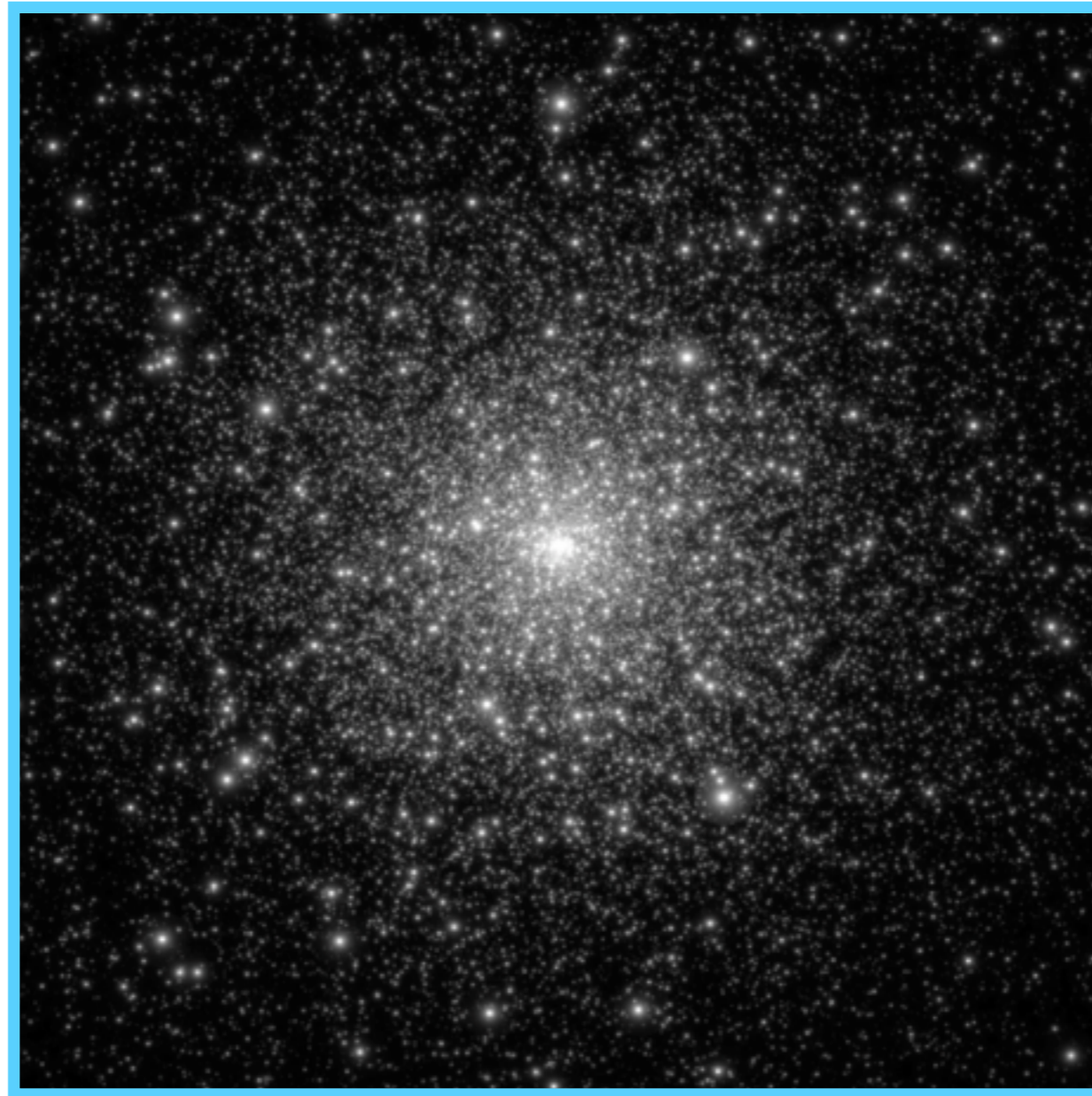


# N-BODY - COMPARE

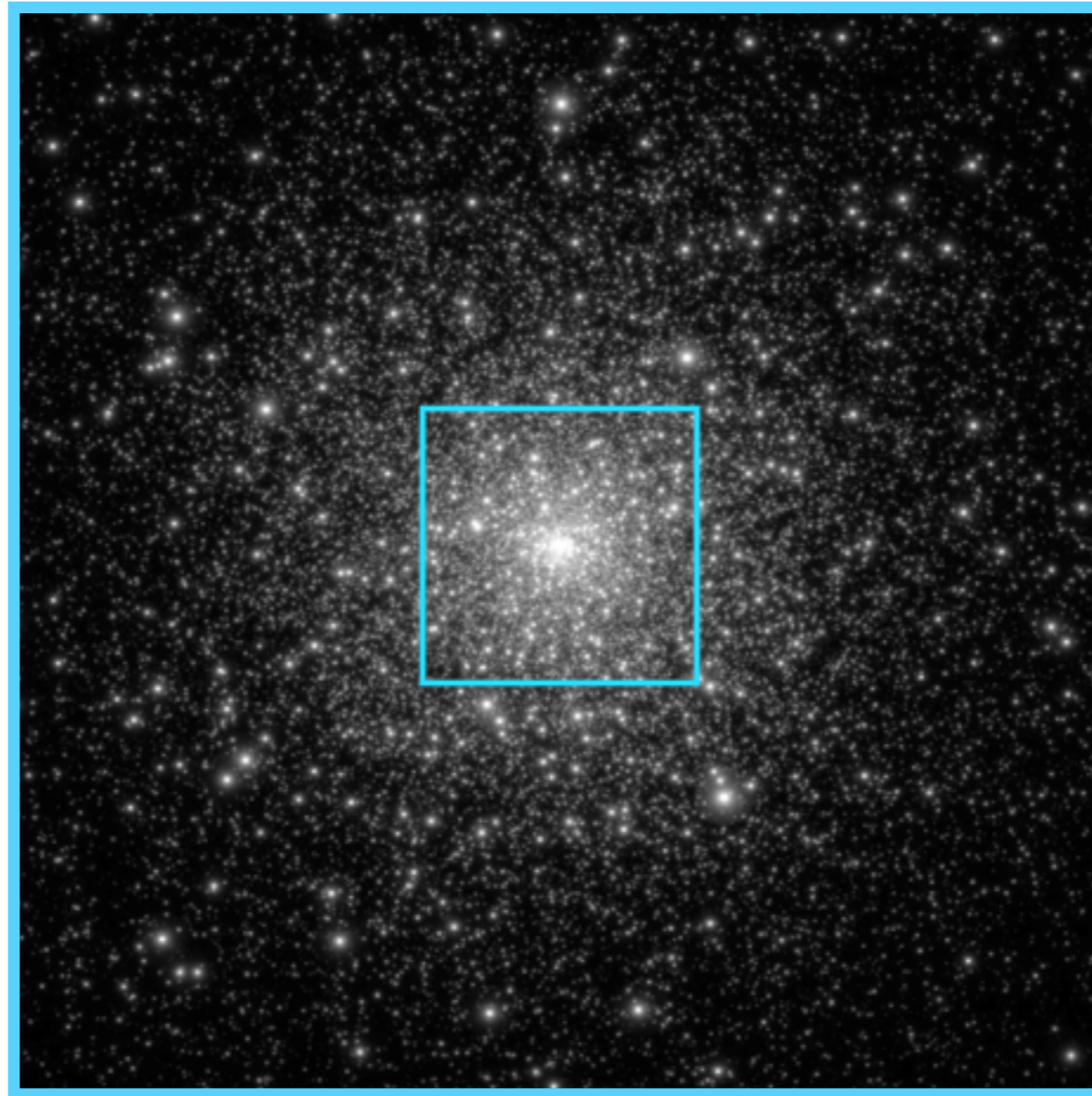
Jalali et al. 2012



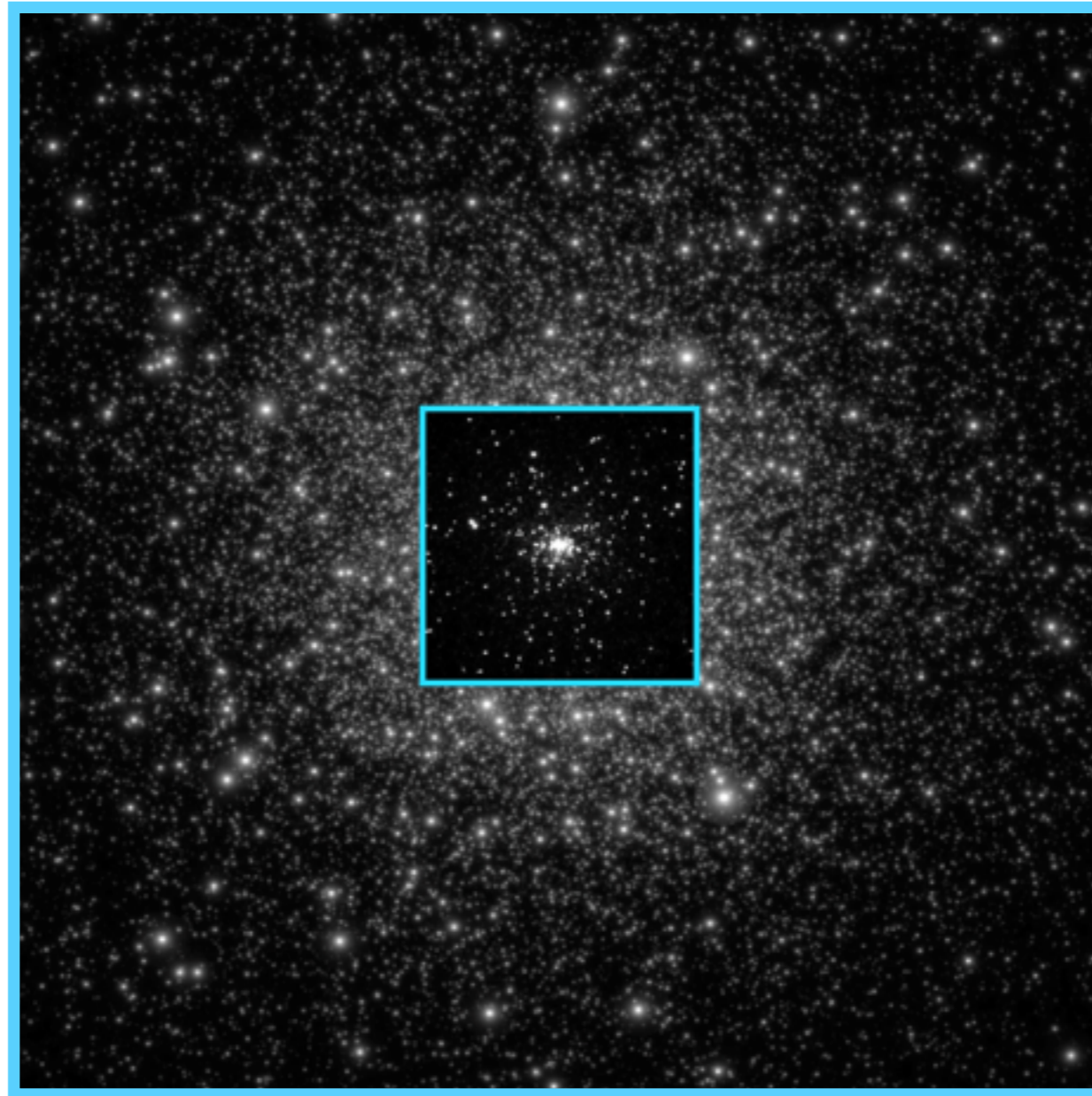
# N-BODY - SIMULATE



# N-BODY - SIMULATE



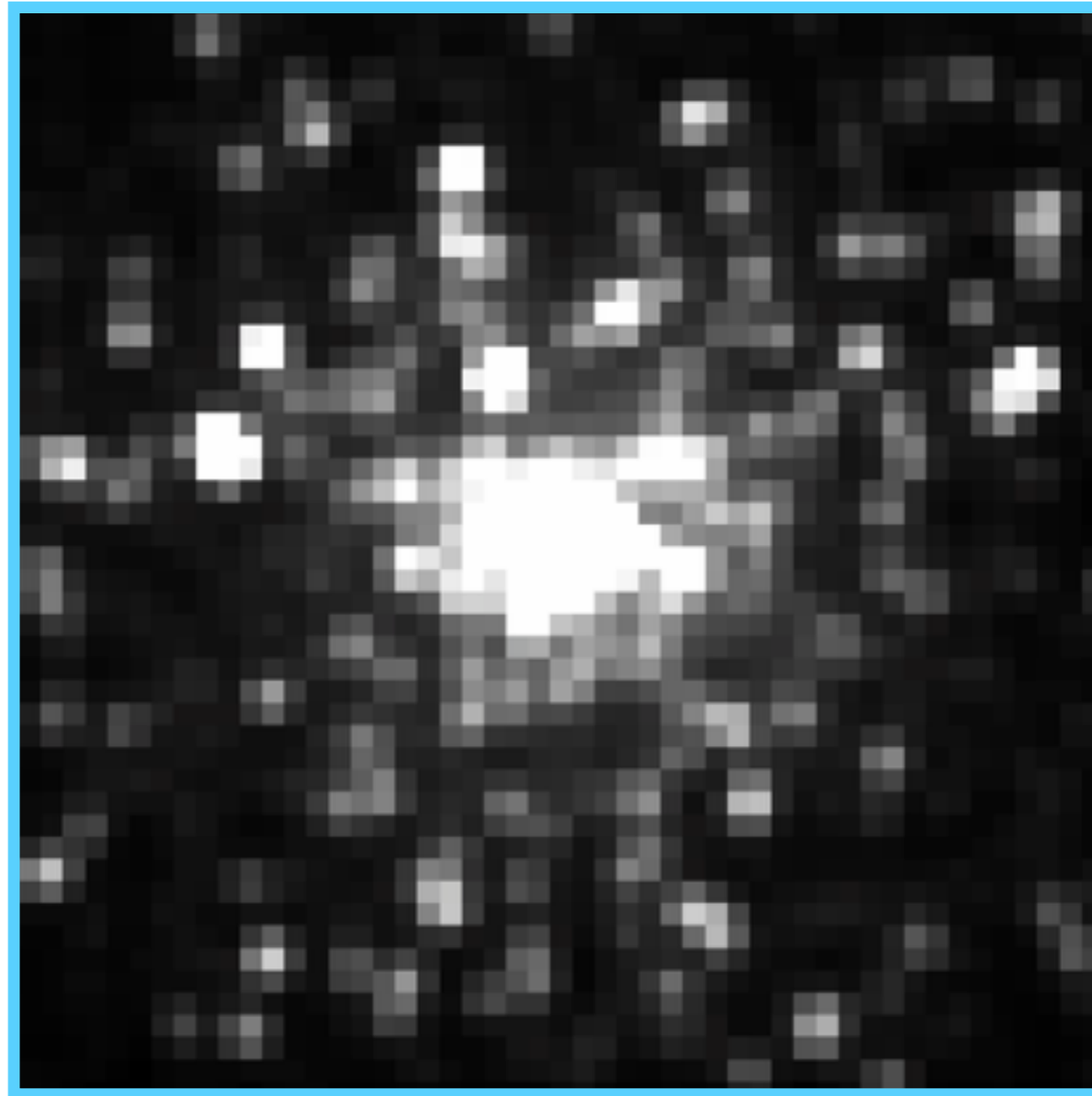
# N-BODY - SIMULATE



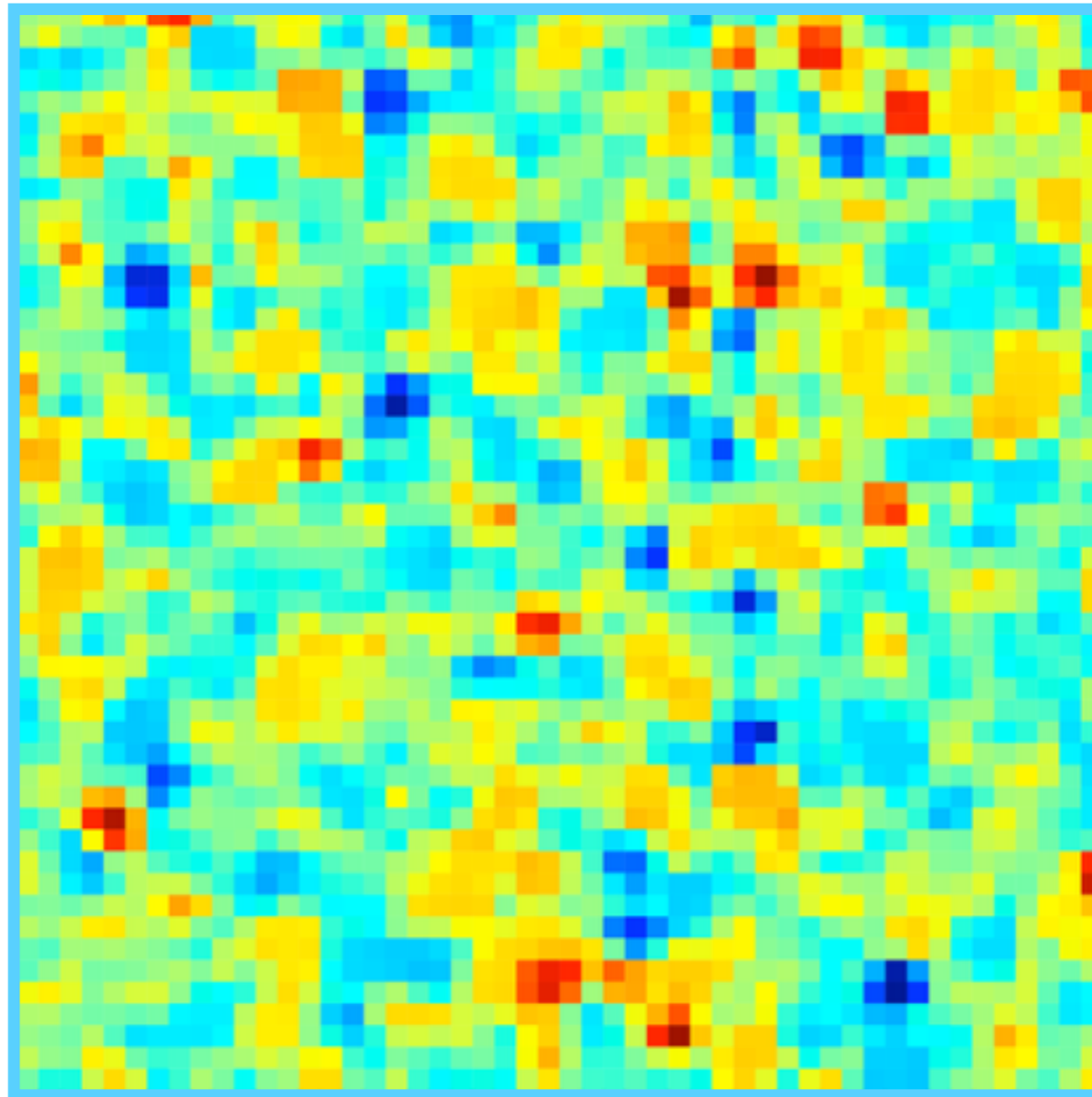
# **N**-BODY - SIMULATE



# N-BODY - SIMULATE

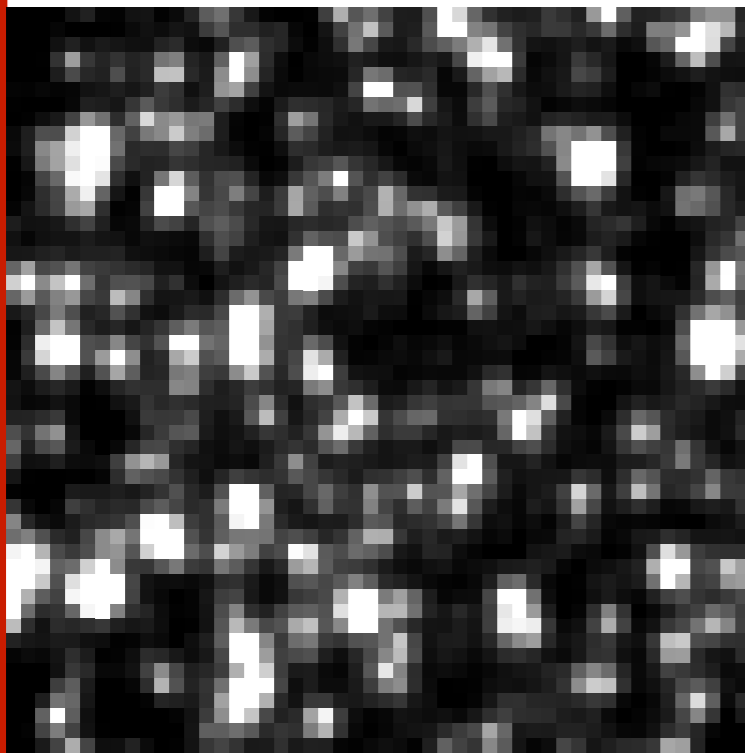


# N-BODY - SIMULATE

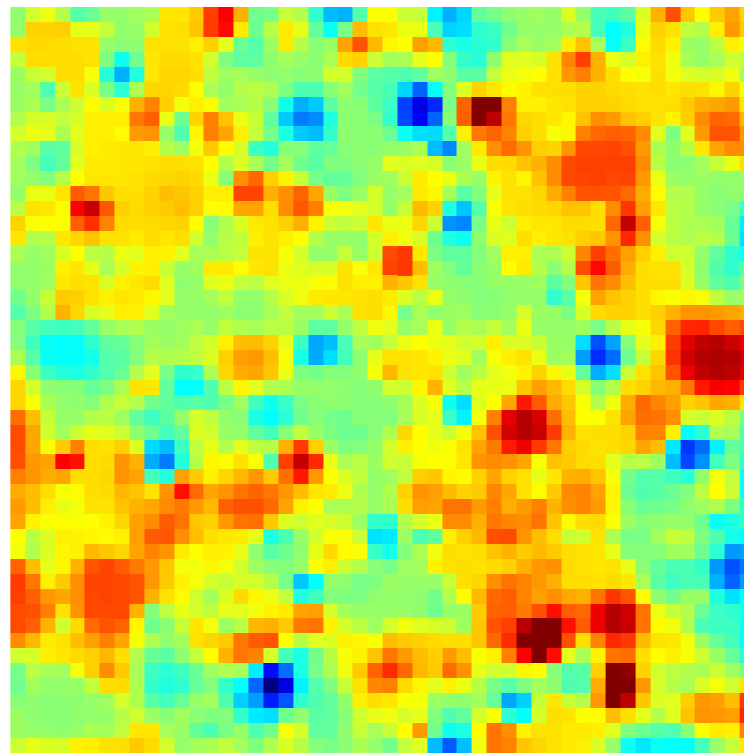


# N-BODY - SIMULATE

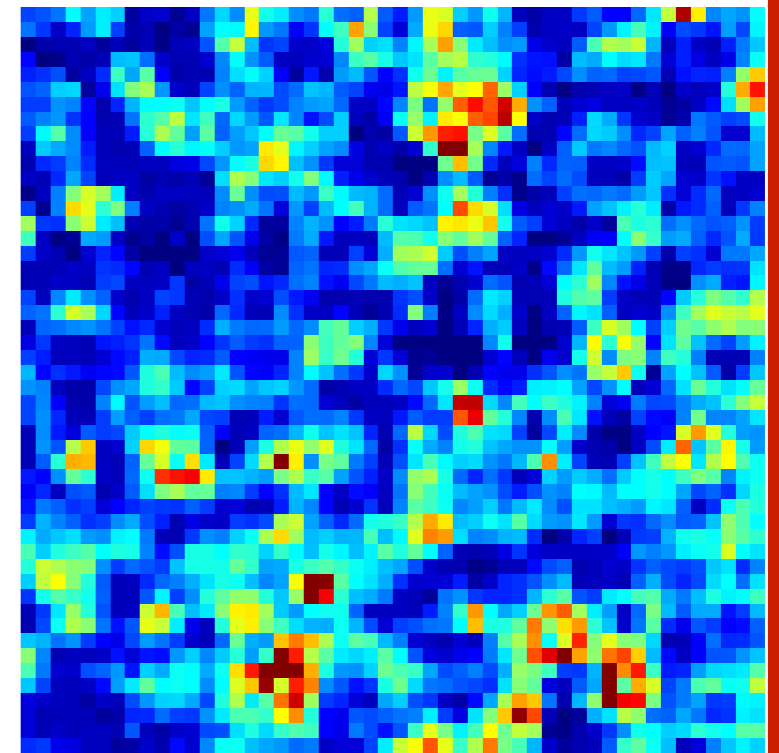
LIGHT



VELOCITY



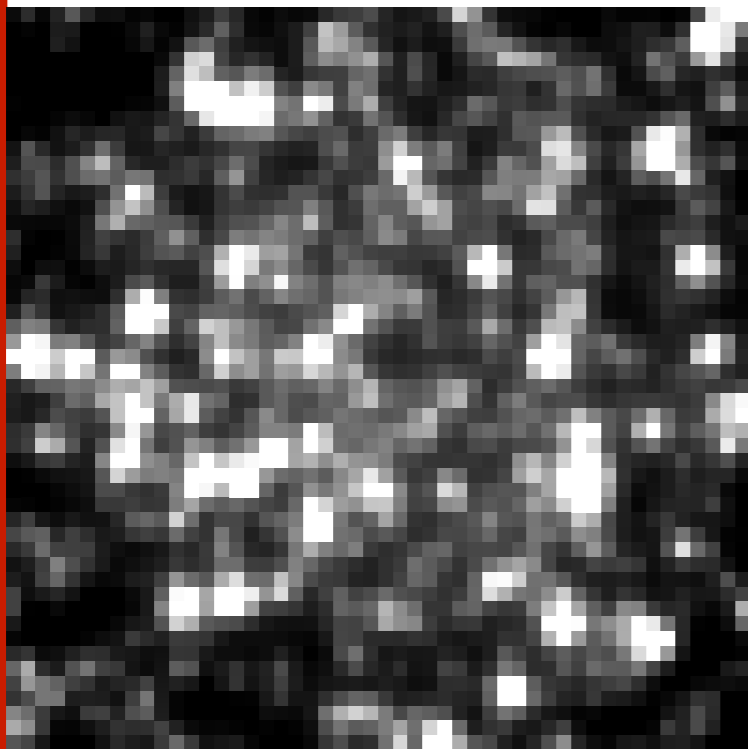
VELOCITY DISPERSION



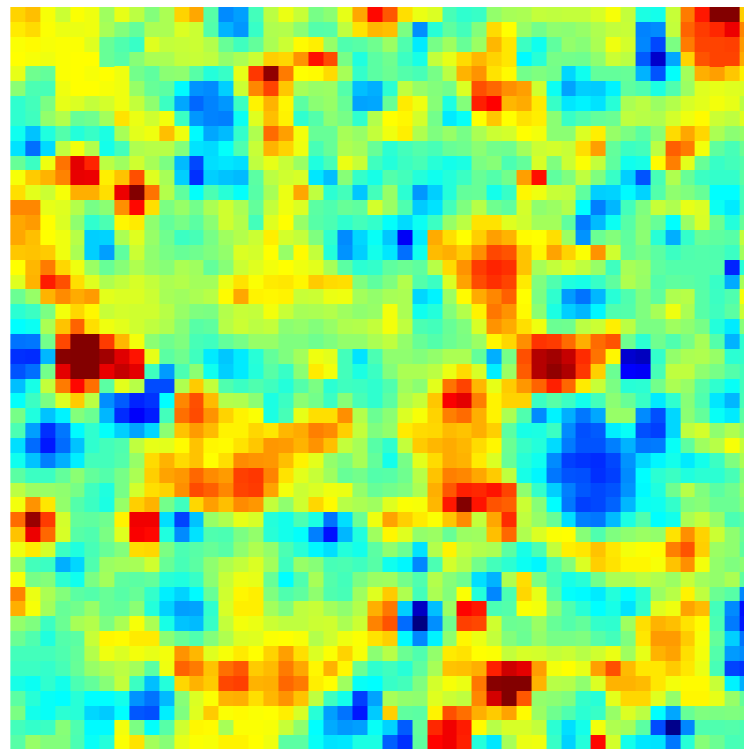
$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 5 \text{ kpc}, s = 1.0''$$

# N-BODY - SIMULATE

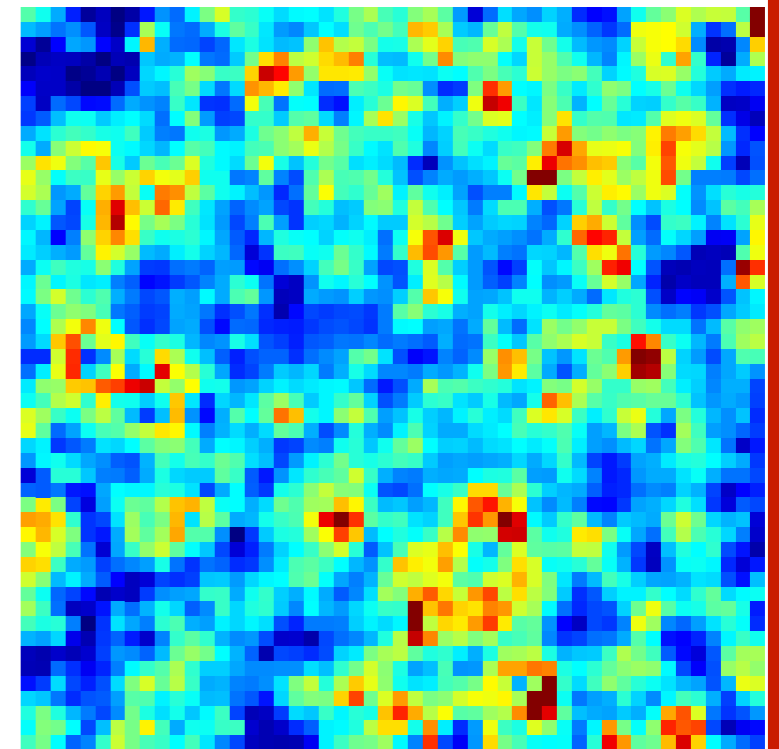
LIGHT



VELOCITY



VELOCITY DISPERSION

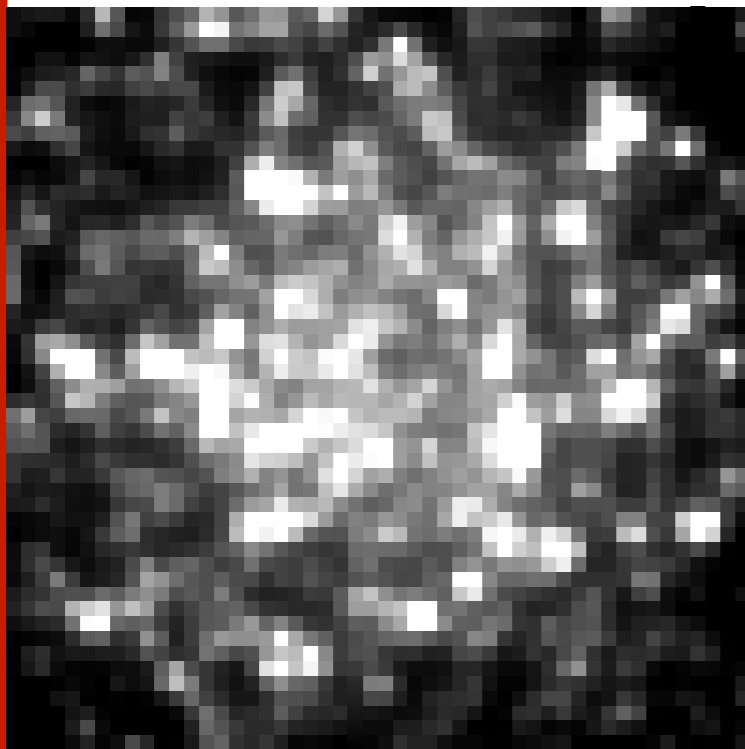


$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 10 \text{ kpc}, s = 1.0''$$

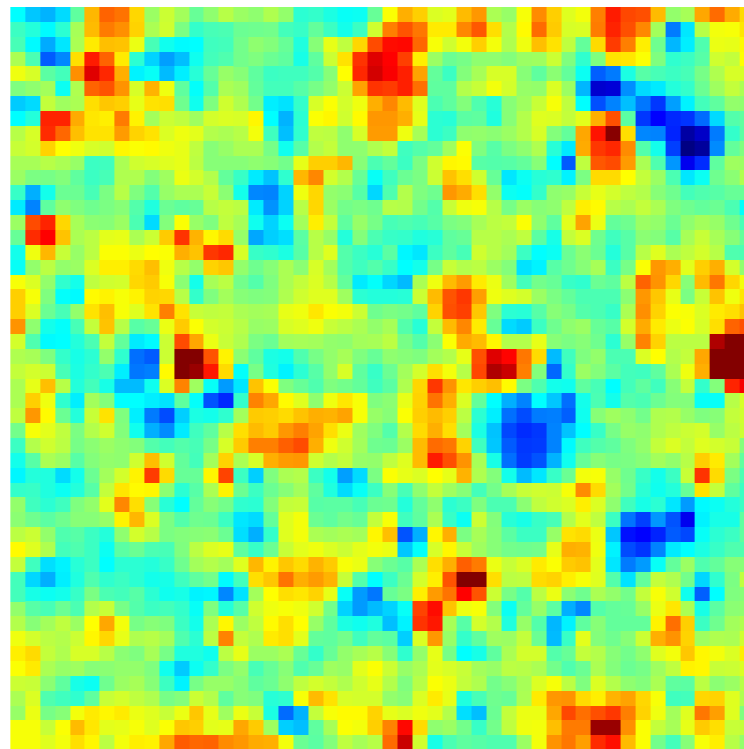


# N-BODY - SIMULATE

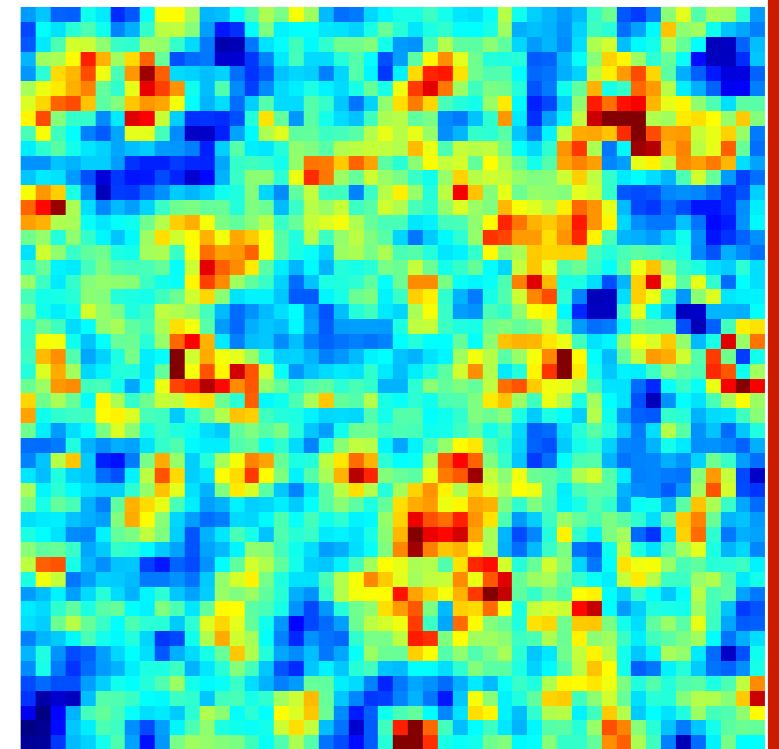
LIGHT



VELOCITY



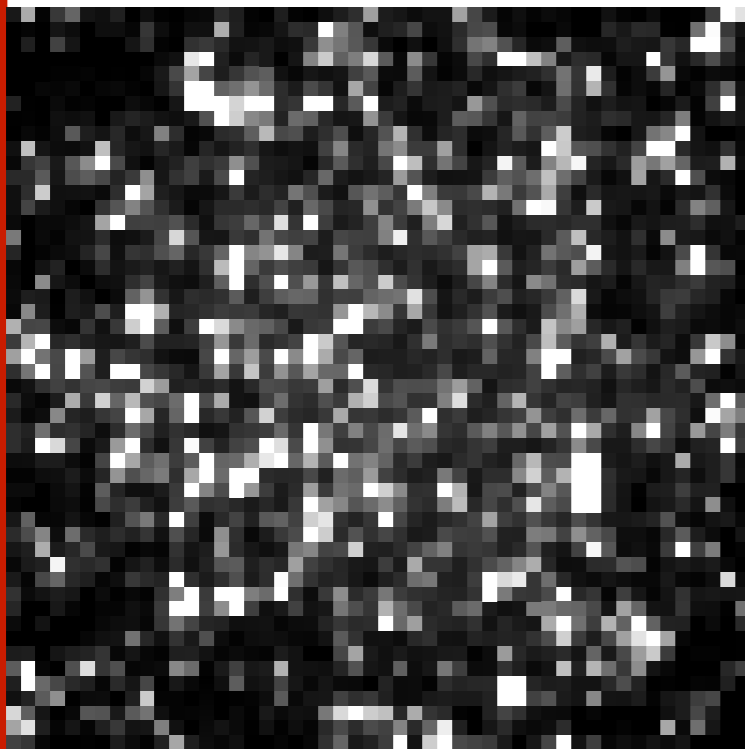
VELOCITY DISPERSION



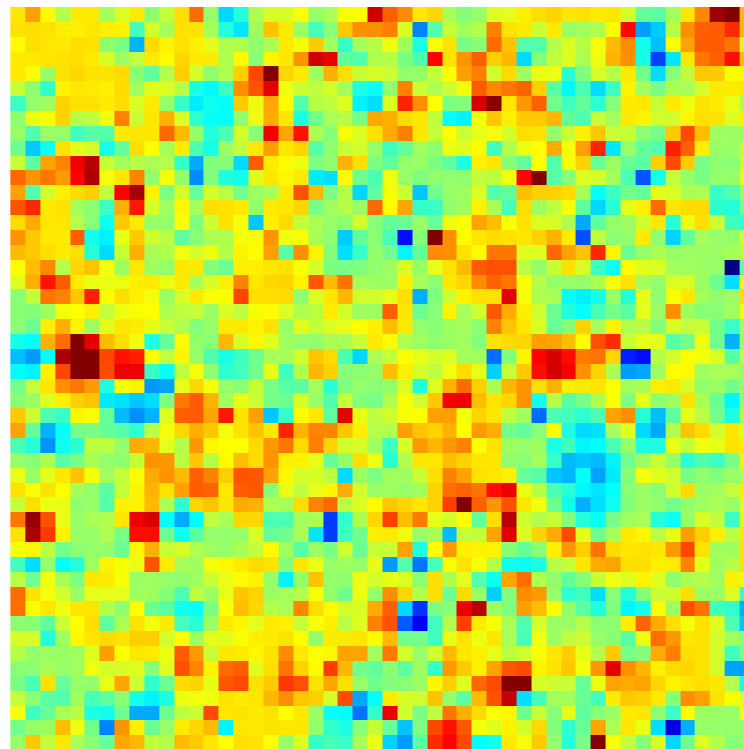
$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 15 \text{ kpc}, s = 1.0''$$

# N-BODY - SIMULATE

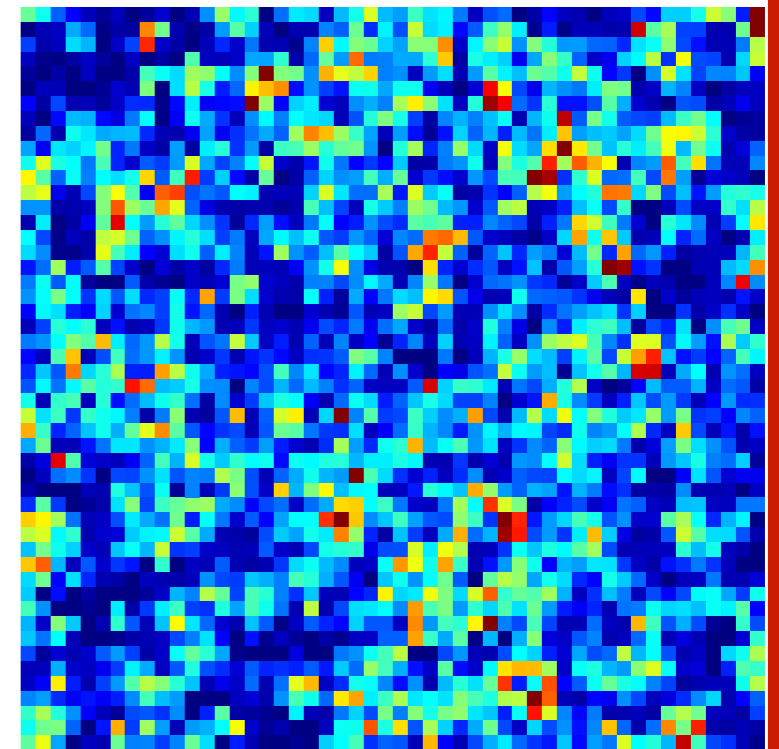
LIGHT



VELOCITY



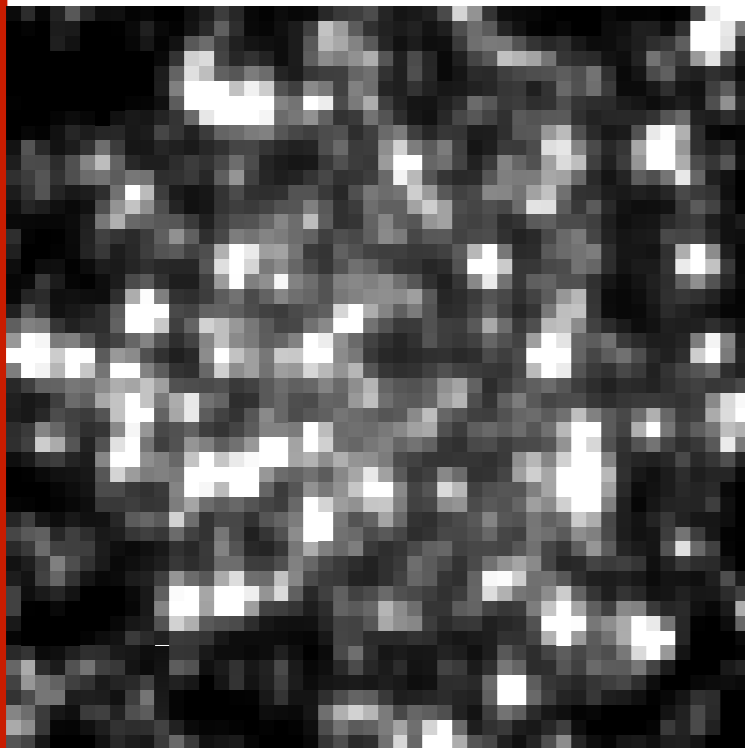
VELOCITY DISPERSION



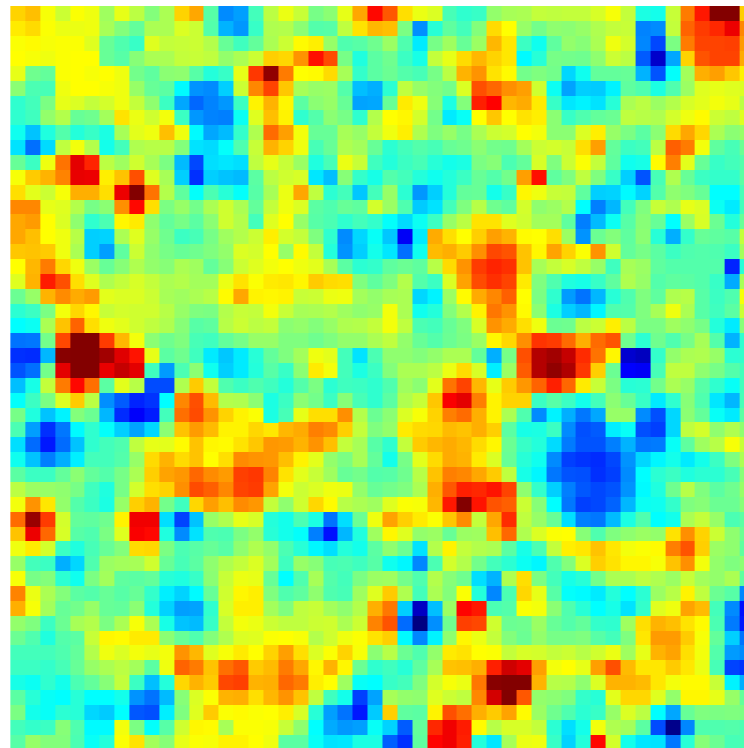
$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 10 \text{ kpc}, s = 0.5''$$

# N-BODY - SIMULATE

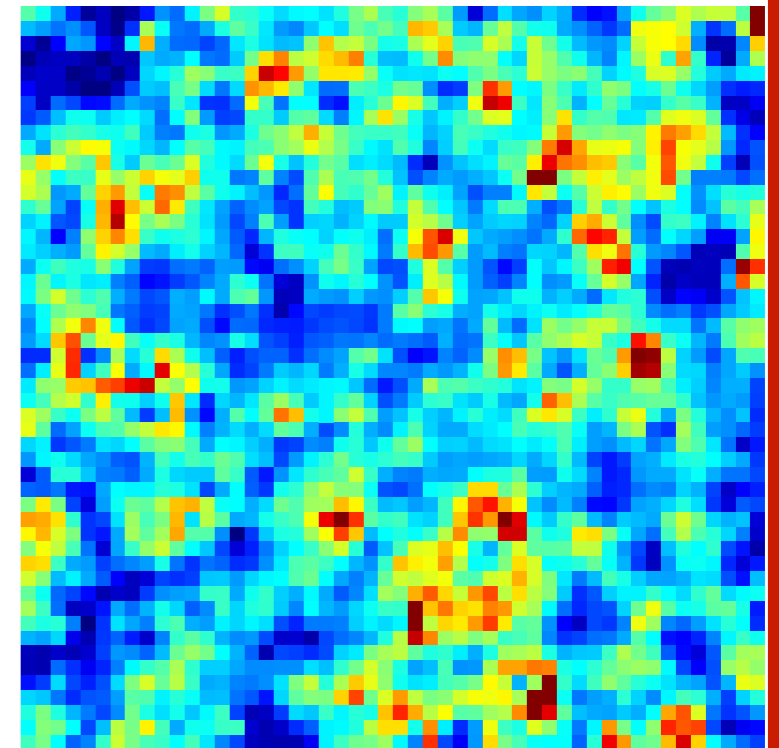
LIGHT



VELOCITY



VELOCITY DISPERSION

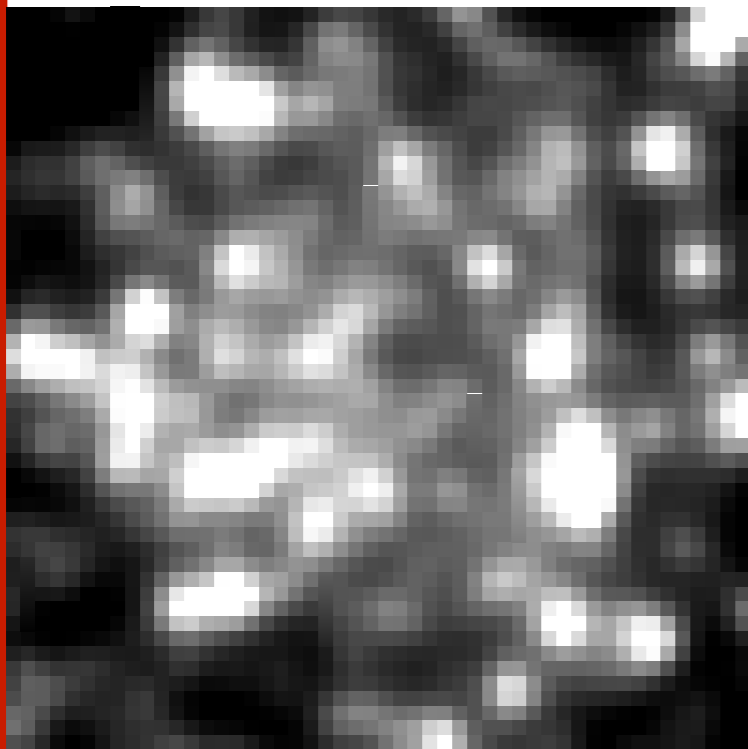


$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 10 \text{ kpc}, s = 1.0''$$

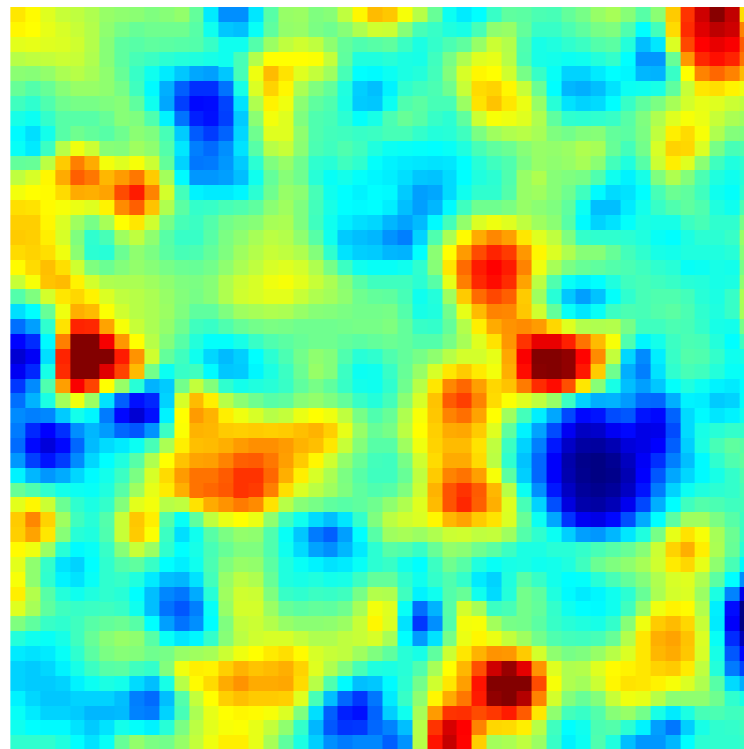


# N-BODY - SIMULATE

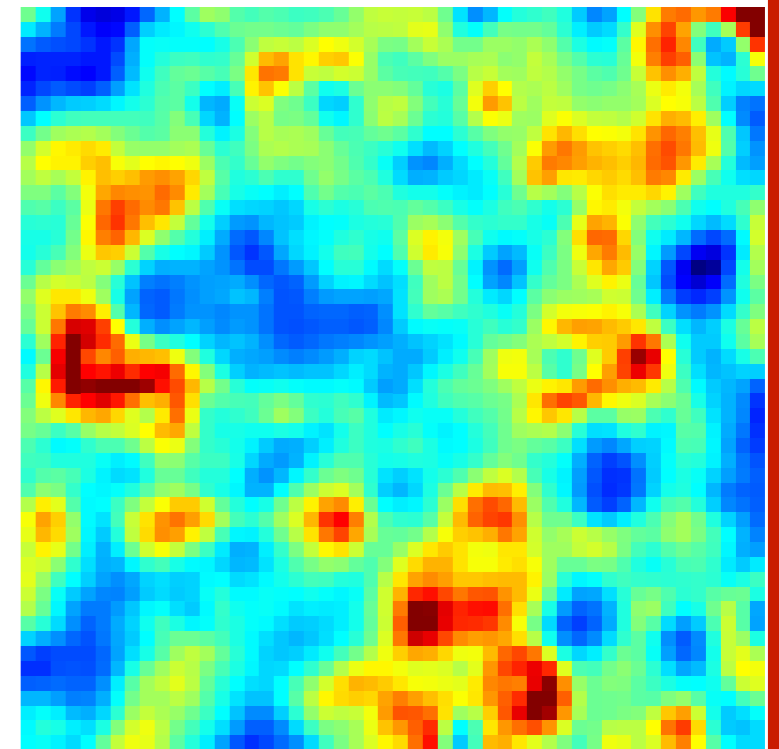
LIGHT



VELOCITY



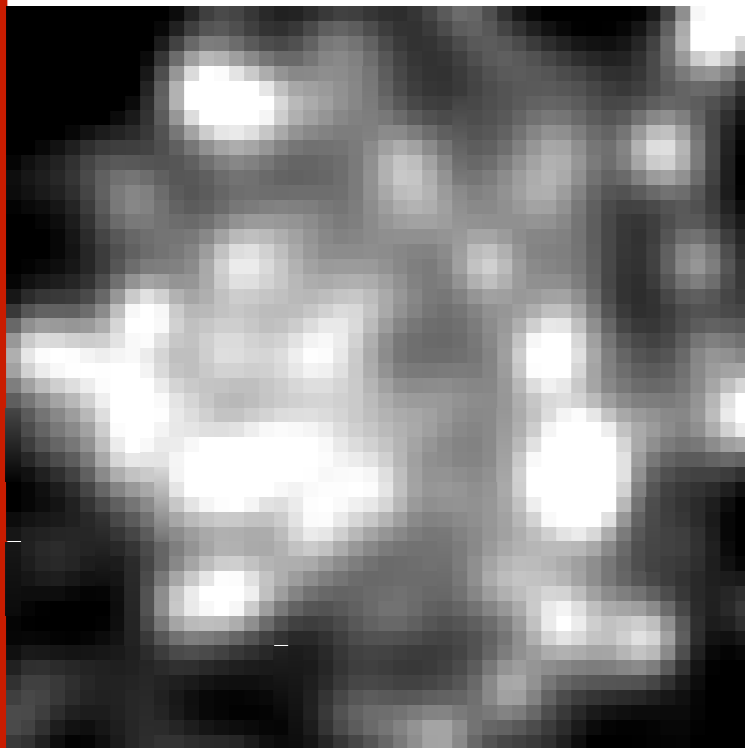
VELOCITY DISPERSION



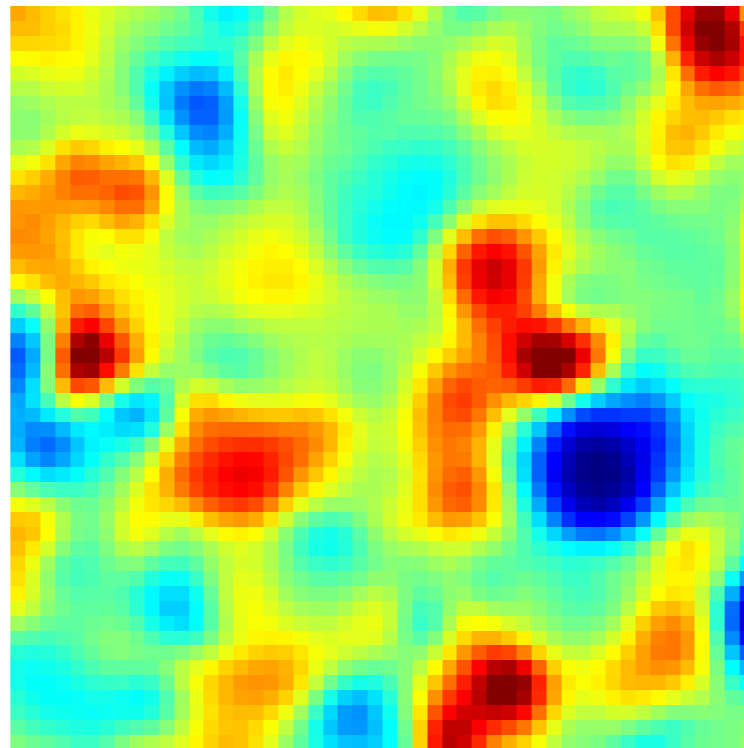
$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 10 \text{ kpc}, s = 2.0''$$

# N-BODY - SIMULATE

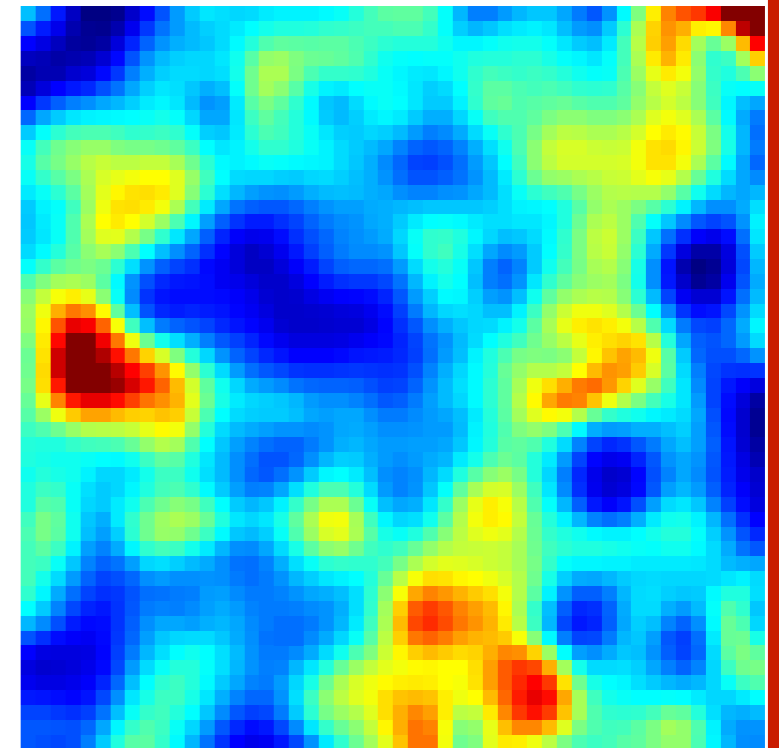
LIGHT



VELOCITY

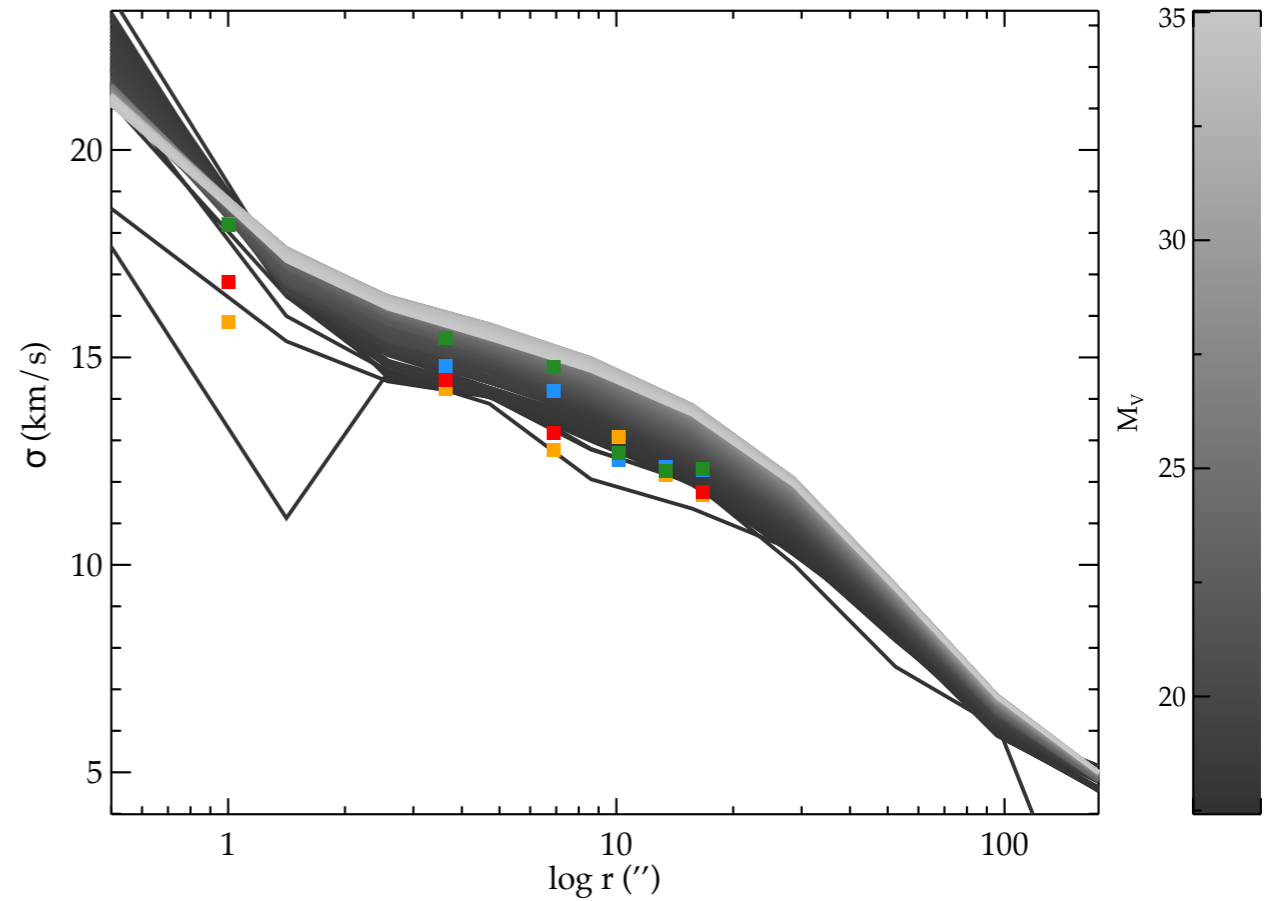
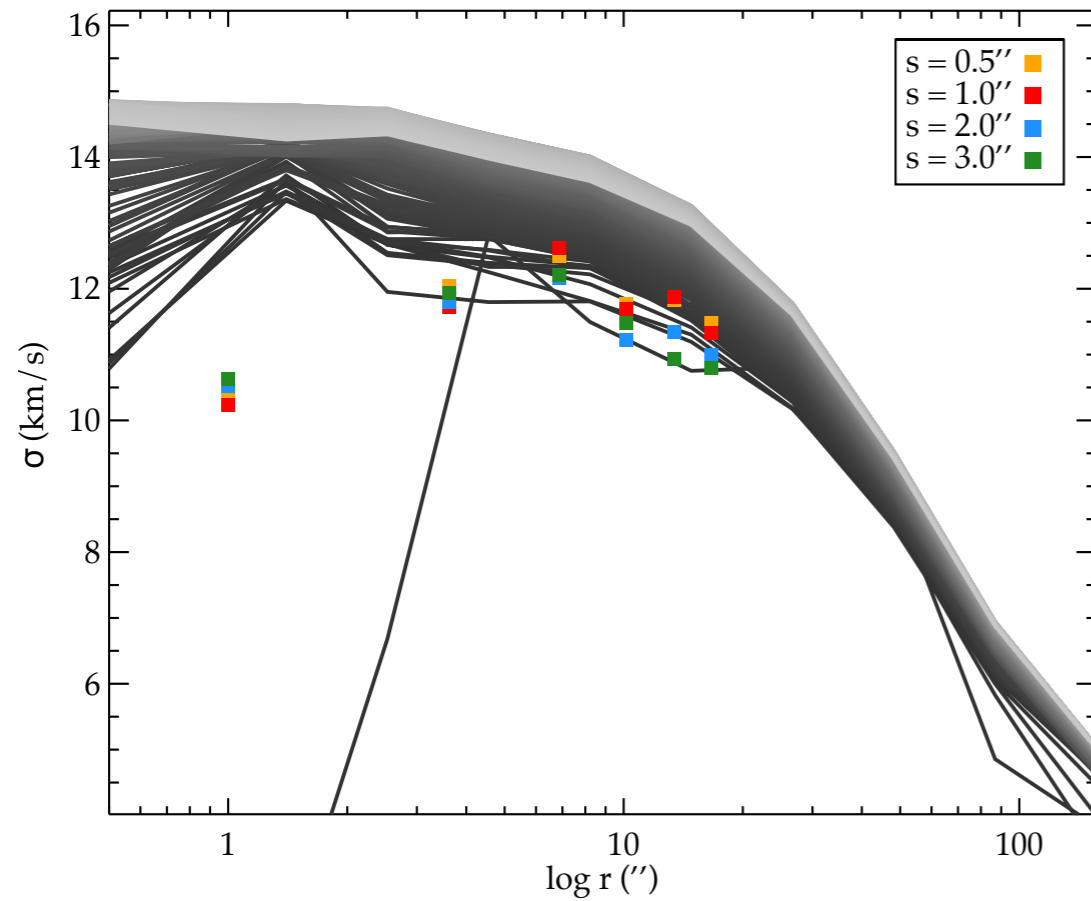


VELOCITY DISPERSION

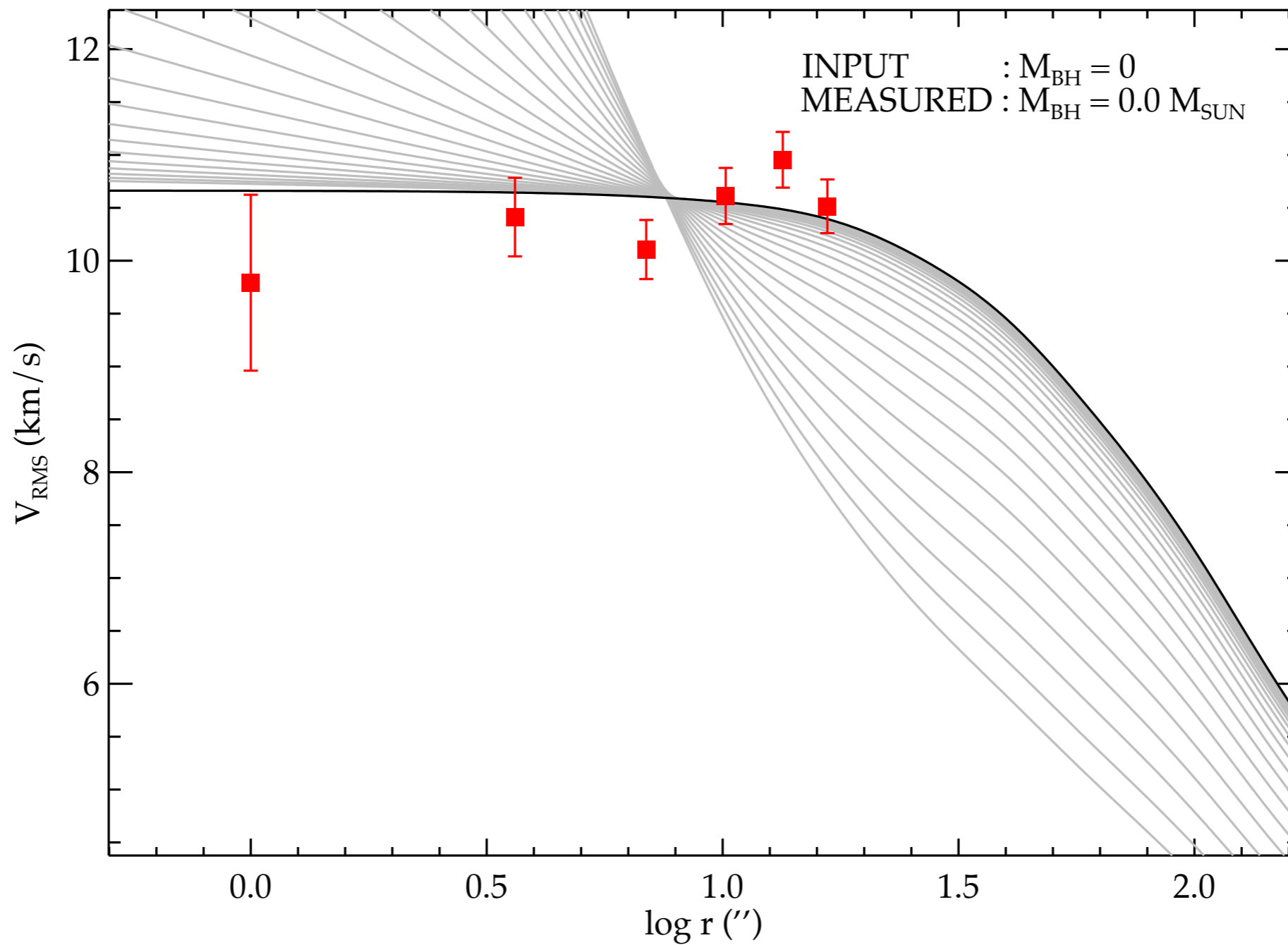


$$M_{\bullet} = 0, M = 10^6 M_{\odot}, d = 10 \text{ kpc}, s = 3.0''$$

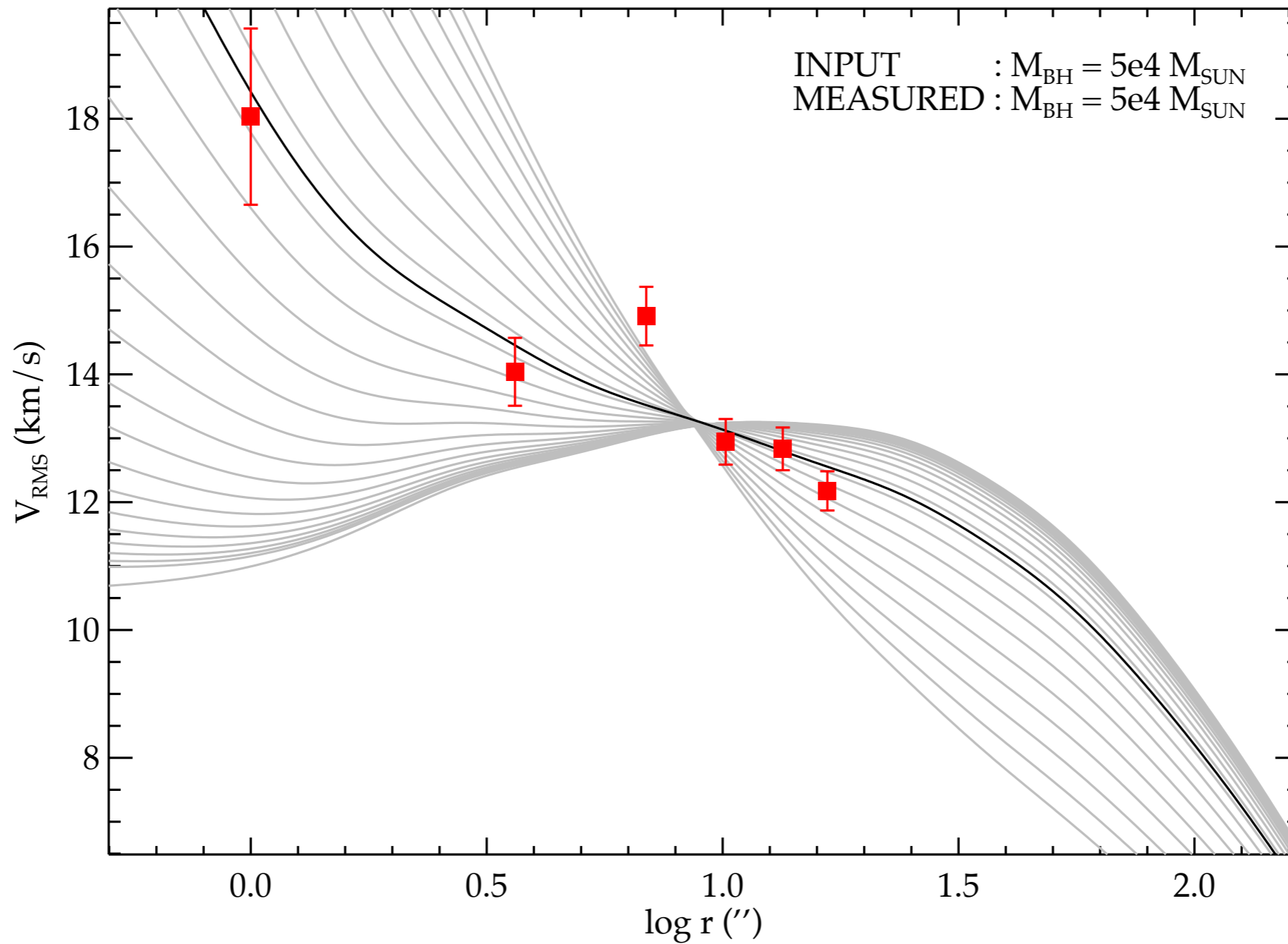
# N-BODY - SIMULATE



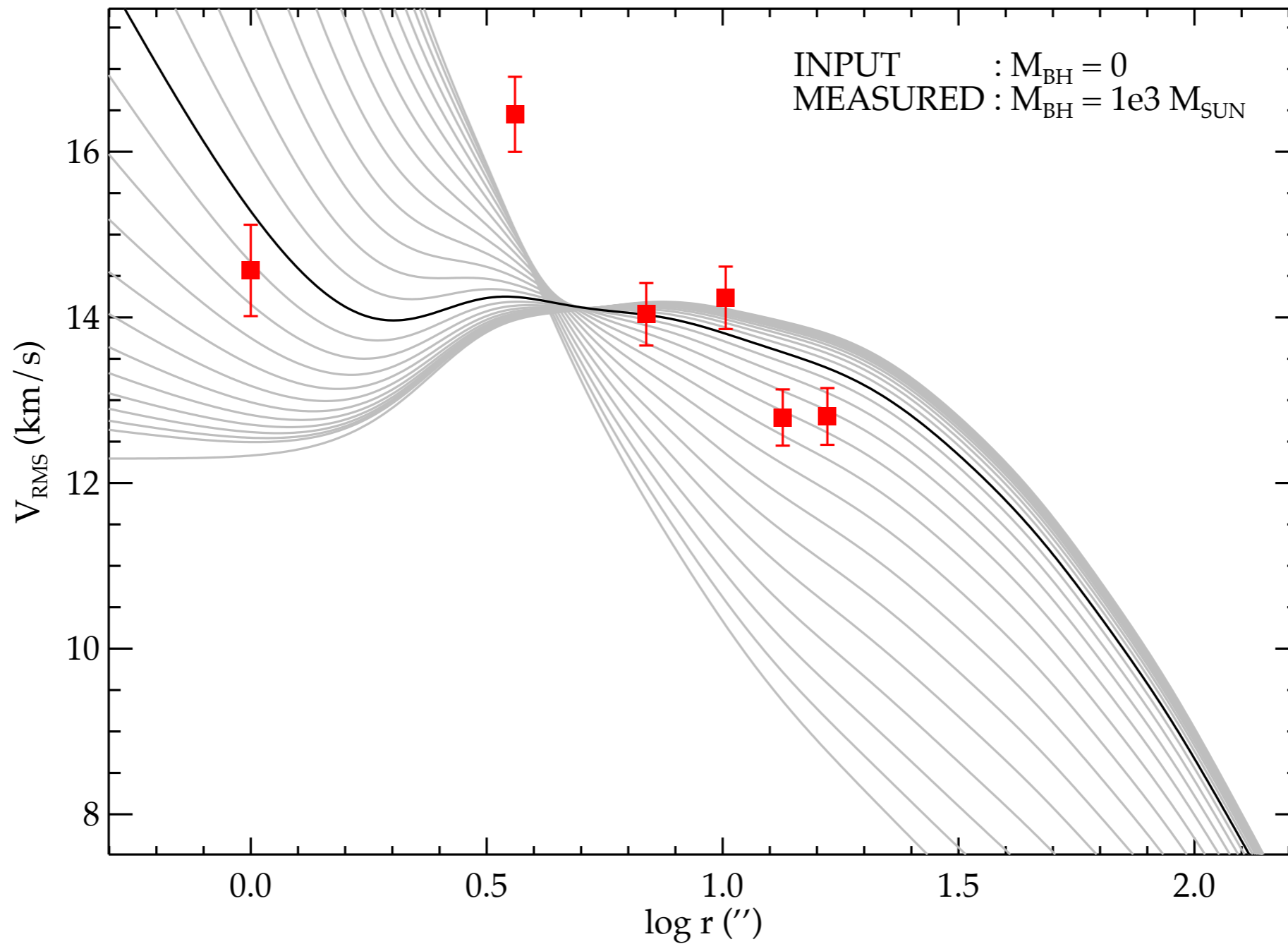
# N-BODY - SIMULATE



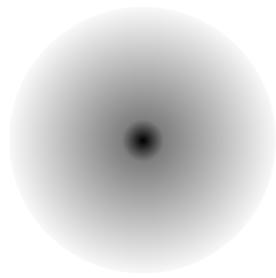
# N-BODY - SIMULATE



# N-BODY - SIMULATE



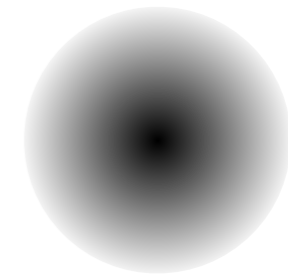
# N-BODY - FIND



← SMALLER

$$r_{10\%}/r_{50\%}$$

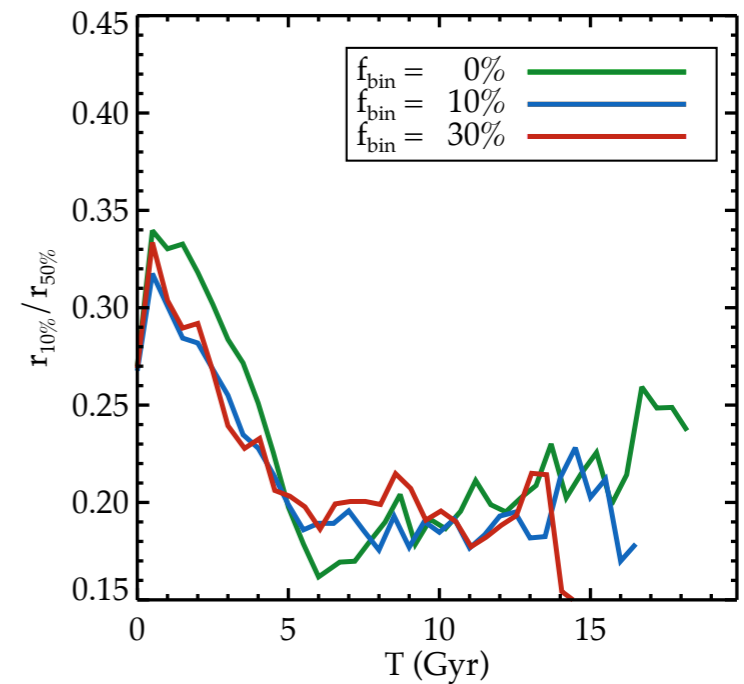
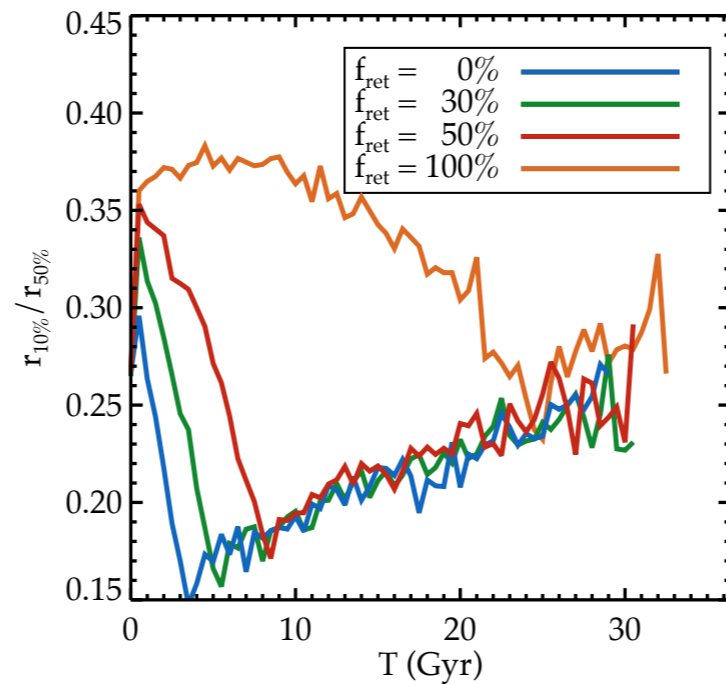
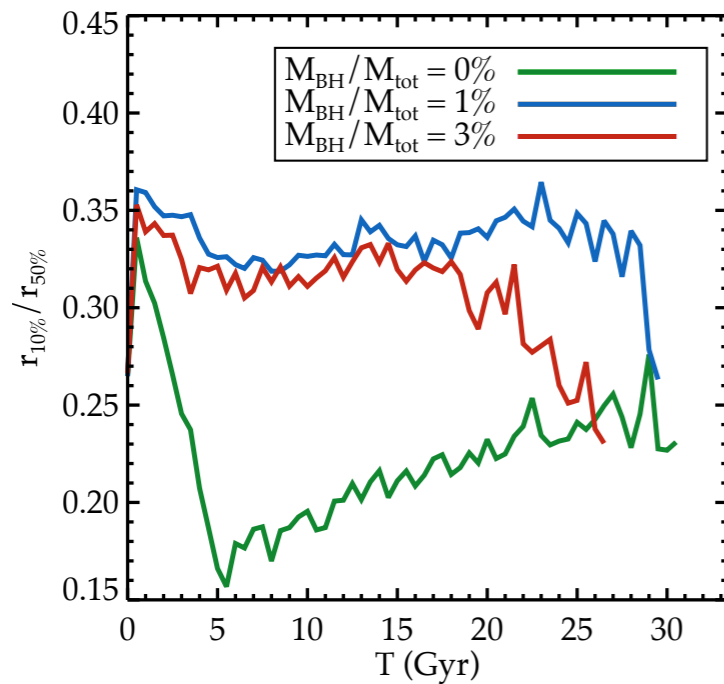
LARGER →



IMBH

STELLAR-MASS  
BLACK HOLES

BINARIES



Lützgendorf et al. 2013c



# Outline

## 1. Introduction

- What, How, Where?

## 2. Observations

- Photometry

- Spectroscopy

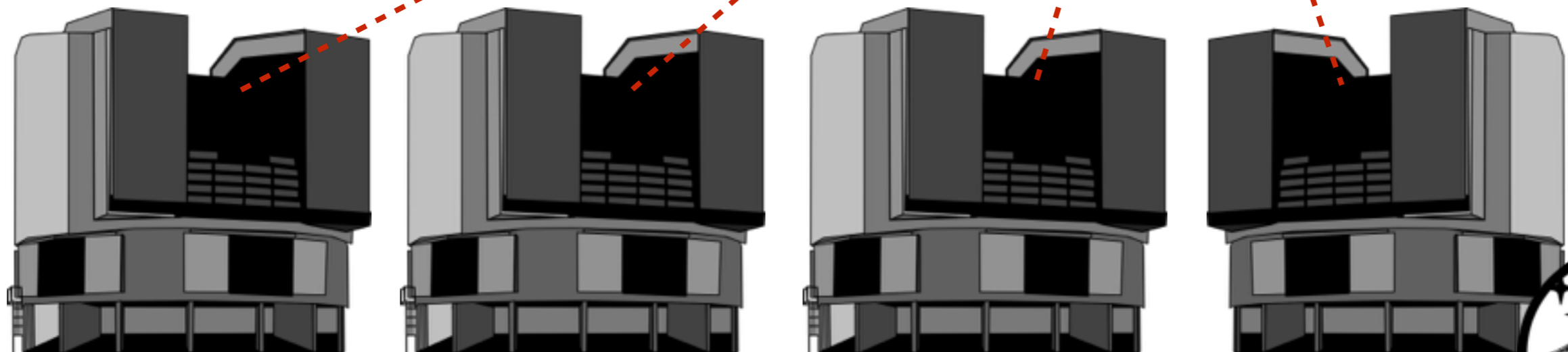
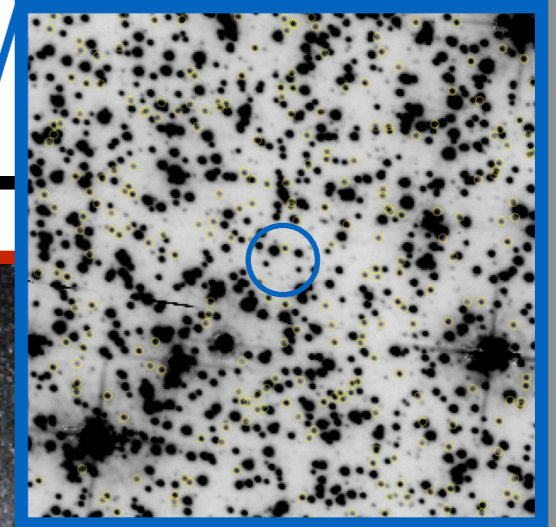
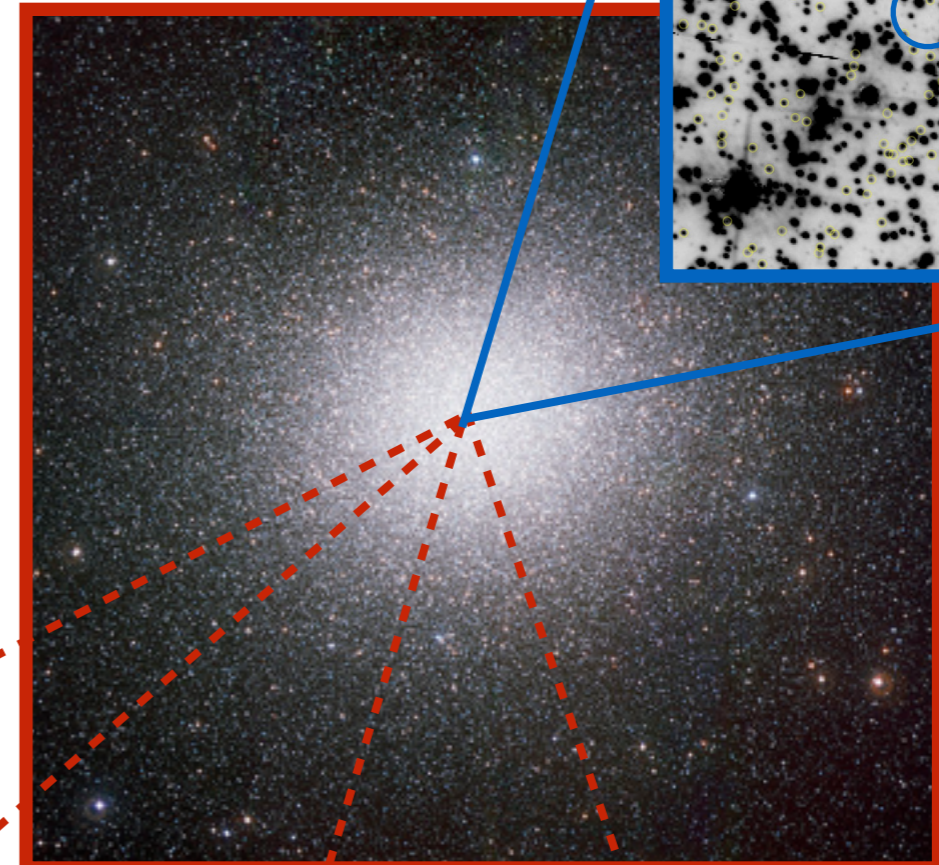
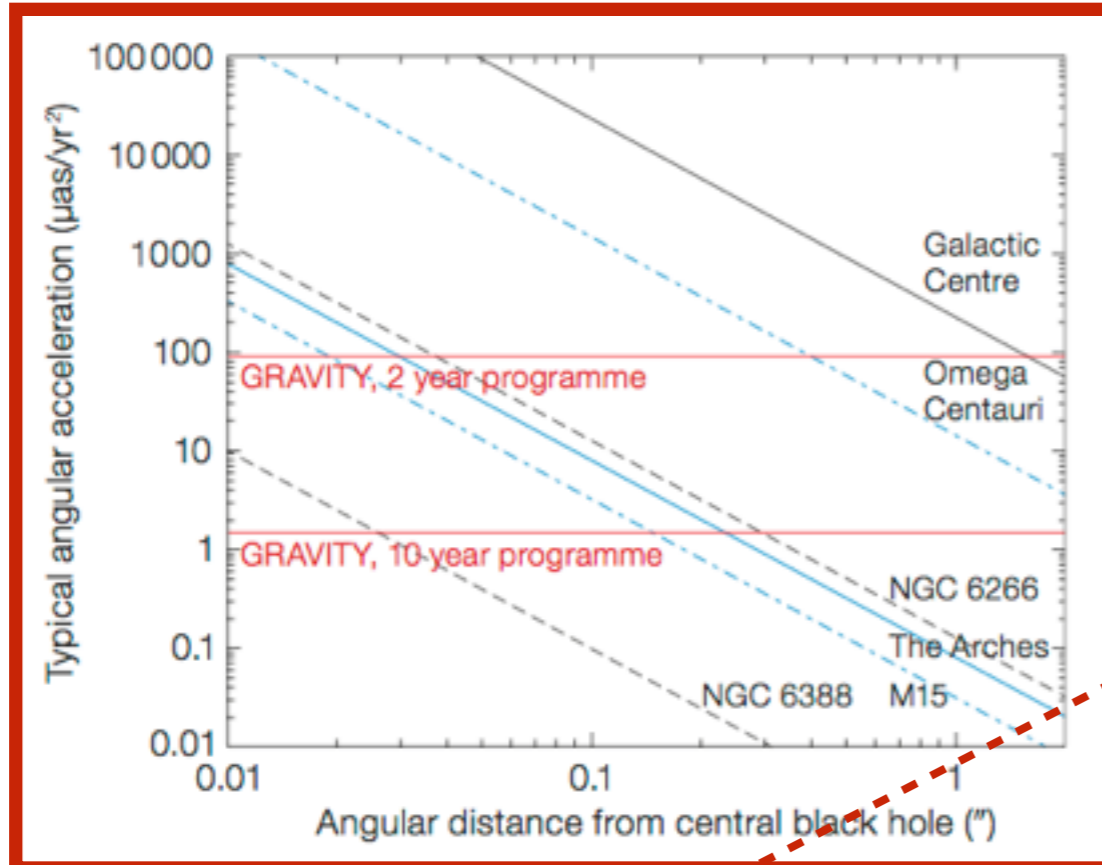
## 3. Simulations

## 4. Future



# Future - GRAVITY

F. Eisenhauer et al., 2011, Messenger



# Future - Simulations



How much accretion would we expect from an IMBH in a Globular Cluster?

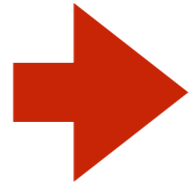


Simulate accretion from stellar winds onto the IMBH!

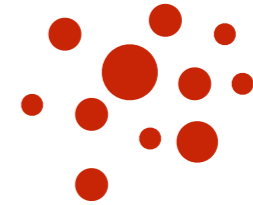


# Future - Simulations

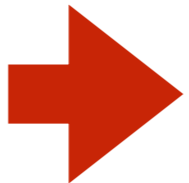
Simulate the Gravity



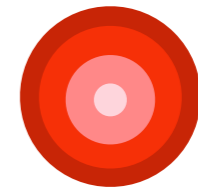
N-body Simulations



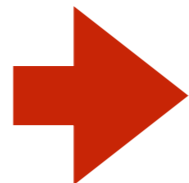
Simulate Stellar Evolution



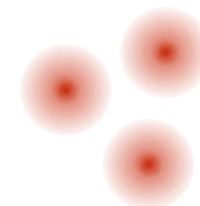
Stellar Evolution Codes



Simulate the Gas

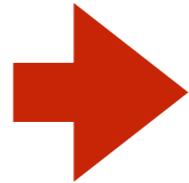


Smoothed Particle Hydrodynamics

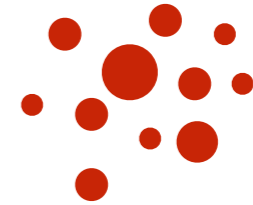


# Future - Simulations

Simulate the Gravity



N-body Simulations



Simulate Stellar Evolution



Stellar Evolution Codes



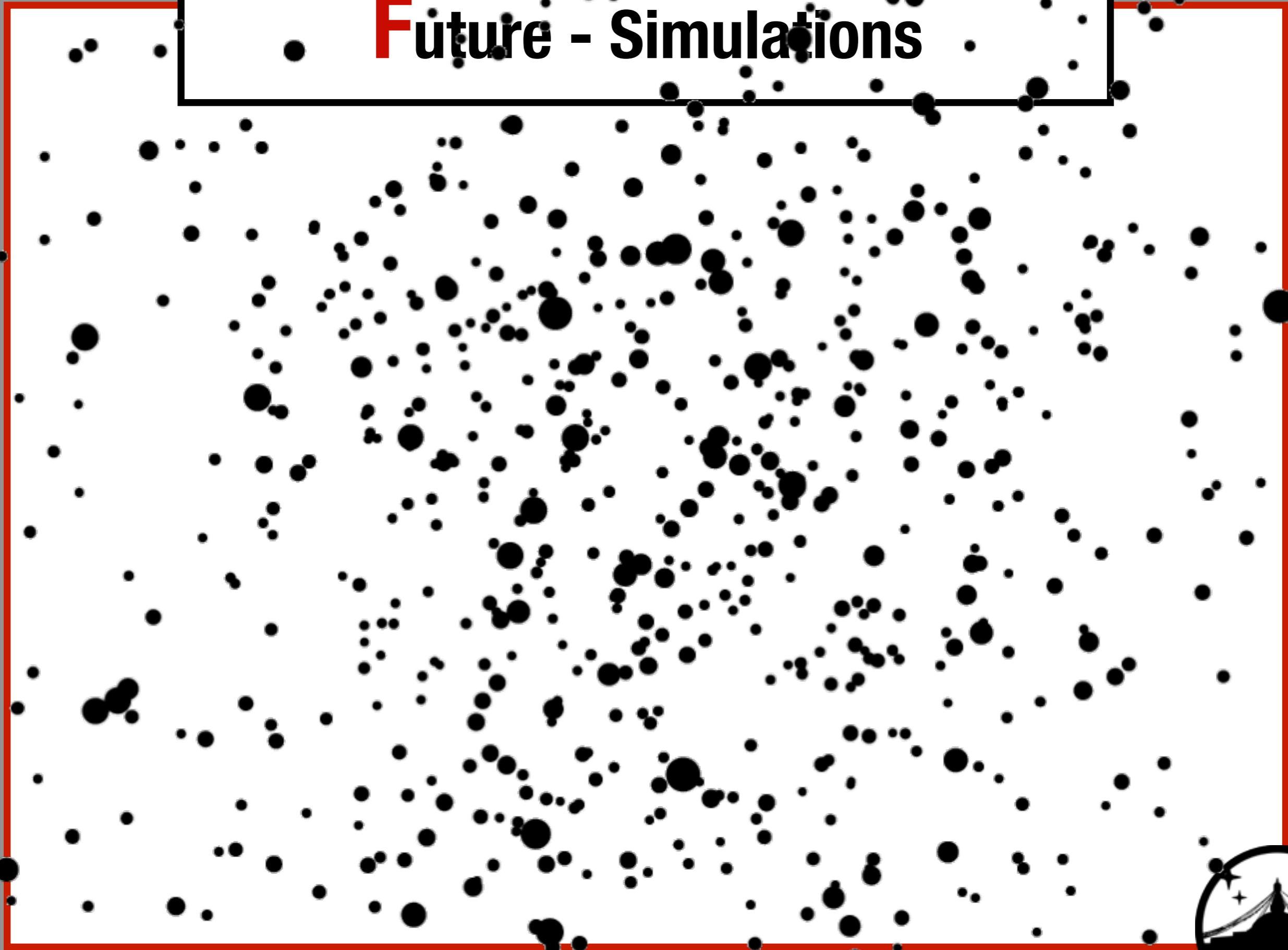
Simulate the Gas



Smoothed Particle Hydrodynamics



# Future - Simulations



# Future - Simulations

Simulate the Gravity



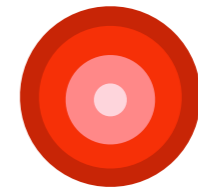
N-body Simulations



Simulate Stellar Evolution



Stellar Evolution Codes



Simulate the Gas



Smoothed Particle Hydrodynamics



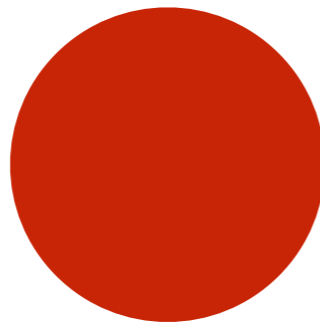
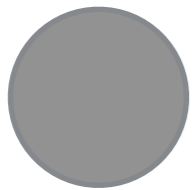
# Future - Simulations

$< 0.8 M_{\odot}$



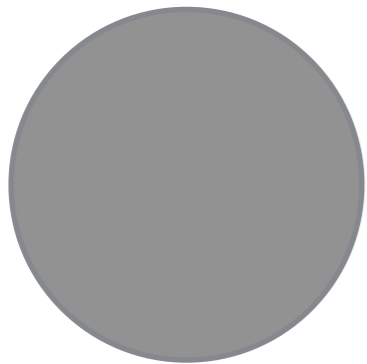
BLACK DWARF

$\sim 1 M_{\odot}$



PLANETARY  
NEBULAR

$10 - 100 M_{\odot}$



NEUTRON STAR



BLACK HOLE



# Future - Simulations

Simulate the Gravity



N-body Simulations



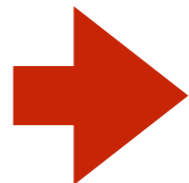
Simulate Stellar Evolution



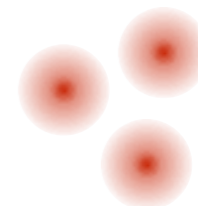
Stellar Evolution Codes



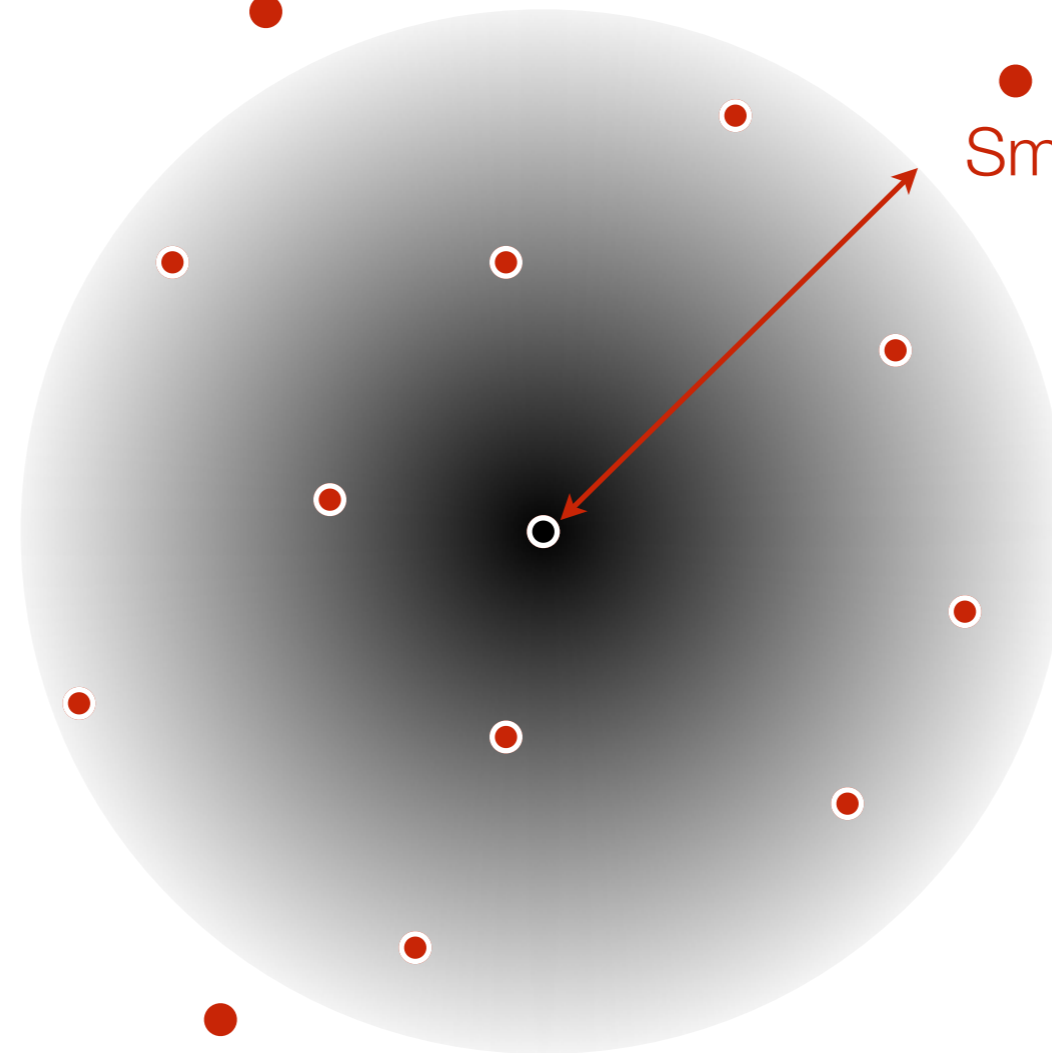
Simulate the Gas



Smoothed Particle Hydrodynamics



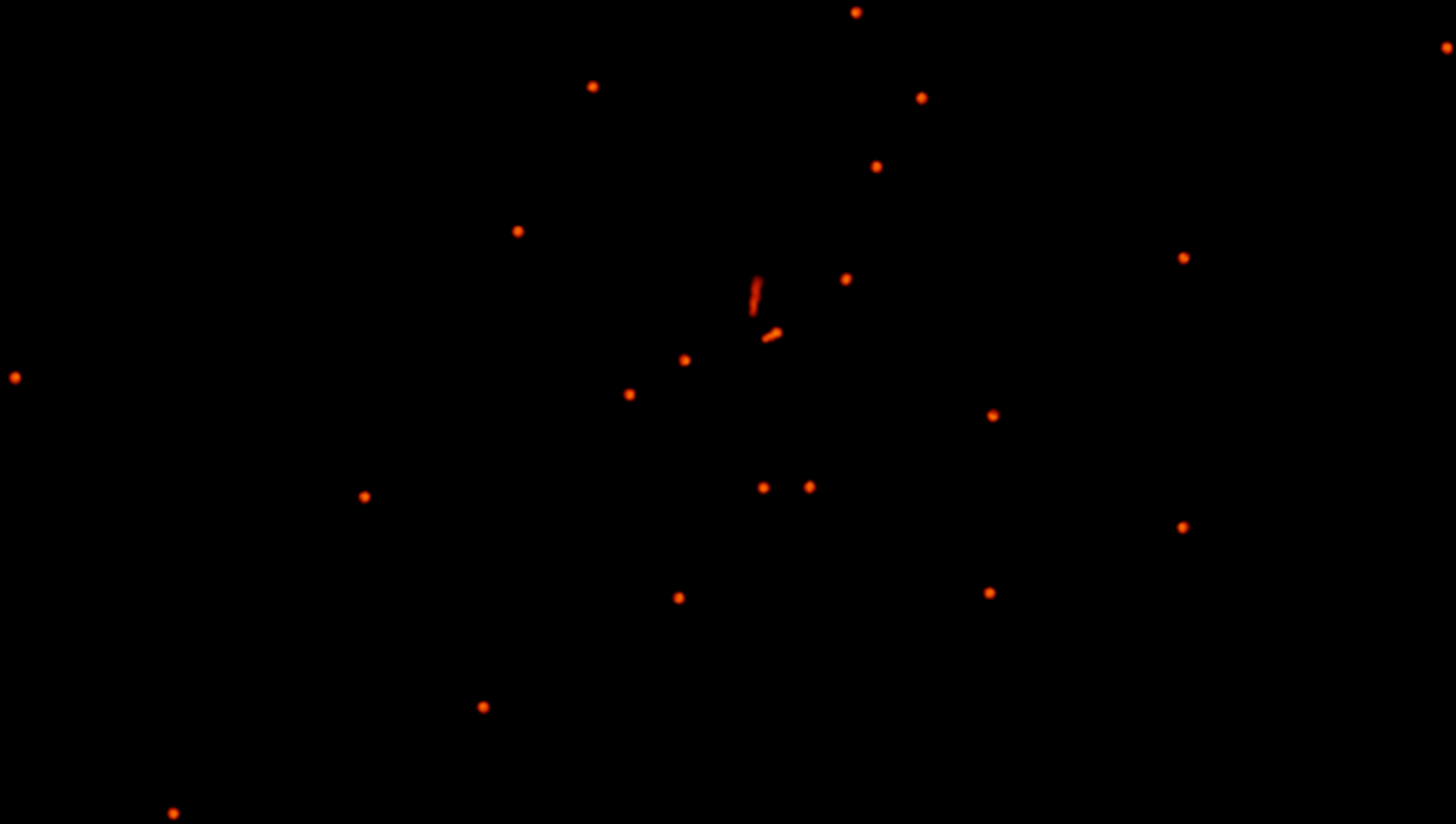
# Future - Simulations



Smoothing Length  $h$



# Future - Simulations



# Summary

## 1. Intermediate-mass black holes

- $10^2 - 10^4 M_{\text{SUN}}$
- could explain how SMBH grow

## 2. Observations

- Photometry:  $\rightarrow$  get surface brightness profile
- Spectroscopy: Integral Field Units (IFU)  $\rightarrow$  get velocities
- Compare to Jeans models

## 3. N-body Simulations

- compare to data, simulate data, find new observables

## 4. Future

- GRAVITY - Interferometer to measure accelerations



# FINAL SUMMARY

## 1. Star Clusters

- OB associations, Embedded Clusters, Open Clusters, **Globular Clusters**, Nuclear Clusters

## 2. Multiple Stellar Populations (MSP)

- **Spectroscopic** and **photometric** evidence for MSP
- Explanations still flawed

## 3. Kinematics

- Gravitational systems have **negative heat capacity**
- Consequences: **core collapse, mass segregation**

## 4. Intermediate-mass black holes

- **Black hole hunt**: Photometry and Spectroscopy
- Simulations to understand observations

